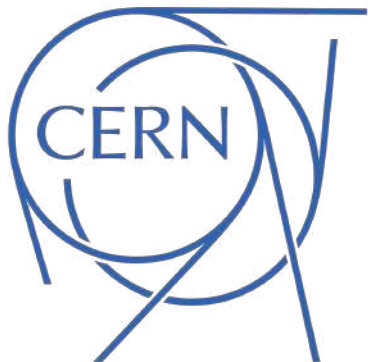


xFitter Tutorial

Francesco Giuli

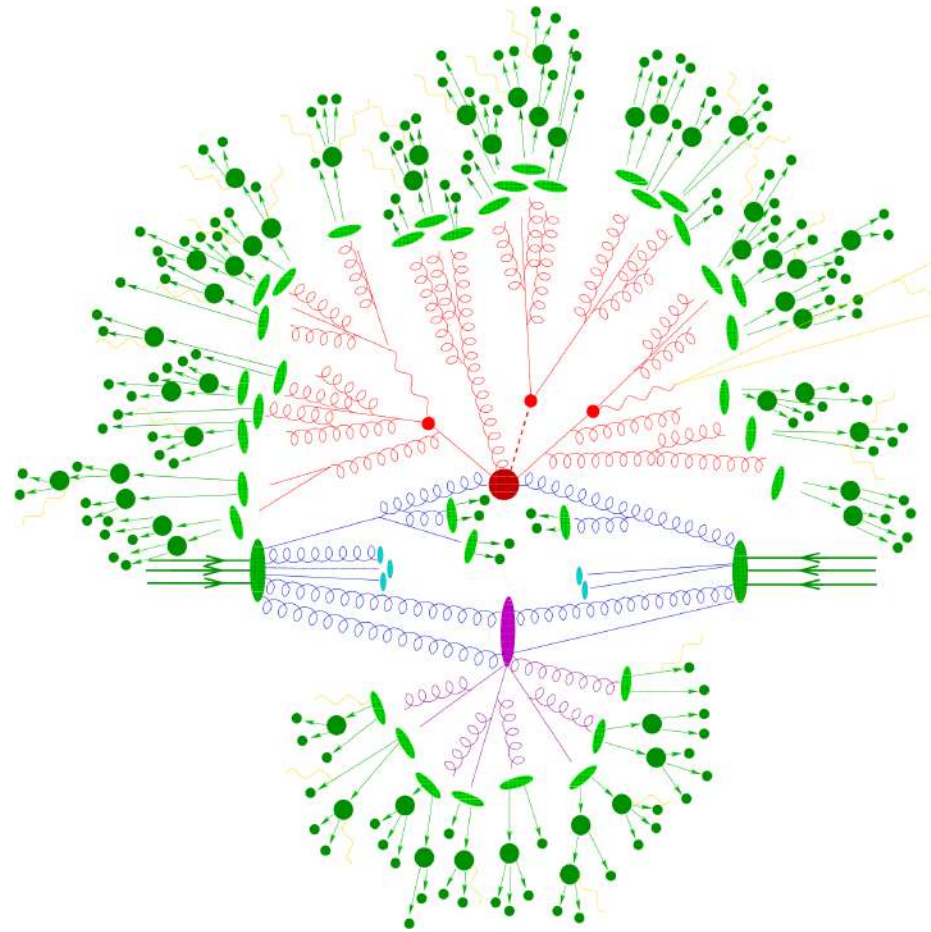
ATLAS SM workshop (Prague, Czech Republic)

14/09/2023



Motivation

- No new physics found at the LHC so far ☹
- Need for precise measurement of SM processes
- This means accurate higher order (HO) calculations...
- ... but also precise knowledge of **Parton Distribution Functions (PDFs)**
- Proton-proton collision at the LHC
- For simplicity, let's consider **Deep Inelastic Scattering (DIS)** process - just one incoming parton
- pp and $p\bar{p}$ collisions will be considered in the exercises



Factorisation theorem

$$\sigma_{DIS}(x, Q^2) = \int_x^1 \frac{dz}{z} C_i(z, \alpha_s(Q^2)) f_i\left(\frac{x}{z}, Q^2\right) = C_i \otimes f_i$$

Partonic cross sections:

- Process dependent
- High-scale (short-distance) objects
- Computable in perturbation theory (LO, NLO, NNLO, N³LO)

PDFs:

- Universal (process independent)
- Low-scale (long-distance) objects
- Non computable in perturbation theory
- Scale dependence perturbative (DGLAP)

➤ Once PDFs have been **determined at a given scale**, the **DGLAP** evolution equations can be used to **evolve them to any other scale**

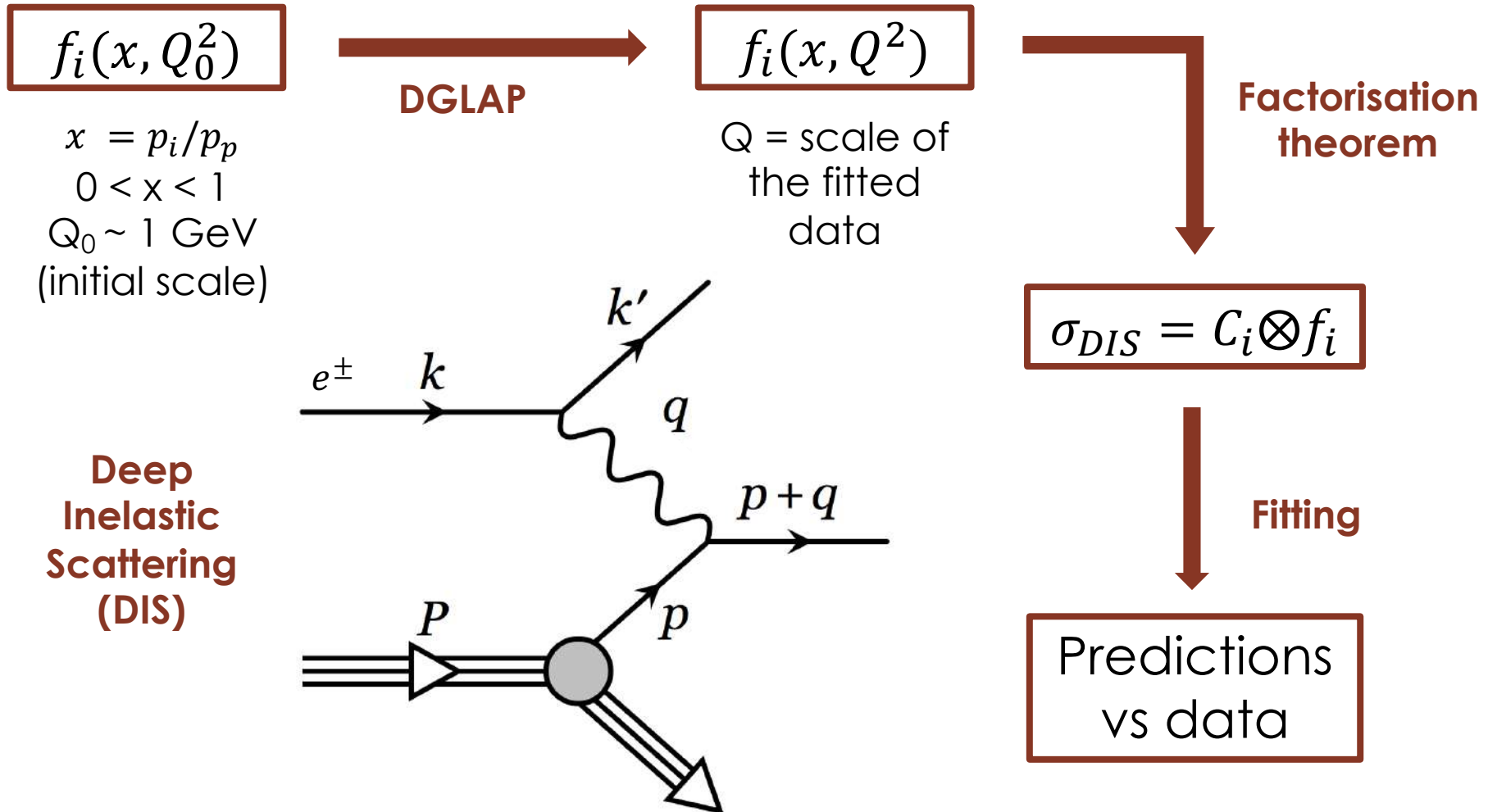
$$\mu^2 \frac{\partial}{\partial \mu^2} f_i(\mu) = P_{ij} \otimes f_j(\mu)$$

$$P_{ij}(y) = \frac{\alpha_s(\mu)}{2\pi} P_{ij}^{(0)}(y) + \left(\frac{\alpha_s(\mu)}{2\pi}\right)^2 P_{ij}^{(1)}(y) + \dots$$

Splitting functions

How do we determine PDFs?

- Presently, the most accurate and reliable way is through **fits to data**



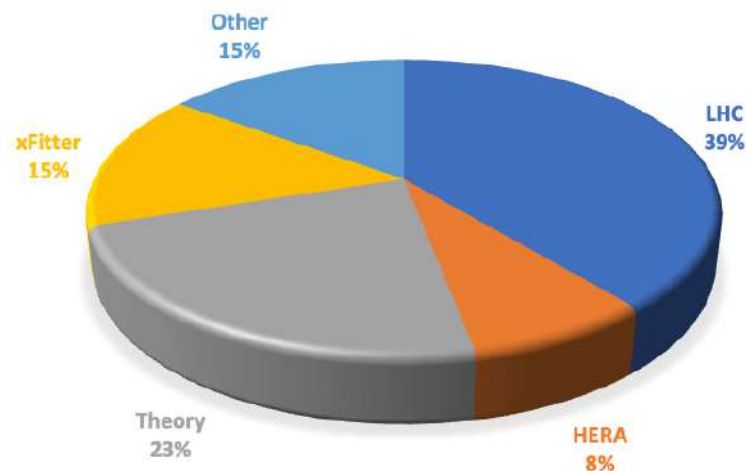
The xFitter Project

➤ The [xFitter](#) project (former HERAFitter) is a **unique open-source QCD fit framework**

➤ [GitLab](#) repository ([open access](#))

➤ This code allows users to:

- **extract PDFs** from a large variety of data
- assess the **impact** of **new data on PDFs**
- check the **consistency** of experimental data
- test different **theoretical assumptions**



➤ Several active developers between experimentalists and theorists

➤ More than [100 publications](#) obtained using xFitter since the beginning of the project

➤ List of recent analyses by the xFitter Developers' Team:

MORE IN PREPARATION!

Phys.Rev.D 104 (2021) 5, 056019,
arXiv:2105.11306

[QCD analysis of pion fragmentation functions in the xFitter framework](#)

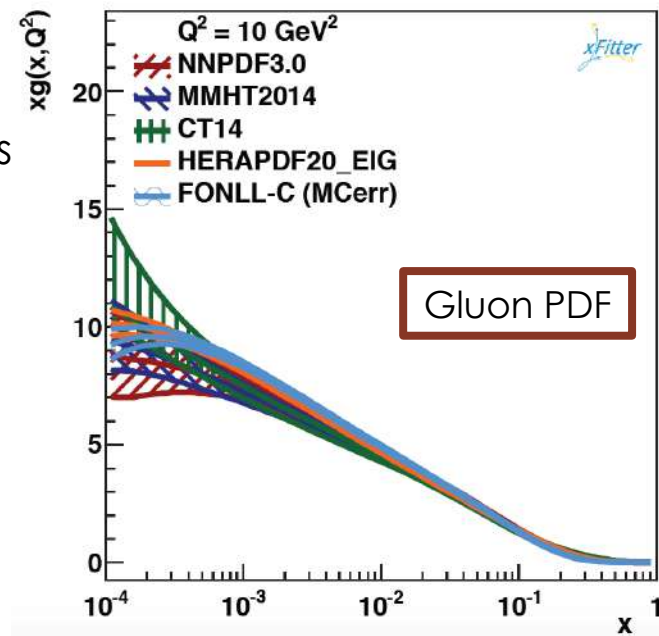
Phys.Rev.D 102 (2020) 1, 014040,
arXiv:2002.02902

[Parton Distribution Functions of the Charged Pion Within The xFitter Framework](#)

xFitter in a nutshell

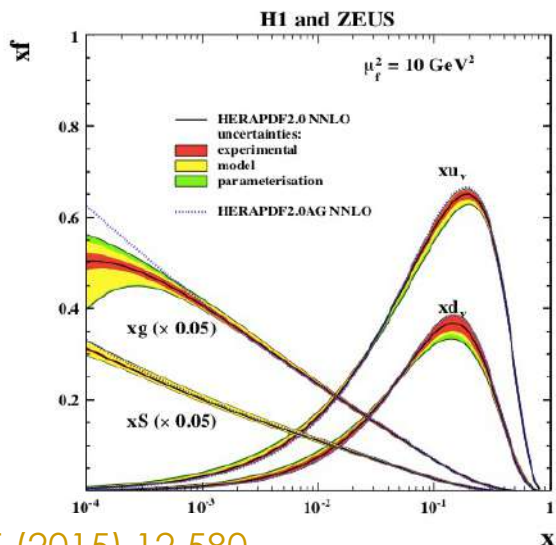


- **Parametrise** PDFs at the initial scale:
 - several functional forms available
 - define PDF parameters to be minimised
- **Evolve** PDFs to the scales of the fitted data points:
 - DGLAP evolution up to NNLO in QCD and NLO QED (QCDNUM, APFEL, MELA)
 - non-DGLAP evolutions (dipole, CCFM)
- **Compute** predictions for the data points:
 - several mass schemes available in DIS (ZM-VFNS, ACOT, FONLL, TR, FFNS)
 - predictions for hadron-collider data through fast interfaces (APPLgrid, FastNLO)
- **Comparison data-predictions** via χ^2 :
 - multiple definitions available
 - consistent treatment of the systematic uncertainties
- **Minimise** the χ^2 w.r.t. the fitted parameters
 - using MINUIT or by Bayesian reweighting
- **Useful drawing tools** – nice and colorful plots
- [Last xFitter External meeting](#) held in May at CERN



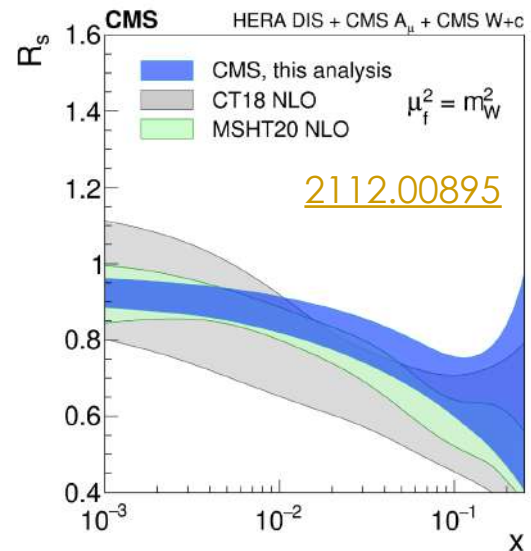
Results obtained with xFitter

DIS inclusive processes (ep)

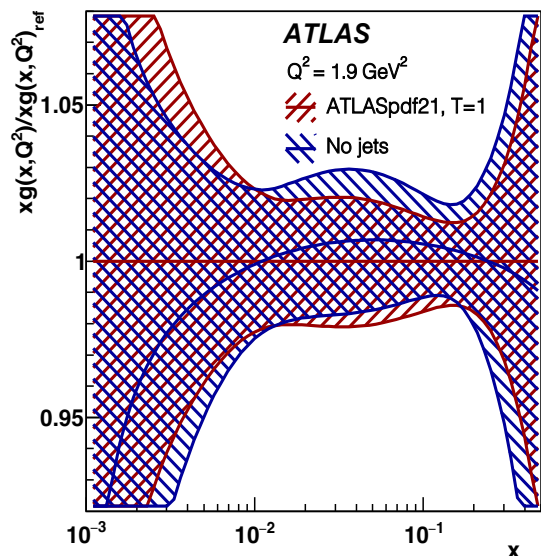


[EPJC 75 \(2015\) 12 580](#)

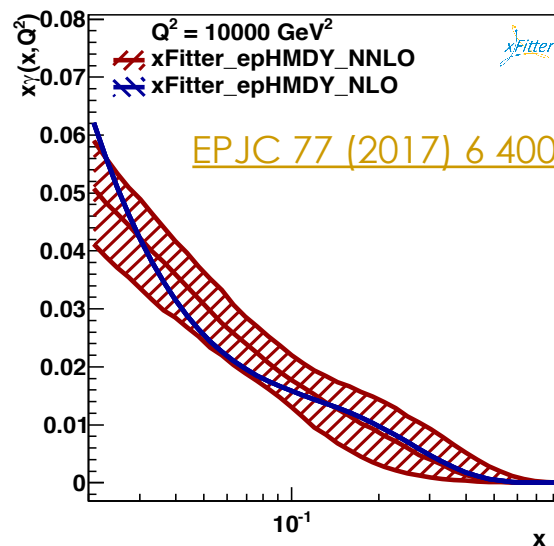
Drell-Yan processes ($pp, p\bar{p}$)



Jet production (ep, pp) [EPJC 82 \(2022\) 5 438](#)



DY data sensitivity to photon PDF



xFitter release 2.2.0



xFitter

Sample data files:

LHC: ATLAS, CMS, LHCb

Tevatron: CDF, D0

HERA: H1, ZEUS, Combined

Fixed Target: ...

User Supplied: ...

GitLab

Wiki

[WikiPolicy](#)
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More Actions: ⌵

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Releases of the xFitter QCD analysis package

- The release notes can be found in this attachment: [xFitter_release_notes.pdf](#).
- Installation script for xFitter together with QCDNUM, APFEL, APPLGRID, LHAPDF [install-xFitter-2.0.1](#)
 - New installation script from master branch [install-xfitter-master](#)
- Data and theory files can be downloaded from gitlab [gitlab data repository](#)

| Date | Version | Files | Remarks |
|---|---------------------------|-----------------------------------|---|
|  03/2022 | 2.2.0 FutureFreeze | xfitter-2.2.0.tgz | Major update of evolution and reaction interfaces |
|  05/2019 | 2.0.1 OldFashioned | xfitter-2.0.1.tgz | update/bug fix to 2.0.0 FrozenFrog |
|  03/2017 | 2.0.0 FrozenFrog | xfitter-2.0.0.tgz | stable release with decoupled data and theory files |



**2.2.0
Future Freeze**

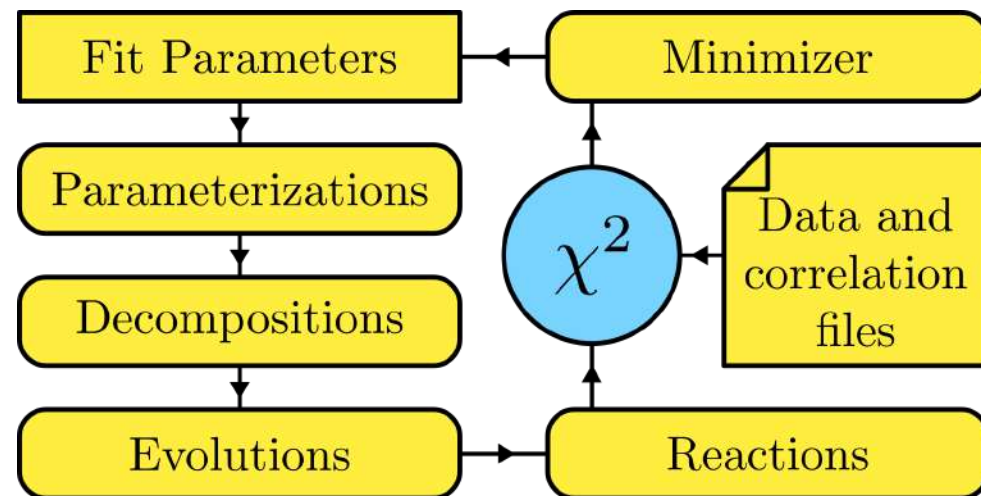
<https://www.xfitter.org/xFitter/xFitter/DownloadPage>

➤ **Release 2.2.0 released!** (major update of evolution and reaction interfaces)

➤ Script to install xFitter and all its dependencies: [install-xFitter](#)

Talking about the new release...

- **Significant changes** in the internal structure
- **Re-written interfaces** to minimizers, PDF parameterisation, decomposition, evolution and theory reactions
- **Large changes in the user interface**
- Data handling, format and χ^2 calculation remain largely the same (but there are changes)
- Nicely summarized in this [talk](#) by S. Glazov
- Picture taken from Ivan Novikov's [talk](#)



xFitter usage in the HEP community

- xFitter is the **tool of choice for PDF/QCD analyses by the LHC Collaborations**
- **ATLAS:**
 - PDF fit from diverse ATLAS data at $\sqrt{s} = 7, 8$ and 13 TeV - [EPJC 82 \(2022\) 5 438](#)
- **Drell-Yan phenomenology:**
 - PDF impact of A_{FB} in NC Drell-Yan events - [JHEP 10 \(2019\) 176](#)
 - PDF sensitivity of the longitudinal Z-boson polarisation - [Phys.Lett.B 821 \(2021\) 136613](#)
 - PDF sensitivity to A_{FB} and A_W in Drell-Yan for Precision EW Measurements and New Physics Searches - [Nucl.Phys.B 968 \(2021\) 115444](#)
 - Enhancing the LHC sensitivity to broad W'/Z' resonances of new gauge sectors - [JHEP 02 \(2022\) 179](#), [PLB 841 \(2023\) 137915](#)
- Important contribution in **several ongoing activities of the LHC EW WG:**
 - **Correlations between different PDFs** through pseudo-data fits
 - ATLAS/CMS/LHCb $\sin^2 \theta_{eff}^l$ **pseudo data** and combination exercise
 - Tevatron/ATLAS (and in future LHCb and CMS) m_W **combination**
- α_s **extraction** from Z boson transverse momentum distribution - [2203.05394](#), [ATLAS-CONF-2023-015](#)

List of exercises

- **Exercise 1:** PDF fit
 - learn the basic settings of a QCD analysis, based on HERA data only
- **Exercise 2:** α_s extraction
 - learn the basic of an α_s extraction using ATLAS Z p_T data
- **Exercise 3:** LHAPDF analysis
 - how to estimate impact of a new data without fitting
 - basis on profiling and reweighting techniques

Other useful/interesting exercise you might want to have a look at in backup:

- **Exercise 4:** Including small-x resummation correction in a PDF fit
- **Exercise 5:** Adding your preferred PDF parametrization
- **Exercise 6:** Fit to final combined HERA+II data and ATLAS W,Z data at 7 TeV
 - strange-quark density: fixed vs free r_s
 - unsuppressed strange at low-x
- **Exercise 7:** Charged pion PDF
- **Exercise 8:** Charged pion Fragmentation Functions (FFs)
- **Bonus:** how to generate fixed-order predictions (key ingredient of a PDF fit)

$$r_s = \frac{s + \bar{s}}{\bar{u} + \bar{d}}$$

Overview

- Each exercise in a separate directory: ~/xFitterTutorial/
 - **Exercise1**
 - **Exercise2**
 - **Exercise3**
 - Exercise4
 - Exercise5
 - Exercise6
 - Exercise7
 - Exercise8
- You can find the xFitter manual and this tutorial in ~/xFitterTutorial/DOC
 - DOC/xFitter_Manual.pdf
 - DOC/xFitter_Tutorial.pdf
- All these exercises (with many more examples) can be found [here](#)
- [Updated Wiki](#) to help users, with also the list of [existing JRAs](#)
- If you cannot find an answer to your question, **create a new JIRA ticket**, with issue type "Question"

Input files for a xFitter run

- Each time we run xFitter, we need to care about three configuration files:
 - **parameters.yaml:**
 - Minimisers – MINUIT or CERES
 - Settings and commands for MINUIT
 - Define parameters of the PDF parameterisation
 - Running mode: PDF fit or LHAPDF analysis
 - QCD order (NLO or NNLO)
 - Heavy flavor scheme (TR, ACOT, FONLL, etc.)
 - **steering.txt:**
 - List of data sets
 - χ^2 settings
 - **constants.yaml:**
 - EW and SM input parameters e.g. couplings, quark masses etc.

```
Minimizer: MINUIT # CERES
CERES:
  offset: 2
  tolerance: 1e-5
  strategy: 0
  covariance: 1
```

(CERES instructions since the tutorial uses MINUIT)

General structure of the exercise

- Each exercise has all the necessary inputs and datafiles for running xFitter
- The results will be saved in the 'output' directory for further manipulation
- Before every exercise, in order to set up environmental variables, do
`$> source ~/Software/setup.sh`
- To run xFitter, in the exercise folder type `$> xfitter`
- To draw graphical visualisation of the results: `$> xfitter-draw output`
 - Many drawing options! Type `$> xfitter-draw --help` to see all of them
- Post-fit and pre-fit manipulation of the LHAPDF files: `$> xfitter-process` (needed for exercise3 in backup)
 - Many modules available! Type `$> xfitter-process --help` to see all of them
 - profile – to be used with Hessian PDF eigenvectors error sets
 - reweight – to be used with NNPDF-style PDF sets (MC replicas)
 - scale90to68 – scale PDF error bands from 90% CL to 68% CL
 - rotate – obtain a PDF set which members are sorted according to their sensitivity to particular data
 - symmetrize – produces symmetric bands out of hessian PDF set

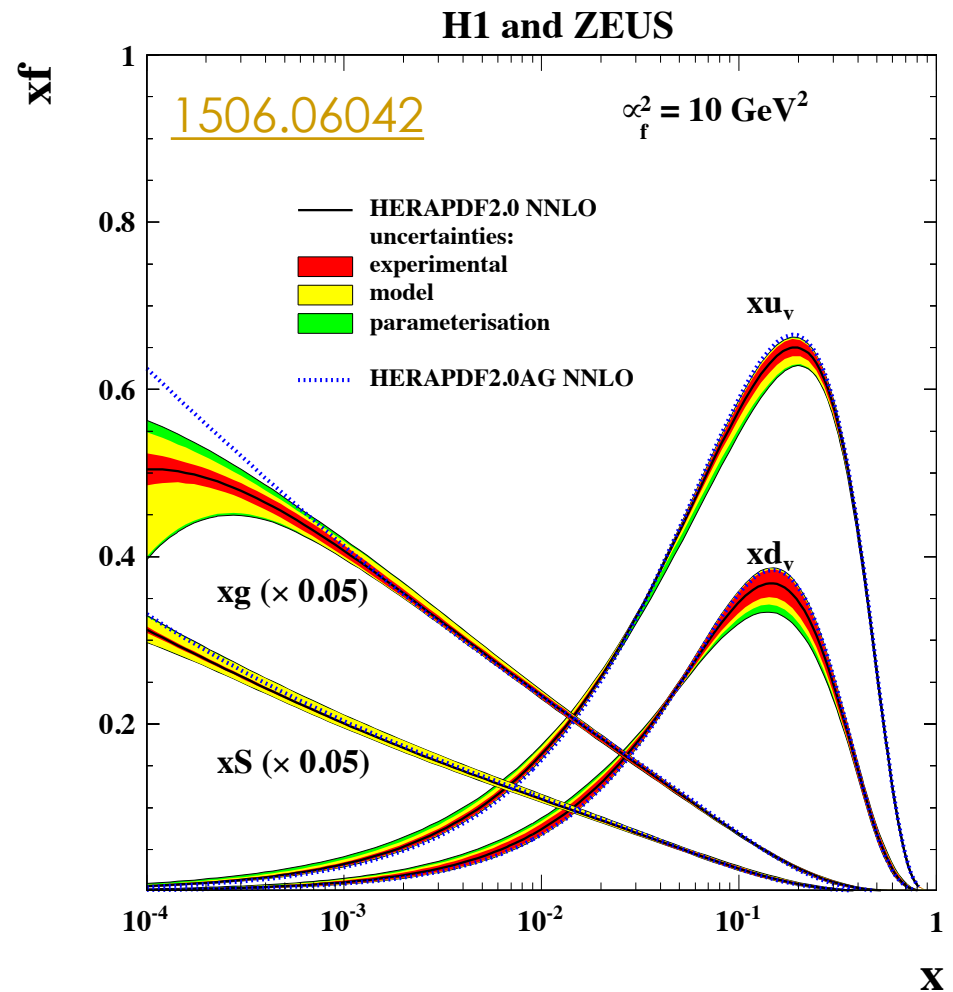
EXERCISE 1

PDF fit

Exercise 1

- **Purpose:** Learn the basic settings of a QCD analysis and reproduce the results of the HERAPDF2.0 fit
- **Data set:** Final combined HERA I+II DIS data
- **QCD order:** NNLO

This data set is very important! **Backbone of all modern PDF fits**



Exercise 1 - settings

- `$> cd ~/xFitterTutorial/exercise1`
- Final combined HERA1+II DIS data in `steering.txt`

```
&InFiles
```

```
! Number of input files
```

```
  NInputFiles = 7
```

```
! Input files:
```

```
  InputFileNames =
```

```
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_920-thexp.dat',  
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_820-thexp.dat',  
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_575-thexp.dat',  
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_460-thexp.dat',  
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCem-thexp.dat',  
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_CCep-thexp.dat',  
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_CCem-thexp.dat',
```

```
&End
```

- FYI you can add as many data sets as you want! The fit will take longer 😊
have a look at this [example](#)

The structure of a xFitter datafile - DIS

```

&Data
  Name = "HERA1+2 NCep 460"
  IndexDataset = 106
  Reaction = "NC e+-p"

  TermName = 'R'
  TermSource = 'use:hf_scheme_DISNC'
  TermInfo = 'type=signed:flav=incl:echarge=1:epolarity=0' ! in CInfo there was also "YSWIMEXP" = 1.0
  TheorExpr = 'R'

  NData = 210
  NCoLumn = 176
  CoLumnType = 3*"Bin","Sigma", 172*"Error"
  CoLumnName = "Q2","x","y","Sigma", "stat", "uncor","sysHZComb1001","sysHZComb1002","sysHZComb1003","sysHZComb1004","sysHZComb1005",
  Percent = 172*true
&End

```

- **'Name'** provides the name of the data set
- **'IndexDataset'** is an internal index of the data set (provide unique numbers to get extra χ^2 info)
- **'Reaction'** indicates the reaction type of the data set (used to trigger the corresponding theory calculation)
- **'NData'** specifies the number of data points in the file
- **'NCoLumn'** is the number of columns in the data table
- **'CoLumnType'** defines layout of the data table: *Bin, Sigma, Error and Ignored*
- **'CoLumnName'** defines names of the columns (e.g. x, Q² and y are required for DIS NC xsec)
 - If CoLumnType = Sigma, it provides a label for the observable
 - If CoLumnType = Error, the following names have special meaning: *stat, uncor and total*
 - Other names specify columns of correlated systematic uncertainties (e.g. each column of the correlated uncertainty must have unique name)
- **'Percent'** tells if an uncertainty is given in absolute (false) or in percent (true)

The structure of a xFitter datafile - LHC

[Gitlab repository](#)

```
TermName = 'A','K'
TermSource = 'APPLgrid','KFactor'
TermInfo = 'GridName=datafiles/lhc/atlas/wzProduction/1612.03016/grid-40-6-15-3-Z0_zypeak_cc.root',
           'FileName=datafiles/lhc/atlas/wzProduction/1612.03016/kf.zypeak_cc.txt:FileColumn=3'
TheorExpr = 'K*A/1000'
```

- **'TermName'** gives names of terms used in the theory expression
- **'TermSource'** might be:
 - **KFactor** → term which denotes an array of K-factors corresponding to the data bins
 - **APPLgrid**, **FastNLO**, ... → this term tells the parser to initialize the correct theory reaction for the cross section evaluation
 - **VirtGrid** → it can be used if the fit is performed using multidimensional measurements (here, each row denotes a single bin of the cross section and, the APPLGRID file location and number of bins in it)

| # | y1 | y2 | applgrid | n_grid_bins |
|-----|-----|----|---|-------------|
| 0.0 | 0.3 | | theoryfiles/atlas/Jets2010-vg/R04/eta1.root | 17 |
| 0.3 | 0.8 | | theoryfiles/atlas/Jets2010-vg/R04/eta2.root | 17 |
| 0.8 | 1.2 | | theoryfiles/atlas/Jets2010-vg/R04/eta3.root | 17 |
| 1.2 | 2.1 | | theoryfiles/atlas/Jets2010-vg/R04/eta4.root | 16 |
| 2.1 | 2.8 | | theoryfiles/atlas/Jets2010-vg/R04/eta5.root | 13 |

- **'TermInfo'** gives paths from where the term numerical values should be taken
- **'TheorExpr'** is the theory expression in simple algebraic form

The structure of a xFitter datafile - Plot

```
&PlotDesc
  PlotN = 1
  PlotDefColumn = 'y_max'
  PlotDefValue = 0., 5.
  PlotOptions(1) = 'Experiment:ATLAS@ExtraLabel:pp #rightarrow Z; #sqrt{s} = 7 TeV; #int L = 4.7 fb^{-1}@Title: 66 < M_{Z} < 116
                    @XTitle: y @YTitle: d#sigma/dy [pb] '
```

- **'PlotN'** tells us the number of distributions to be plotted
- **'PlotDefColumn'** is the variable name you want to plot
- **'PlotDefValue'** specifies the x-axis range of the variable you're plotting
- **'PlotOptions'** are several plotting options to have some graphical improvement and labels on the standard xFitter plots in output

Exercise 1 - settings

- The PDF parametrisation is set in parameters.yaml

Parameterisations:

```

par_uv:
  class: HERAPDF
  parameters: [Auv, Buv, Cuv, Duv, Euv]
par_dv:
  class: HERAPDF
  parameters: [Adv, Bdv, Cdv]
par_uubar:
  class: HERAPDF
  parameters: [Adbar, Bdbar, Cubar, Dubar]
par_dbar:
  class: HERAPDF
  parameters: [Adbar, Bdbar, Cdbar]
par_s: # s=fs/(1-fs) * Dbar
  class: Factor
  factor: DbarToS #name of parameter
  input: par_dbar
par_g:
  class: NegativeGluon
  parameters: [Ag, Bg, Cg, ZERO, ZERO, Agp, Bgp, Cgp]

```

```

DefaultDecomposition: proton
Decompositions:
  proton:
    class: UvDvUbarDbarS
    xuv: par_uv
    xdv: par_dv
    xubar: par_uubar
    xdbar: par_dbar
    xs: par_s
    xg: par_g

```

equivalent
to...

```

#par_s:
#class: Expression
#expression: "Adbar*fs/(1-fs)*(x^Bdbar*(1-x)^Cdbar)"
# Another example for Expression parameterisation
#par_g:
#class: Expression
#expression: "Ag*(x^Bg*(1-x)^Cg-Agp*x^Bgp*(1-x)^Cgp)"

```

- HERAPDF-like PDF parametrisation:

$$Ax^B(1-x)^C(1+Dx+Ex^2) - \underbrace{A'x^{B'}(1-x)^{C'}}_{\text{to suppress negative contributions at high-x}}$$

Just for the gluon PDF ($C'_g = 25$)
to suppress negative
contributions at high-x

- Sum rules
- Asymptotic behaviour
- To better model the high-x region

Exercise 1 - settings

- The starting values of the parameters are set in parameters.yaml

Parameters:

```

Ag   : DEPENDENT
Bg   : [ -0.061953, 0.27 ]
Cg   : [ 5.562367, 0.32 ]
Agp  : [ 0.166092, 0.01 ] # negative gluon ...
Bgp  : [ -0.383100, 0.01 ]
Cgp  : [ 25.0, 0. ] # fix C of negative gluon
Auv  : DEPENDENT
Buv  : [ 0.810476, 0.016 ]
Cuv  : [ 4.823512, 0.06 ]
Euv  : [ 9.921366, 0.8 ]
Adv  : DEPENDENT
Bdv  : [ 1.029995, 0.06 ]
Cdv  : [ 4.846279, 0.3 ]
CUbar: [ 7.059694, 0.8 ]
DUbar: [ 1.548098, 1.0 ]
ADbar: [ 0.26883, 0.01 ]
BDbar: [ -0.1273, 0.004 ]
CDbar: # another example of providing value, step etc.
      value: 9.586246
      step: 1.2345
      #min
      #max
      #pr_mean
      #pr_sigma
ZERO  : [ 0. ] # zero
fs    : [ 0.4, 0.0 ]
fd    : "=1-fs"
AUbar: "(1-fs)*ADbar"

```

- The first number is the starting value, the second number the step size in the minimisation (if set to 0, the parameter is fixed)

- You can also define parameters as a function of other parameters i.e. AUBar

} Another possible way to provide values, step, etc.

Exercise 1 - settings

➤ Settings for PDFs as output of the fit in steering.txt

&Output

! -- Q2 values at which the pdfs & errors are done (up to 20)

Q2VAL = 1.9, 3.0, 4.0, 5., 10., 100., 6464, 8317

! Q2VAL = 1.9, 4., 10., 100., 6464, 8317

! How many x points to write (standard = 101)

OUTNX = 101

! x-range of output (standard = 1E-4 1.0)

OUTXRANGE = 1E-4, 0.9999

! Write out LHAPDF5 output

! WriteLHAPDF5 = false

&End

➤ Process dependent cuts in steering.txt

!----- CC ep -----

ProcessName(3) = 'CC e+-p'

Variable(3) = 'Q2'

CutValueMin(3) = 3.5

CutValueMax(3) = 1000000.0

Should be identical to 'Name' in the datafile

ProcessName(4) = 'CC e+-p'

Variable(4) = 'x'

CutValueMin(4) = 0.000001

CutValueMax(4) = 1.0

Should be one of the variable name ('ColumnName') in the datafile

There's also a 'binFlag' in the datafiles:

0 → bin not included in the fit

1 → bin included in the fit

Exercise 1 - settings

- We want to perform a PDF fit...
- ... So we will use the option 'DefaultEvolution: proton-QCDNUM' in parameters.yaml

```
DefaultEvolution: proton-QCDNUM
```

```
Evolutions:
```

```
  proton-QCDNUM:
```

```
    ? !include evolutions/QCDNUM.yaml
```

```
    decomposition: proton #this could be omitted, as the default decomposition is set
```

- The QCD perturbative order is set in parameters.yaml as well:

```
# QCD parameters
```

```
Order: NNLO
```

```
NFlavour: 5
```

```
isFFNS: 0
```

```
Q0 : 1.378404875209 # Initial scale =sqrt(1.9)
```

```
alphas : 0.118
```

```
? !include constants.yaml
```

Q_0 is the starting scale
where we parametrize PDFs

- Here you can see other parameters as well i.e. number of flavours, Q_0 , α_s value etc. – this will overwrite what you have in constants.yaml (leaving everything else unchanged)

Exercise 1 - settings

- The Heavy Flavour scheme is set in `parameters.yaml`

```
# Specify HF scheme used for DIS NC processes:
hf_scheme_DISNC :
  defaultValue : 'RT_DISNC'      # global specification
# defaultValue : 'BaseDISNC'    # global specification
# defaultValue : 'FONLL_DISNC'  # global specification
# defaultValue : 'FFABM_DISNC'
# 'HERA1+2 NCep 920' : 'BaseDISNC' # datafile specific (based on name)
# 1 : BaseDISNC
# 'HERA1+2 NCep 920' : 'Fractal_DISNC' # Fractal model. Add parameters file if you want to try it (see above)

# Specify HF scheme used for DIS CC processes:
hf_scheme_DISCC :
  defaultValue : 'BaseDISCC'    # global specification
# defaultValue : 'FONLL_DISCC'  # global specification
# defaultValue : 'FFABM_DISCC'  # global specification
```

- Several mass schemes available in DIS:
 - ZM-VFNS
 - ACOT
 - FONLL
 - TR
 - FFNS

Exercise 1 - settings

- To do a real fit with proper MINUIT minimisation:

MINUIT:

```
Commands: |
call fcn 1
set str 2
call fcn 3
migrad
hesse
call fcn 3
```

minimisation

- To run just 3 iterations:

MINUIT:

```
Commands: |
set str 2
call fcn 3
```

PDF errors – 3 options:

- Pumplin – Eq. 43 of [hep-ph/0611148](https://arxiv.org/abs/hep-ph/0611148) (asymmetric)
- Hesse – symmetric version of Pumplin
- None – no error bands evaluation

Regulated by **doErros: ###**

- To obtain datafiles: `$> ln -s ~/Software/xfitter-master/datafiles .`
- To run xFitter: `$> xfitter`
- To draw your results: `$> xfitter-draw output`
- To see the full list of plotting options: `$> xfitter-draw --help`

The output folder

- You can modify the folder name by changing `OutputDirectory: "output"`
- `'Status.out'` tells us if the fit has converged (OK) or not (Failed)
- `'minuit.out.txt'` contains the information about the MINUIT output of the fit
- `'Results.txt'` shows the global and partial χ^2 , as well as the pulls of each systematic uncertainty present in the fit
- `'parsout_0'` contains the output fit parameters (and their associated errors) in MINUIT format
- `'fittedresults.txt'` shows the comparison between data and fit predictions for each data point
- The `'proton'` contains the output PDFs in LHAPDF format
 - You can modify the name in `parameters.yaml`
- `'pdfs_q2val_0*.txt'` are `.txt` files with the PDF values at different Bjorken x ('01' represents the starting scale, and then you have one file for each scale defined in the steering card → Q2VAL)

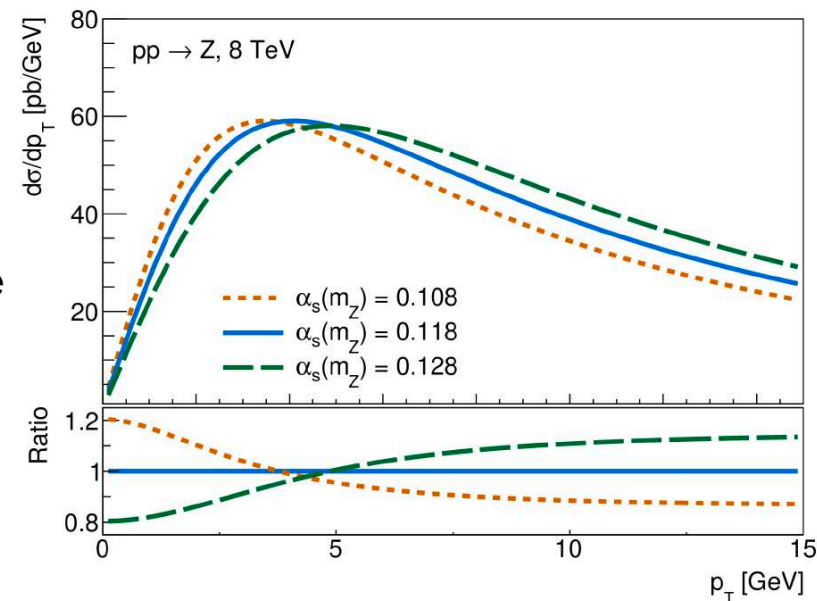
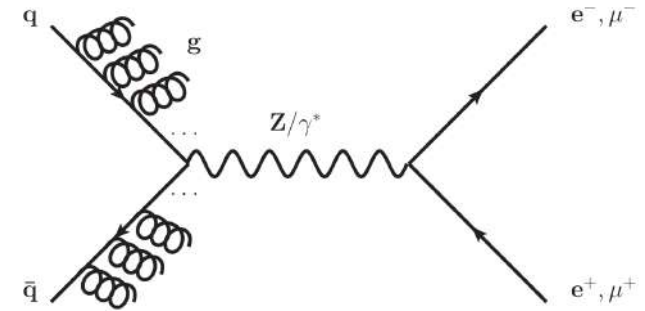
```
WriteLHAPDF6:  
  name: "proton"  
  description: "..."  
  authors: "..."  
  reference: "..."
```

EXERCISE 2

α_s extraction from
ATLAS Z p_T data

Exercise 2

- **Purpose:** Learn the basics of an α_s extraction
- **Data set:** Final combined HERA+II DIS data + ATLAS 8 TeV Z p_T data ([ATLAS-CONF-2023-013](#)) – see backup for more details
- **QCD order:** N³LL + N³LO (through [DYTurbo](#) predictions)
- Strong coupling constant α_s is the **least well known in nature**
- **Dominant uncertainties** to precision measurements of **Higgs coupling** at LHC or **EW precision observables** at e^+e^- colliders
- Non-zero value of Z p_T arises from initial state radiations from incoming partons due to momentum conservation
- The **peak position of Z p_T** and above is **sensitive to $\alpha_s(m_Z)$**



Exercise 2 - settings

- `$> cd ~/xFitterTutorial/exercise2/`
- We added the ATLAS 8 TeV Z p_T data on top of the final combined HERA+II DIS data in `steering.txt`

```
'datafiles/lhc/atlas/zptfull8tev/zpt_y00_bwi.dat',  
'datafiles/lhc/atlas/zptfull8tev/zpt_y01_bwi.dat',  
'datafiles/lhc/atlas/zptfull8tev/zpt_y02_bwi.dat',  
'datafiles/lhc/atlas/zptfull8tev/zpt_y03_bwi.dat',  
'datafiles/lhc/atlas/zptfull8tev/zpt_y04_bwi.dat',  
'datafiles/lhc/atlas/zptfull8tev/zpt_y05_bwi.dat',  
'datafiles/lhc/atlas/zptfull8tev/zpt_y06_bwi.dat',  
'datafiles/lhc/atlas/zptfull8tev/zpt_y07_bwi.dat',
```

- Additional datasets which have sensitivity to α_s (i.e. CDF Z p_T [data](#)) can be downloaded using the `./tool/xfitter_getdata.sh` script
- Very easy to use! `./tool/xfitter_getdata.sh arXiv_number`
- To see available data sets: `./tool/xfitter-getdata.sh --print`

Exercise 2 – Z p_T datafiles

- Open e.g.
./datafiles/lhc/atlas/zptfull8tev/zpt_y00_bwi.dat

```

Reaction =      'NC pp'
TheoryType     = 'expression'
TermName =     'A1','K','C'
TermSource =   'DYPurbo','KFactor','KFactor'
TermInfo =     'FileName=datafiles/lhc/atlas/zptfull8tev/dyturbo/z-8tev-y00-n311.in',
               'FileName=datafiles/lhc/atlas/zptfull8tev/qedisr/qedisr_zpt_y00.txt:FileColumn=3',
               'FileName=datafiles/lhc/atlas/zptfull8tev/mcfm/afactor/n3lo-afactor-y00.txt:FileColumn=3'
TheorExpr=    '(2*A1+C)*K*0.996/1000'

```

- Note the kind of reaction → 'NC pp' (Neutral Current production in pp collisions)
- 'TermSource = DYPurbo' thanks to a direct interface to xFitter
- The first file is literally a DYPurbo input file
- Additional k_F to take into account e.g. ISR QED corrections or missing N³LO QCD contributions

Exercise 2 - settings

- We add the statistical correlation matrices in `steering.txt`

```
&InCorr
! Number of correlation (statistical, systematical or full) files
NCorrFiles = 36

! Correlation files:
CorrFileNames(1) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y0_y0.corr',
CorrFileNames(2) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y0_y1.corr',
CorrFileNames(3) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y0_y2.corr',
CorrFileNames(4) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y0_y3.corr',
CorrFileNames(5) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y0_y4.corr',
CorrFileNames(6) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y0_y5.corr',
CorrFileNames(7) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y0_y6.corr',
CorrFileNames(8) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y0_y7.corr',
CorrFileNames(9) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y1_y1.corr',
CorrFileNames(10) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y1_y2.corr',
CorrFileNames(11) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y1_y3.corr',
CorrFileNames(12) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y1_y4.corr',
CorrFileNames(13) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y1_y5.corr',
CorrFileNames(14) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y1_y6.corr',
CorrFileNames(15) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y1_y7.corr',
CorrFileNames(16) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y2_y2.corr',
```

```
CorrFileNames(17) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y2_y3.corr',
CorrFileNames(18) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y2_y4.corr',
CorrFileNames(19) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y2_y5.corr',
CorrFileNames(20) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y2_y6.corr',
CorrFileNames(21) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y2_y7.corr',
CorrFileNames(22) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y3_y3.corr',
CorrFileNames(23) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y3_y4.corr',
CorrFileNames(24) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y3_y5.corr',
CorrFileNames(25) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y3_y6.corr',
CorrFileNames(26) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y3_y7.corr',
CorrFileNames(27) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y4_y4.corr',
CorrFileNames(28) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y4_y5.corr',
CorrFileNames(29) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y4_y6.corr',
CorrFileNames(30) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y4_y7.corr',
CorrFileNames(31) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y5_y5.corr',
CorrFileNames(32) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y5_y6.corr',
CorrFileNames(33) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y5_y7.corr',
CorrFileNames(34) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y6_y6.corr',
CorrFileNames(35) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y6_y7.corr',
CorrFileNames(36) = 'datafiles/lhc/atlas/zptfull8tev/corr/zpt_y7_y7.corr',
&End
```

- The general format of correlation matrices 

- ‘Name1, Name2’ are the dataset name(s)
- ‘IdColumns’ are the variables i.e. p_T , m_{ll} , etc.
- ‘NBins’ are the number of bins for each variables
- You need to specify the kind of correlation (i.e. you can also have ‘Full covariance matrix’)
- The input format is very easy to understand!

```
&StatCorr
Name1 = 'ATLAS 1D ttbar vs ptavt 13 TeV'
Name2 = 'ATLAS 1D ttbar vs mtt 13 TeV'

NIdColumns1 = 2
NIdColumns2 = 2

IdColumns1 = 'ptlow', 'pthigh'
IdColumns2 = 'mtt1', 'mtt2'

NBins1 = 2
NBins2 = 3

MatrixFormatIsTable = true

MatrixType = 'Statistical correlations'
&End
0      0      325      400      480
0      0      400      480      580
0      50     0.5      0.2     -0.07
50     100     0.5      0.4      0.07
```


Exercise 2 - settings

- Let's also have a look at the DYTurbo part in parameters.yaml

DYTurbo:

```

#? !include reactions/DYTurbo.yaml
order: 3      # Perturbative order in QCD: 0 for LL, 1 for NLL+NLO, 2 for NNLL+NNLO, 3 for NNNLL+NNLO
muR: 1.       # Renormalization scale
muF: 1.       # Factorization scale
muRes: 1.     # Resummation scale
g1: 0.66      # Universal Gaussian non-perturbative form factor
g2: 0         # Q-dependent Gaussian non-perturbative form factor
g3: 0         # x-dependent Gaussian non-perturbative form factor
q: 0.1        # quartic term
debug: 0

```

- g_1 , g_2 and g_3 regulates a non-perturbative form factor which affects the region of Z $p_T < 5$ GeV

$$S_{\text{NP}}(b) = \exp \left[-g_j(b) - g_K(b) \log \frac{m_{\ell\ell}^2}{Q_0^2} \right]$$

- q regulates the quartic term

- **g_1 and q are free parameters of the fit!**

Constrained by data

DYTurbo/g1: [0.488881, 0.0434729]

DYTurbo/q: [-0.187143, 0.0296958]

$$g_j(b) = \frac{g b^2}{\sqrt{1 + \lambda b^2}} + \text{sign}(q) \left(1 - \exp[-|q| b^4] \right)$$

$$g_K(b) = g_0 \left(1 - \exp \left[-\frac{C_F \alpha_s(b_0/b_*) b^2}{\pi g_0 b_{\text{lim}}^2} \right] \right)$$

Exercise 2 - settings

- We have to free the $\alpha_s(m_Z)$ parameter in `parameters.yaml`

```
alphas: [ 0.117178, 0.000417857 ]
```

- We want to do a real MINUIT minimisation fit, so:

MINUIT:

```
Commands: |
call fcn 1
set str 2
call fcn 3
migrad
hesse
call fcn 3
```

[EPJ Plus \(2019\) 134, 531](#)

As regards the PDF parametrisation, we adopt one with more flexibility at low x - see Exercise 5 in backup!

```
doErrors : Hesse # None
```

- To obtain datafiles: `$> ln -s ~/Software/xfitter-master/datafiles .`
- To run xFitter: `$> xfitter`
- To draw your results: `$> xfitter-draw output_PDF_aS`
- Bonus: you can also run separate fits with fixed values of α_s (see next slide)
 - In this way we can check the correlation between α_s and the gluon PDF

Exercise 2 - results

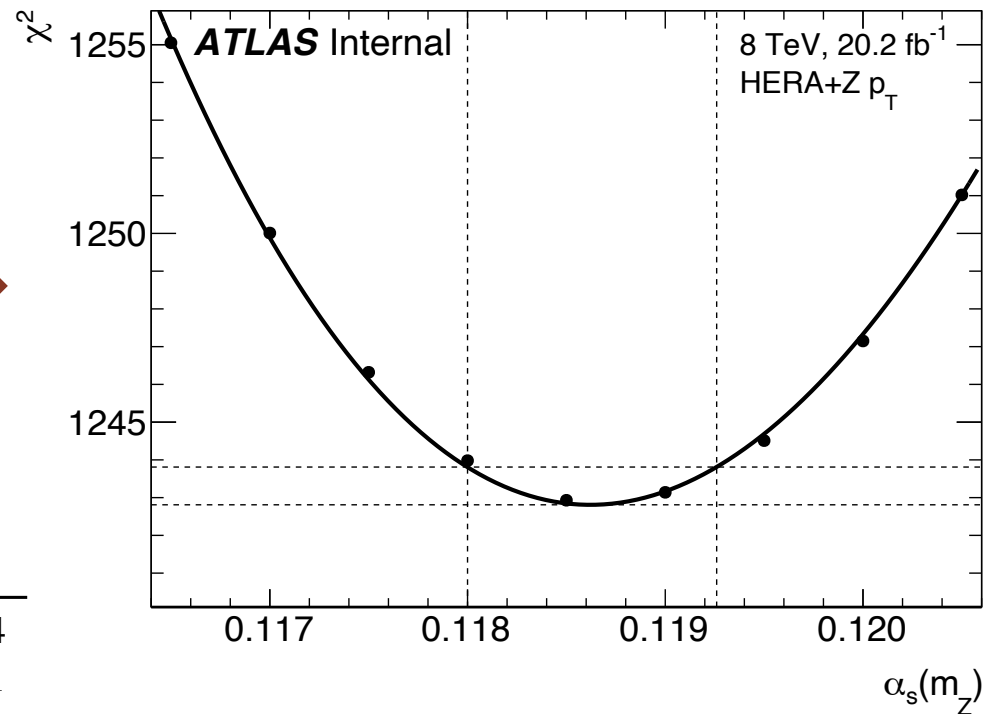
ATL-COM-PHYS-2023-076

- We find: $\alpha_s(m_Z) = \#\#\# \pm \#\#\#$
- Now we can compare the results with what has been found in the:
 - N³LO+N³LL scan ➔
 - $\alpha_s(m_Z)$ determination based on aN⁴LL+N³LO predictions



| | | |
|--------------------------------|-----------------|-----------------|
| Experimental uncertainty | +0.00044 | -0.00044 |
| PDF uncertainty | +0.00051 | -0.00051 |
| Scale variations uncertainties | +0.00042 | -0.00042 |
| Matching to fixed order | 0 | -0.00008 |
| Non-perturbative model | +0.00012 | -0.00020 |
| Flavour model | +0.00021 | -0.00029 |
| QED ISR | +0.00014 | -0.00014 |
| N4LL approximation | +0.00004 | -0.00004 |
| Total | +0.00084 | -0.00088 |

$$\alpha_s(m_Z) = 0.11828^{+0.00084}_{-0.00088}$$



$$\alpha_s(m_Z) = 0.11866 \pm 0.00064$$

(from the $\Delta\chi^2 = 1$ criterion)

All the three approaches give consistent results!

EXERCISE 3

LHAPDF analysis

Exercise 3

- **Purpose:** Learn how to include a new dataset into an existing PDF set, without redoing a PDF fit (profiling/reweighting) – a very simple exercise which can be nicely put in a paper
- **Data set:** Tevatron W-boson charge asymmetry
- **QCD order:** NLO
- PDF sets from LHAPDF stored in `~/Software/deps/lhapdf/share/LHAPDF/`
- LHAPDF is a convenient library for the generic interpolation of PDFs as functions of x and Q^2
- PDFs are saved in tables of PDF values at fixed points in x and Q^2 , and fast interpolation functions allow to access the PDFs at any other value
- To download from PDF sets in LHAPDF format:

```
$> cd ~/Software/deps/lhapdf/share/LHAPDF/  
$> lhpdf --pdfdir=./install HERAPDF20_NNLO_EIG (VAR)  
$> export LHAPATH='pwd'/:$LHAPATH
```

Exercise 3 - settings

- Settings for running a LHAPDF Analysis in `parameters.yaml`
- We need to specify that we want to use LHAPDF evolution

```
DefaultEvolution: proton-QCDNUM
```

```
Evolutions:
```

```
  proton-QCDNUM:
```

```
    ? !include evolutions/QCDNUM.yaml
```

```
    decomposition: proton #this could be omitted, as the default decomposition is set
```

```
    # The following allows QCDNUM to read PDFs from other evolutions:
```

```
    EvolutionCopy: "proton-LHAPDF"
```

```
  proton-LHAPDF:
```

```
    class: LHAPDF
```

```
    set: "HERAPDF20_NNLO_EIG" ←
```

```
    member: 0
```

Here you specify the LHAPDF set you want to use

Profiling methodology

- The inclusion of new data into an existing PDF set can be done with a Hessian profiling technique
- We define a χ^2 with theory uncertainties (β_{th} represent the PDF uncertainties)

$$\begin{aligned} \chi^2(\beta_{exp}, \beta_{th}) &= \chi_{exp}^2 + \chi_{th}^2 \\ &= \sum_{i=1}^{N_{data}} \frac{(\sigma_i^{exp} + \sum_j \Gamma_{ij}^{exp} \beta_{j,exp} - \sigma_i^{th} - \sum_k \Gamma_{ik}^{th} \beta_{k,th})^2}{\Delta_i^2} + \sum_j \beta_{j,exp}^2 + \sum_k \beta_{k,th}^2 \end{aligned}$$

- Find the $\beta_{k,th}$ which minimised the χ^2 on the new data
- The fit is done by solving a system of liner equations
- Reinterpret the $\beta_{k,th}^2$ shifts as optimisation of the PDFs

Exercise 3 - settings

- `$> cd ~/xFitterTutorial/exercise3/`
- The Tevatron W asymmetry data sets and correlations files are set in `steering.txt`

```
&InFiles
! Number of input files
  NInputFiles = 2

! Input files:

  InputFileNames =
    'datafiles/tevatron/cdf/wzProduction/0901.2169/CDF_W_asymmetry-thexp.dat',
    'datafiles/tevatron/d0/wzProduction/1312.2895/D0_W_asymmetry-thexp.dat',
&End

&InCorr
! Number of correlation (statistical, systematical or full) files
  NCorrFiles = 1

! Correlation files:
  CorrFileNames(1) = 'datafiles/tevatron/d0/wzProduction/1312.2895/D0_W_asymmetry.corr'
&End
```

- We also include a correlation matrix to take statistical correlation into account (see Exercise 2 for more details)

Exercise 3 - settings

- We follow the instructions described in the [xFitter twiki](#)

Profiler:

Evolutions:

proton-LHAPDF:

```
sets: [HERAPDF20_NNLO_EIG, HERAPDF20_NNLO_VAR, HERAPDF20_NNLO_VAR]
```

```
members: [, [0,1,10], [0,11,13]] # when omitted, default members is [0,1,end]
```

```
error_type_override: [None, hessian, symmhessian] # treat parametrisation variations (members 11-13
```

```
Status: "On" # "Off" to turn off profiler
```

```
WriteTheo: "Asymmetric" # Can be "Off", "On" or "Asymmetric" (to store asymmetric variations)
```

```
getChi2: "On" # determine and report chi2 for each variation
```

- Remember to set enableExternalProfiler: "On" (it creates of additional files, needed for `xfitter-draw` command)
- PDFs are taken from LHAPDF, so there is no need to specify a parametrisation in `parameters.yaml` file
- We also enable the treatment of asymmetric PDF uncertainties with 'WriteTheo' and we get the χ^2 at every single iteration ('getChi2')

Exercise 3 – produce a new PDF set

- To produce a new PDF set in LHAPDF format

```
$> xfitter-process profile output/pdf_shifts.dat output/pdf_rotate.pdf
output/HERAPDF20nnlo/ HERAPDF20nnlo-TevatronW
```

- Save the new PDF set into our LHAPDF collection

```
$> mv HERAPDF20nnlo-TevatronW ~/Software/deps/lhapdf/share/LHAPDF/
```

- Run a new LHAPDF analysis specifying the new PDF set in parameters.yaml file

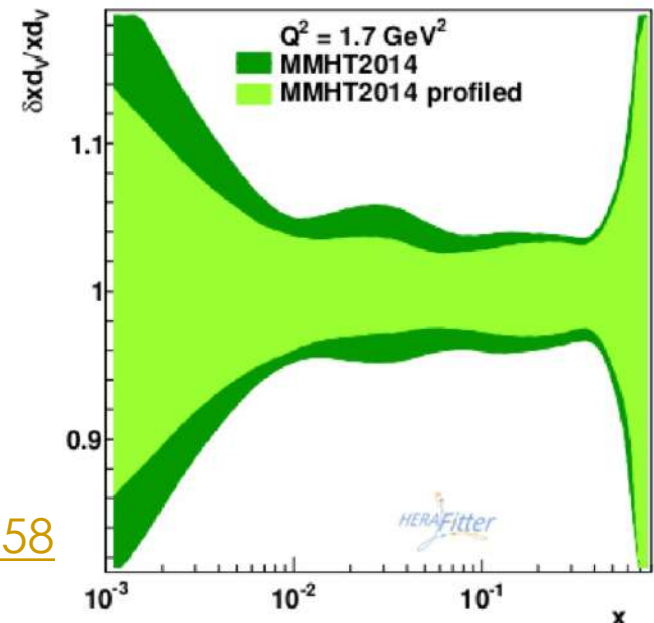
proton-LHAPDF:

```
sets: [HERAPDF20nnlo-TevatronW]
```

- To run xFitter: `$> xfitter`

- To draw your results: `$> xfitter-draw`
HERAPDF20nnlo HERAPDF20nnlo-TevatronW

[EPJC 75 \(2015\) 458](#)



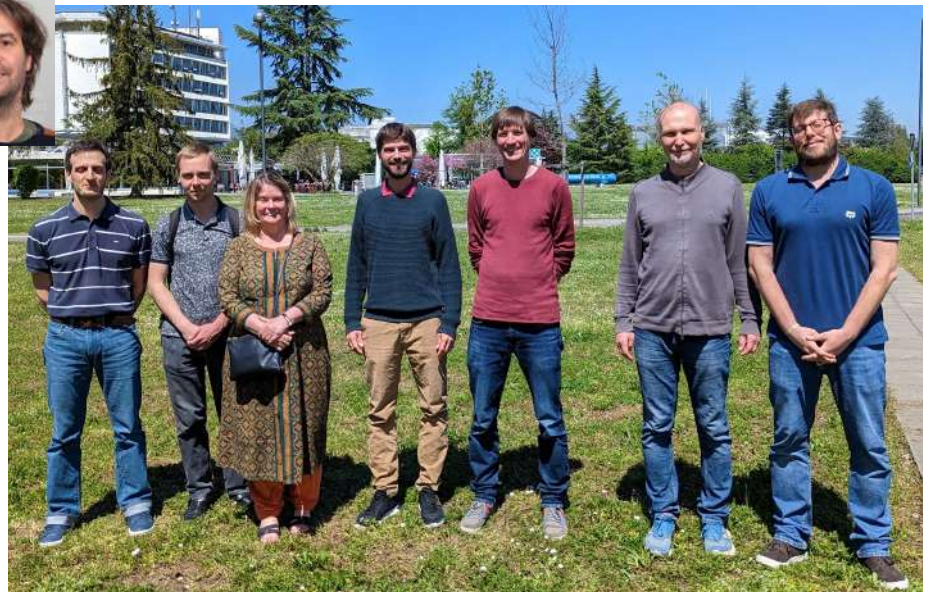
Summary

- xFitter is **open-source QCD fit framework!** The program has many settings to address very different problems
- Big efforts have been made to keep the user interface accessible for simple and basic usage
- **Release 2.2.0** now out! (major update of evolution and reaction interfaces)
 - Modular and flexible! More examples in the '[examples](#)' folder
- The PDF world is amazing, fantastic and marvellous! 😊



WE WANT YOU!

We are nice people! You should really consider the possibility to join and work with us! 😊



Backup Slides

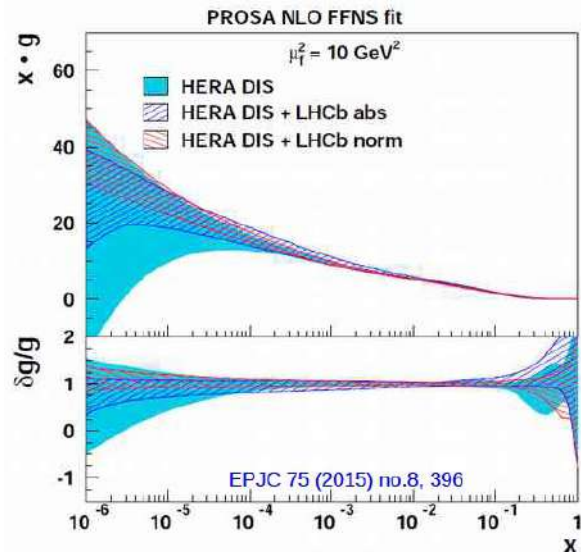


xFitter usage in the HEP community

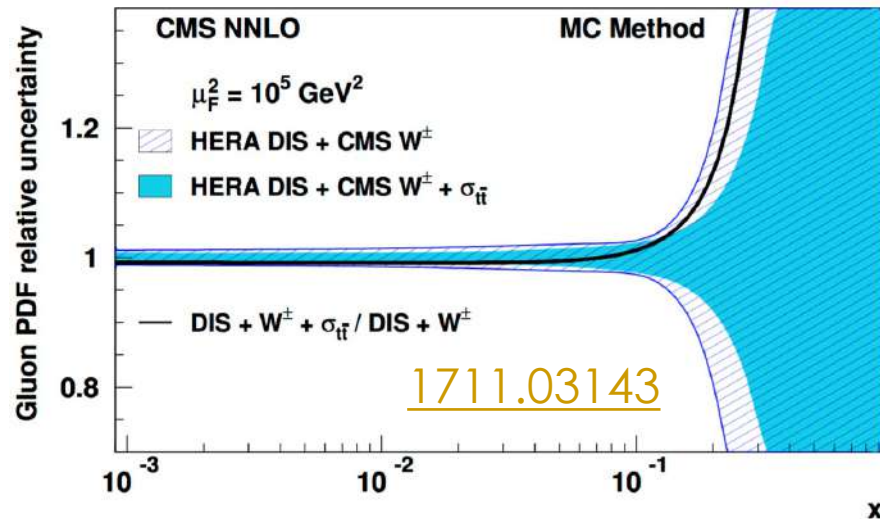
- **CMS:**
 - Multi-differential $t\bar{t}$ cross sections at 13 TeV - [EPJC 80 \(2020\) 7 658](#)
 - Extraction of PDFs, α_s and contact-interactions from new inclusive jet cross section measurement at 13 TeV - [JHEP 02 \(2022\) 142](#) (more in this [talk](#))
 - W+charm analysis at 8 TeV - [2112.00895](#)
- Strange quark PDF analysis with DIS HERA2 data, ATLAS W,Z cross-sections and ATLAS, CMS W+charm cross-sections - [PRD 104 \(2021\) 7 076004](#)
- NLO analysis of heavy-quark production cross-sections using **different mass renormalisation schemes** - [JHEP 04 \(2021\) 043](#)
- **TMD parton densities** and corresponding parton showers: the advantage of four- and five-flavour schemes - [2106.09791](#)
- Implementation of **target mass corrections and higher-twist effects** in the xFitter framework - [PRD 101 \(2020\) 7 074015](#)
- NNLO PDFs with EW boson data from the LHC (**nuclear PDFs**) - [2112.11904](#)

Results obtained with xFitter: Examples (2)

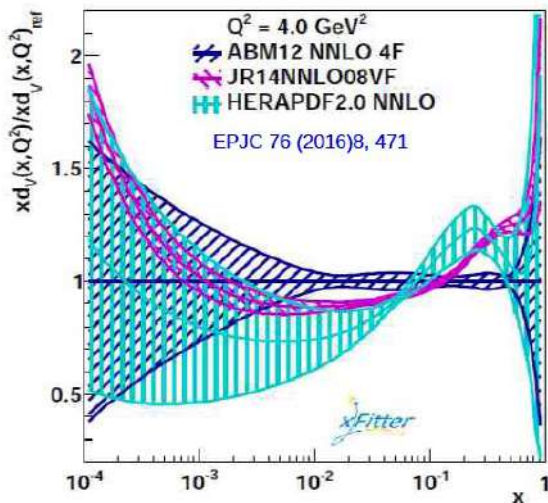
Heavy quark production ($ep, pp, p\bar{p}$)



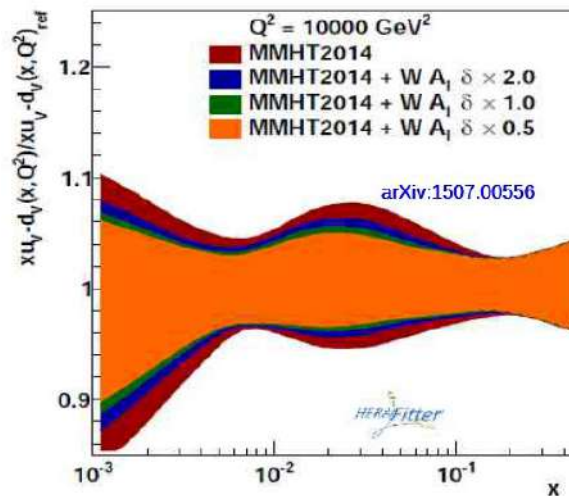
Top-quark production ($pp, p\bar{p}$)



Evolution of moder PDFs (benchmarking)



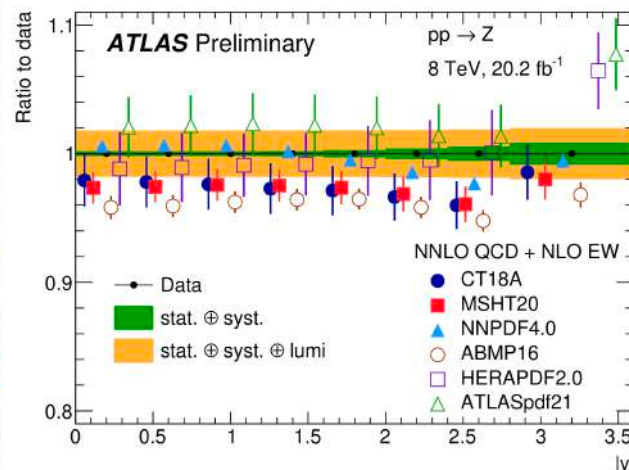
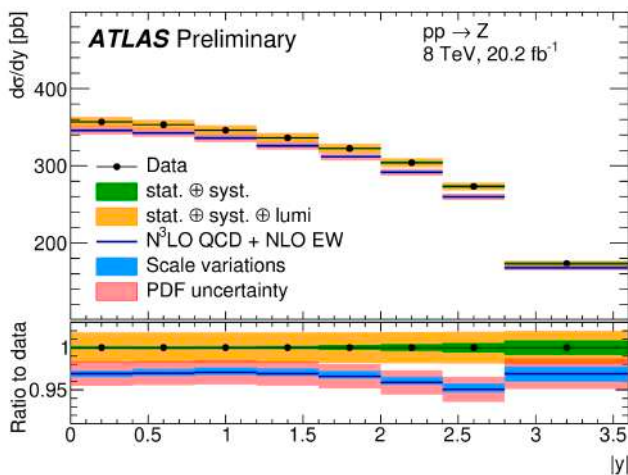
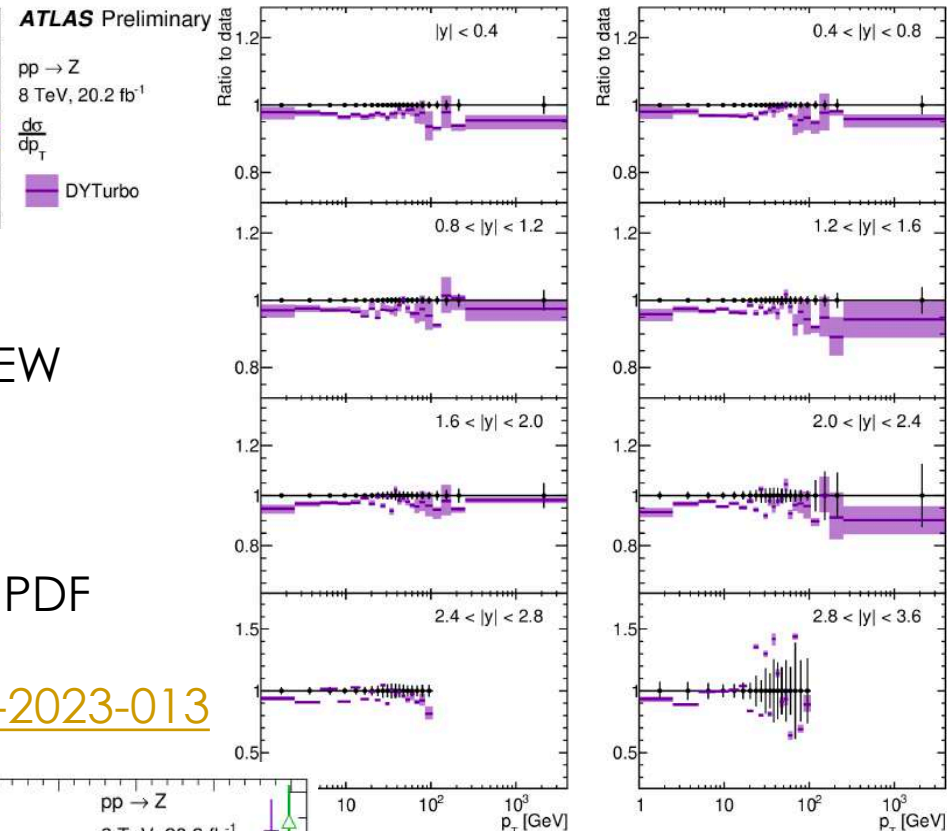
PDF4LHC report (benchmarking)



Z p_T and rapidity at 8 TeV

- Per mille level precision in the central region
- Sub-percent precision up to $|y| < 3.6$
- First comparison to N³LO QCD + NLO EW predictions ([DYTurbo](#) + [ReneSANCe](#))
- Allow precise PDF interpretations with QCD scale uncertainties smaller than PDF uncertainties

[ATLAS-CONF-2023-013](#)



**Good agreement
with several high-
order q \bar{t} -resummed
predictions**

α_s extraction from Z p_T at 8 TeV

correlated
systematic
uncertainties

$$\chi^2(\beta_{\text{exp}}, \beta_{\text{th}}) =$$

$$\sum_{i=1}^{N_{\text{data}}} \frac{\left(\sigma_i^{\text{exp}} + \sum_j \Gamma_{ij}^{\text{exp}} \beta_{j,\text{exp}} - \sigma_i^{\text{th}} - \sum_k \Gamma_{ik}^{\text{th}} \beta_{k,\text{th}} \right)^2}{\Delta_i^2} + \sum_j \beta_{j,\text{exp}}^2 + \sum_k \beta_{k,\text{th}}^2$$

uncorrelated
systematic
uncertainties

- Evaluate $\chi^2(\alpha_s)$ with α_s variations in LHAPDF
 - Include experimental ($\beta_{j,\text{exp}}$) and PDF uncertainties ($\beta_{k,\text{th}}$) in the $\chi^2(\alpha_s)$ definition
 - For each value of α_s , $\beta_{k,\text{th}}$ terms explore the PDF space to find the best fit to Z p_T data
 - aN³LO MSHT20 PDF set is used for the α_s extraction

➤ Fit Z $p_T < 29$ GeV region

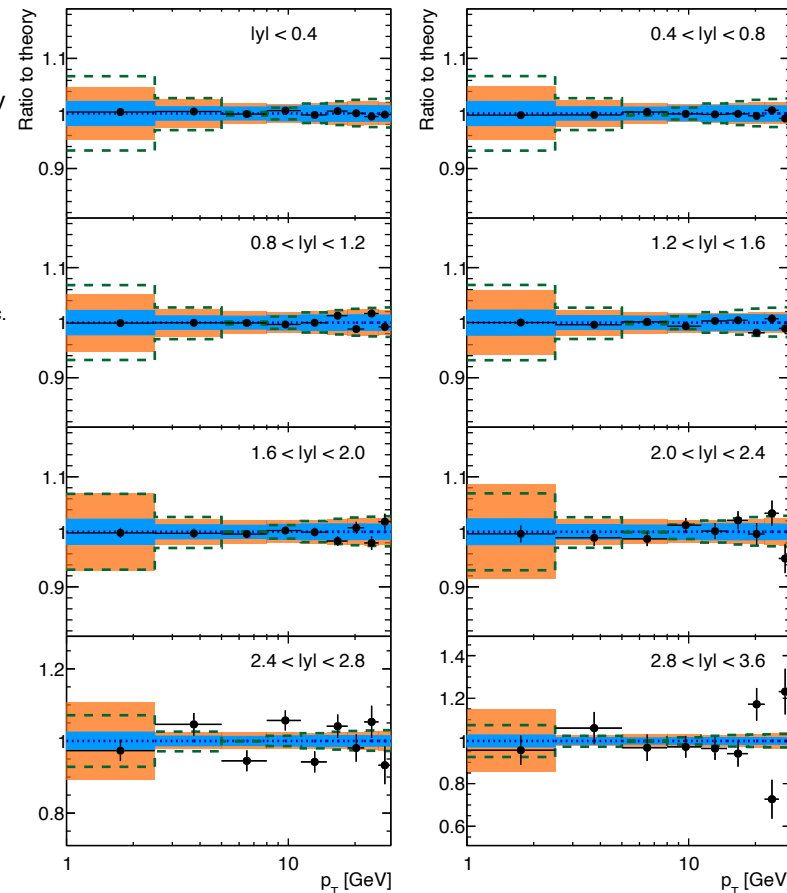
- Non-perturbative form factor (affecting Z $p_T < 5$ GeV) is added with unconstrained nuisance parameter
- $\alpha_s(m_Z)$ extracted by fitting the **2D (p_T , y) cross section** in full lepton phase space

➤ $\chi^2/\text{ndf} = 82/72$

ATLAS Preliminary

pp \rightarrow Z
8 TeV, 20.2 fb⁻¹

• Data
⋯ Post-fit
■ PDF unc.
■ PDF \oplus Theory unc.
- - $\alpha_s(m_Z) \pm 0.002$

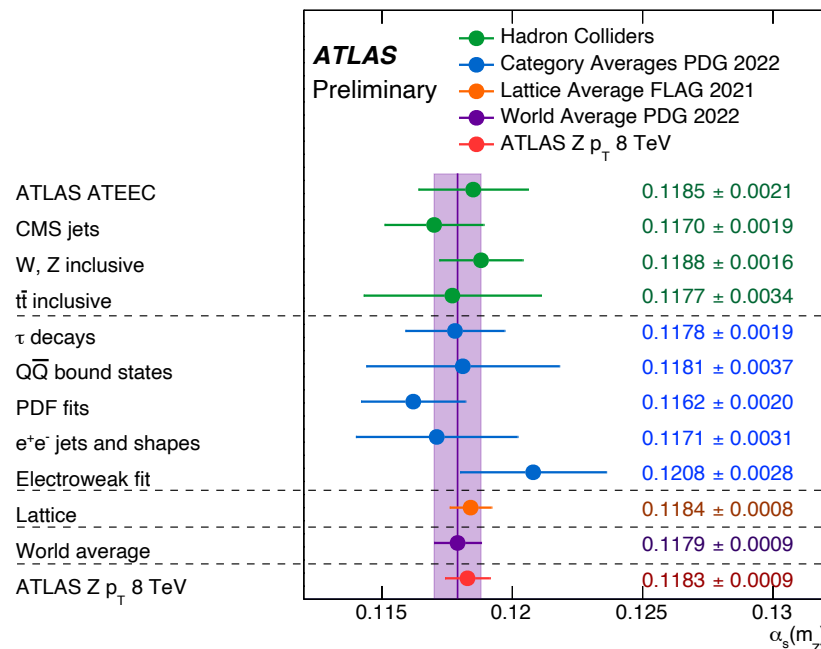
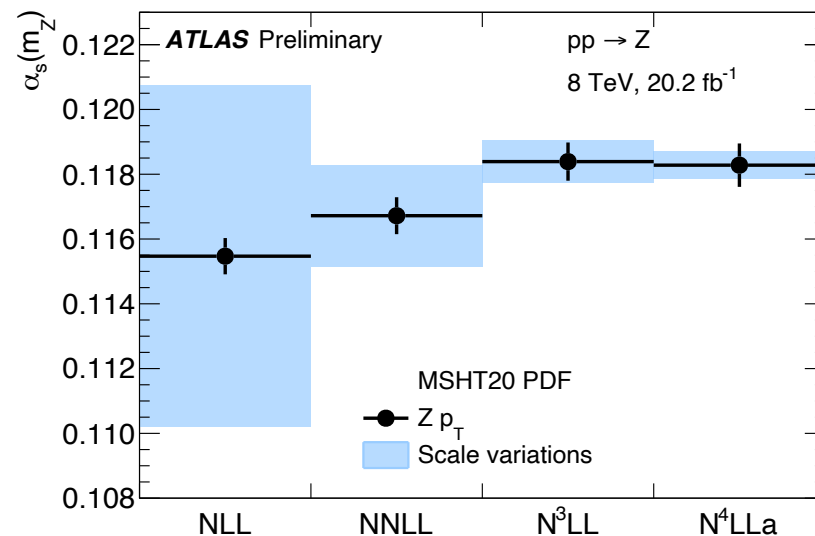


Exercise 2 - results

- **First $\alpha_s(m_Z)$ determination based on $\alpha\text{N}^4\text{LL}+\text{N}^3\text{LO}$ predictions**
- $\alpha_s(m_Z)$ determined at lower orders \rightarrow good perturbative series convergence
- **Most precise experimental determination of $\alpha_s(m_Z)$**
- [ATLAS-CONF-2023-015](#)

| | | |
|--------------------------------|-----------------|-----------------|
| Experimental uncertainty | +0.00044 | -0.00044 |
| PDF uncertainty | +0.00051 | -0.00051 |
| Scale variations uncertainties | +0.00042 | -0.00042 |
| Matching to fixed order | 0 | -0.00008 |
| Non-perturbative model | +0.00012 | -0.00020 |
| Flavour model | +0.00021 | -0.00029 |
| QED ISR | +0.00014 | -0.00014 |
| N4LL approximation | +0.00004 | -0.00004 |
| Total | +0.00084 | -0.00088 |

$$\alpha_s(m_Z) = 0.11828^{+0.00084}_{-0.00088}$$

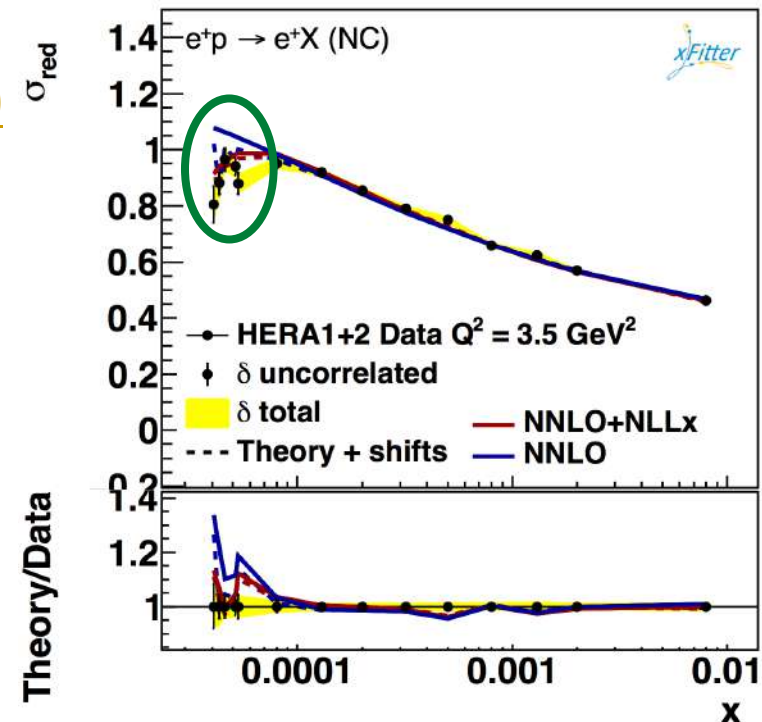


EXERCISE 4

**Including small-x
resummation corrections**

Exercise 4

- **Purpose:** Test the impact of small- x resummation corrections on PDFs
- **Data set:** Final combined HERA I+II DIS data
- **QCD order:** NNLO (+ NLLx)
- Small- x resummation formalism based on **k_T -factorization** and **BFKL**
- Developed in the 90s-00s
- Recent developments: [1607.02153](#), [1708.07510](#)
 - Resummation matched to NNLO, allowing NNLO+NLLx phenomenology
 - Public code: [HELL](#)
 - Installed automatically with the provided [install-xFitter](#) script



Small-x logarithmic enhancement

$$\sigma_{DIS} = C_i \otimes f_i$$

$$\mu^2 \frac{\partial}{\partial \mu^2} f_i(\mu) = P_{ij} \otimes f_j(\mu)$$

LO $\frac{1}{x} \alpha_S^0 [\quad 1 \quad]$

NLO $\frac{1}{x} \alpha_S [\# \log \left(\frac{1}{x} \right) + \quad 1 \quad]$

NNLO $\frac{1}{x} \alpha_S^2 [\# \log^2 \left(\frac{1}{x} \right) + \# \log \left(\frac{1}{x} \right) + \quad 1 \quad]$

N³LO $\frac{1}{x} \alpha_S^3 [\# \log^3 \left(\frac{1}{x} \right) + \# \log^2 \left(\frac{1}{x} \right) + \# \log \left(\frac{1}{x} \right) + \quad 1 \quad]$

LL

NLL

NNLL

If $\alpha_S \log \left(\frac{1}{x} \right) \sim 1 \rightarrow$ all such terms in the perturbative series are equally important

Reorganisation of the expansion:

$$\frac{1}{x} \left[1 + \# \alpha_S \log \left(\frac{1}{x} \right) + \# \alpha_S^2 \log^2 \left(\frac{1}{x} \right) + \# \alpha_S^3 \log^3 \left(\frac{1}{x} \right) + \dots \right] \quad \text{(LL)}$$

$$\frac{\alpha_S}{x} \left[1 + \# \alpha_S \log \left(\frac{1}{x} \right) + \# \alpha_S^2 \log^2 \left(\frac{1}{x} \right) + \# \alpha_S^3 \log^3 \left(\frac{1}{x} \right) + \dots \right] \quad \text{(NLL)}$$

All-order resummation

Exercise 4 - settings

- `$> cd ~/xFitterTutorial/exercise4`
- Final combined HERA+II DIS data in `steering.txt`

```
&InFiles
```

```
! Number of input files
```

```
  NInputFiles = 7
```

```
! Input files:
```

```
  InputFileNames =
```

```
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_920-thexp.dat',
```

```
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_820-thexp.dat',
```

```
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_575-thexp.dat',
```

```
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_460-thexp.dat',
```

```
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCem-thexp.dat',
```

```
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_CCep-thexp.dat',
```

```
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_CCem-thexp.dat',
```

```
&End
```

- Bonus: you can repeat this exercise with more data sets which are probing the low-x region 😊 i.e. low mass or very forward DY, J/ψ or Υ production etc.

Exercise 4 - settings

- First, we change the program to evolve PDFs: from QCDNUM to APFEL
- Then:
 - We raise the charm matching scale $\mu_c = \kappa_c \cdot m_c$ (with $m_c = 1.43$ GeV), so it can be generated perturbatively
 - We switch on the small-x resummation

```
DefaultEvolution: proton-APFELff
```

```
Evolutions:
```

```
proton-APFELff:
```

```
? !include evolutions/APFEL.yaml
decomposition: proton
kmc : 1.2 # ratio between charm quark threshold and mass
nllxResummation : "On"
```

- We change HF scheme

```
byReaction:
```

```
# FONLL scheme settings:
```

```
FONLL_DISNC:
```

```
? !include reactions/FONLL_DISNC.yaml
```

```
FONLL_DISCC:
```

```
? !include reactions/FONLL_DISCC.yaml
```

```
# Specify HF scheme used for DIS NC processes:
```

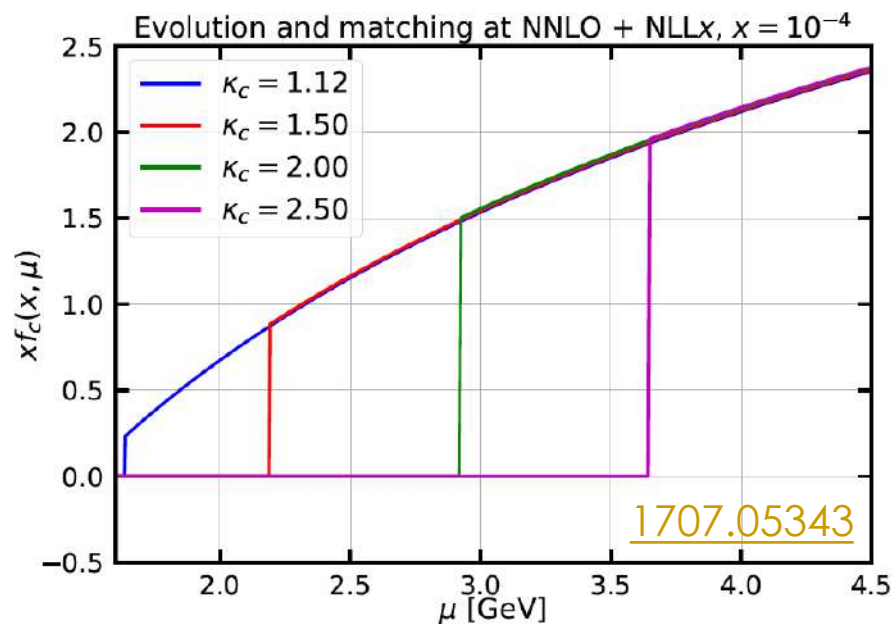
```
hf_scheme_DISNC :
```

```
  defaultValue : 'FONLL_DISNC' # global specification
```

```
# Specify HF scheme used for DIS CC processes:
```

```
hf_scheme_DISCC :
```

```
  defaultValue : 'FONLL_DISCC' # global specification
```



| | NNLO | NNLO+NLLx |
|-----------------------|-----------|-----------|
| Total χ^2 /d.o.f | 1388/1131 | 1316/1131 |

Gain in χ^2 of 72 units

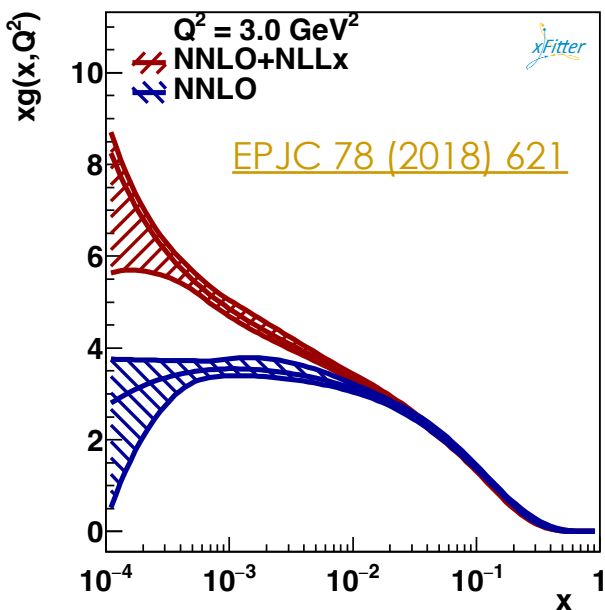
Exercise 4 - results

- To obtain datafiles: `$> ln -s ~/Software/xfitter-master/datafiles .`
- To run xFitter: `$> xfitter`
- To draw your results: `$> xfitter-draw output`
- You need to compare these PDFs with HERAPDF2.0 NNLO

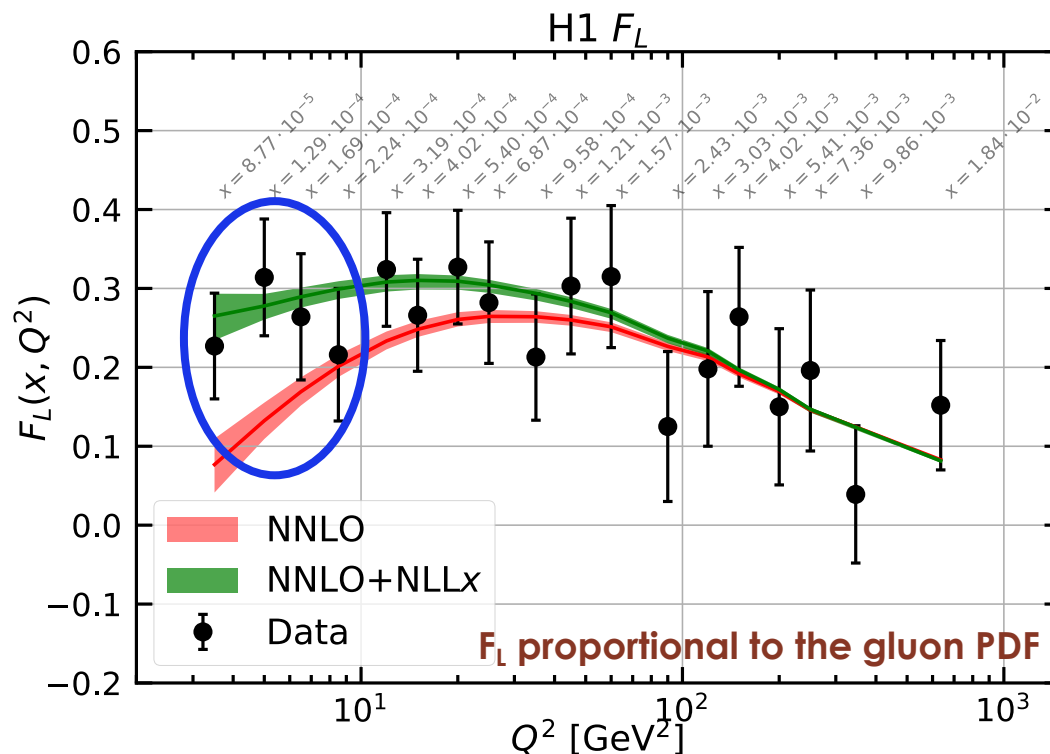
$$\sigma_{\text{red}} = F_2 - \frac{y^2}{Y_+} F_L$$

$$Y_+ = (1 + (1 - y)^2)$$

$$y = Q^2/(sx)$$



Other PDFs
unaffected



EXERCISE 5

**Add your preferred
PDF parametrisation**

Exercise 5

- **Purpose:** Test alternative PDF parametrisation
 - **Data set:** Final combined HERA-I+II DIS data
 - **QCD order:** NNLO (+ NLLx)
 - To model small-x region we proposed polynomial in $\log(x)$
 $(1 + F \log(x) + G \log^2(x) + H \log^3(x) + \dots)$
 - Considered both a multiplicative and an additive option, and we chose the latter:
[EPJ Plus \(2019\) 134, 531](#)
- $$xf(x, \mu_0^2) = Ax^B(1-x)^C[1 + Dx + Ex^2 + F \log(x) + G \log^2(x) + H \log^3(x)]$$
- Public code: [HELL](#)
 - Installed automatically with the provided [install-xFitter](#) script
 - FYI this is just one possible alternative parametrisation → many more to test!
Bernstein or Chebyshev polynomials etc.

Exercise 5 - settings

- `$> cd ~/xFitterTutorial/exercise5`
- Final combined HERA1+II DIS data in `steering.txt`

```
&InFiles
```

```
! Number of input files
```

```
  NInputFiles = 7
```

```
! Input files:
```

```
  InputFileNames =
```

```
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_920-thexp.dat',  
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_820-thexp.dat',  
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_575-thexp.dat',  
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCep_460-thexp.dat',  
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_NCem-thexp.dat',  
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_CCep-thexp.dat',  
  'datafiles/hera/h1zeusCombined/inclusiveDis/1506.06042/HERA1+2_CCem-thexp.dat',
```

```
&End
```

Exercise 5 - settings

- We need to modify the parametrization in `parameters.yaml`
- You can define as many parameters as you want
- You provide your preferred parametrization here

Parameterisations:

```

par_uv:
  class: Expression
  expression: "Auv*(x^Buv*(1-x)^Cuv)*(1+Euv*x^2+Fuv*ln(x)+Guv*ln(x)^2)"
par_dv:
  class: Expression
  expression: "Adv*(x^Bdv*(1-x)^Cdv)"
par_ubar:
  class: Expression
  expression: "Adbar*(x^Bdbar*(1-x)^Cubar)*(1+Dubar*x+Fdbar*ln(x))"
par_dbar:
  class: Expression
  expression: "Adbar*(x^Bdbar*(1-x)^Cdbar)*(1+Ddbar*x+Fdbar*ln(x))"
par_s:
  class: Expression
  expression: "Adbar*fs/(1-fs)*(x^Bdbar*(1-x)^Cdbar)*(1+Ddbar*x+Fdbar*ln(x))"
par_g:
  class: Expression
  expression: "Ag*(x^Bg*(1-x)^Cg)*(1+Fg*ln(x)+Gg*ln(x)^2)"

```

Parameters:

```

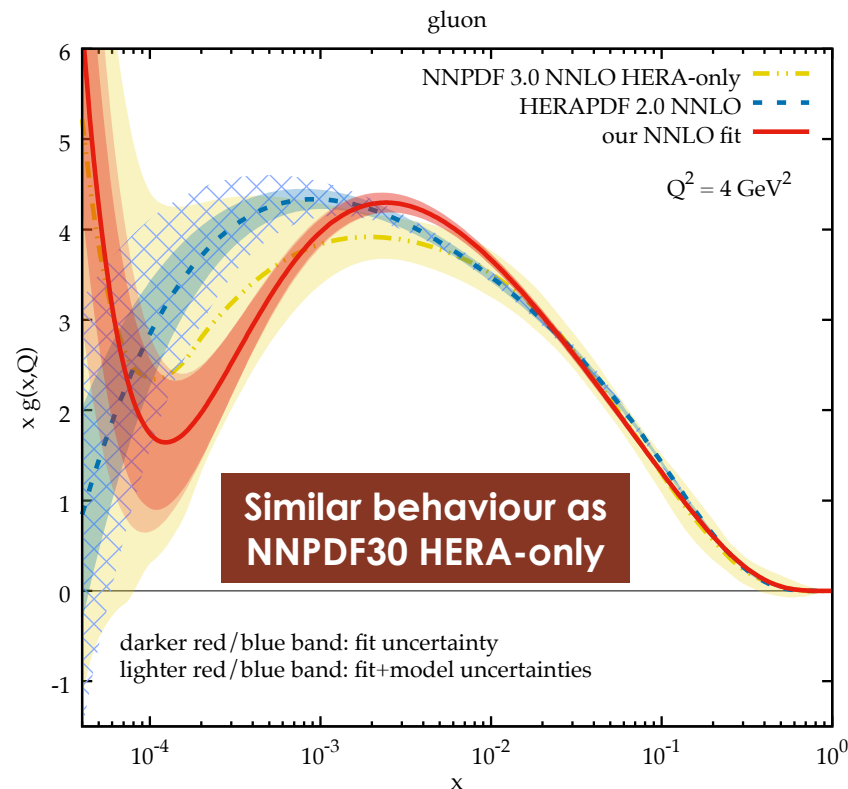
Ag   : DEPENDENT
Bg   : [ -0.5009, 0.0060 ]
Cg   : [ 4.4885, 0.1944 ]
Fg   : [ 0.2156, 0.0005 ]
Gg   : [ 0.0119, 0.0010 ]
Auv  : DEPENDENT
Buv  : [ 0.7392, 0.0021 ]
Cuv  : [ 4.5845, 0.0170 ]
Euv  : [ 2.7839, 0.0633 ]
Fuv  : [ 0.3416, 0.0027 ]
Guv  : [ 0.0470, 0.0040 ]
Adv  : DEPENDENT
Bdv  : [ 0.9882, 0.0108 ]
Cdv  : [ 4.6983, 0.0742 ]
Cubar: [ 10.9607, 0.2749 ]
Dubar: [ 17.2935, 0.2808 ]
Adbar: [ 0.0854, 0.0241 ]
Bdbar: [ -0.3354, 0.0031 ]
Cdbar: [ 23.8266, 0.9917 ]
Ddbar: [ 35.0368, 4.5302 ]
Fdbar: [ 0.0744, 0.0011 ]
ZERO : 0
fs   : [ 0.4, 0.0 ]

```

- You can also switch on small-x resummation (see Exercise 4) to check if any improvement in χ^2

Exercise 5 - results

- To obtain datafiles: `$> ln -s ~/Software/xfitter-master/datafiles .`
- To run xFitter: `$> xfitter`
- To draw your results: `$> xfitter-draw output`
- You need to compare these PDFs with HERAPDF2.0 NNLO



| Contribution to χ^2 | HERAPDF2.0 | Our fit (new parametrization) |
|--|------------------|-------------------------------|
| subset NC e^+ 920 $\tilde{\chi}^2/\text{n.d.p.}$ | 444/377 | 403/377 |
| subset NC e^+ 820 $\tilde{\chi}^2/\text{n.d.p.}$ | 66/70 | 74/70 |
| subset NC e^+ 575 $\tilde{\chi}^2/\text{n.d.p.}$ | 219/254 | 221/254 |
| subset NC e^+ 460 $\tilde{\chi}^2/\text{n.d.p.}$ | 217/204 | 222/204 |
| subset NC e^- $\tilde{\chi}^2/\text{n.d.p.}$ | 219/159 | 220/159 |
| subset CC e^+ $\tilde{\chi}^2/\text{n.d.p.}$ | 45/39 | 38/39 |
| subset CC e^- $\tilde{\chi}^2/\text{n.d.p.}$ | 56/42 | 50/42 |
| correlation term + log term | 91 + 5 | 75 - 3 |
| Total $\chi^2/\text{d.o.f.}$ | 1363/1131 | 1301/1127 |

- If small-x resummation included, further gain of 28 units in χ^2
- **The addition of small-x resummation is thus very important**

EXERCISE 6

ATLASepWZ16: fixed vs free r_s

Exercise 6

- **Purpose:** Reproduce the ATLASepWZ16 fit results and χ^2 comparison for two different cases → fixed VS free r_s
- **Data set:** Final combined HERAI+II DIS data and ATLAS W,Z precise measurement at 7 TeV
- Below the datasets we need to add to the steering.txt file:

```
'datafiles/lhc/atlas/wzProduction/1612.03016/wminus-thexp.dat',  
'datafiles/lhc/atlas/wzProduction/1612.03016/wplus-thexp.dat',  
'datafiles/lhc/atlas/wzProduction/1612.03016/zyhigh_cc-thexp.dat',  
'datafiles/lhc/atlas/wzProduction/1612.03016/zyhigh_cf-thexp.dat',  
'datafiles/lhc/atlas/wzProduction/1612.03016/zypeak_cc-thexp.dat',  
'datafiles/lhc/atlas/wzProduction/1612.03016/zypeak_cf-thexp.dat',
```
- We also need to apply a cut on the minimum Q^2 of the data to enter the fit to be greater than 10 GeV – so we are not sensitive to non-perturbative effects i.e. higher-twist, small-x logarithmic enhancement, etc.
- Do you remember how to do it?
 - Hint: look inside steering.txt ☺

Exercise 6

- Two different folders:

```
$> cd ~/xFitterTutorial/exercise6/rsFixed
```

```
$> cd ~/xFitterTutorial/exercise6/rsFree
```

$$r_s = \frac{f_s}{1 - f_s}$$

$$f_s = \frac{r_s}{1 + r_s}$$

- Then, we have to freeze/free r_s parameter in the `parameters.yaml` file

- ATLASepWZ16 $\rightarrow r_s \sim 1.19$ so $f_s \sim 0.54$

Parameters:

```
rs : [ 1.1007, 0.1785 ]
```

Proposed range to scan:
 $0.91 < r_s < 1.21$

- FYI in HERAII $\rightarrow f_s = 0.4$ (fixed) so $r_s \sim 0.667$

- To obtain datafiles:

```
$> ln -s ~/Software/xfitter-master/datafiles .
```

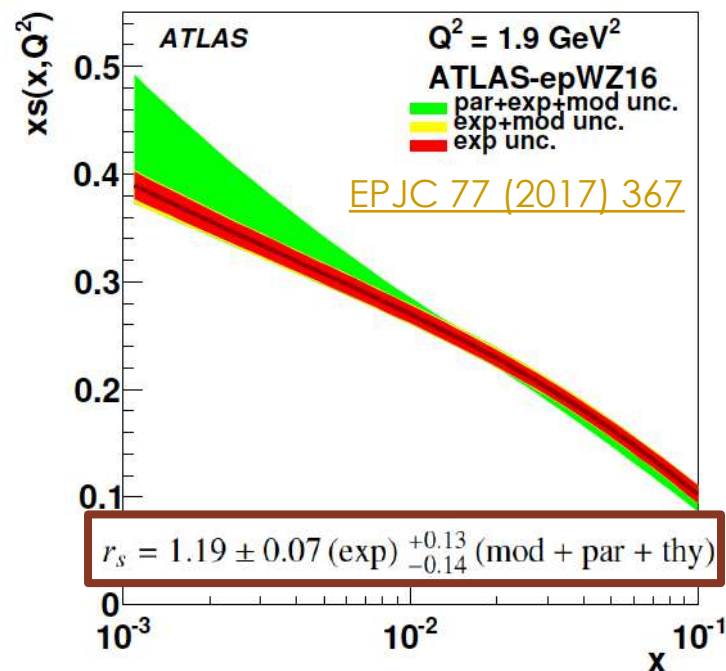
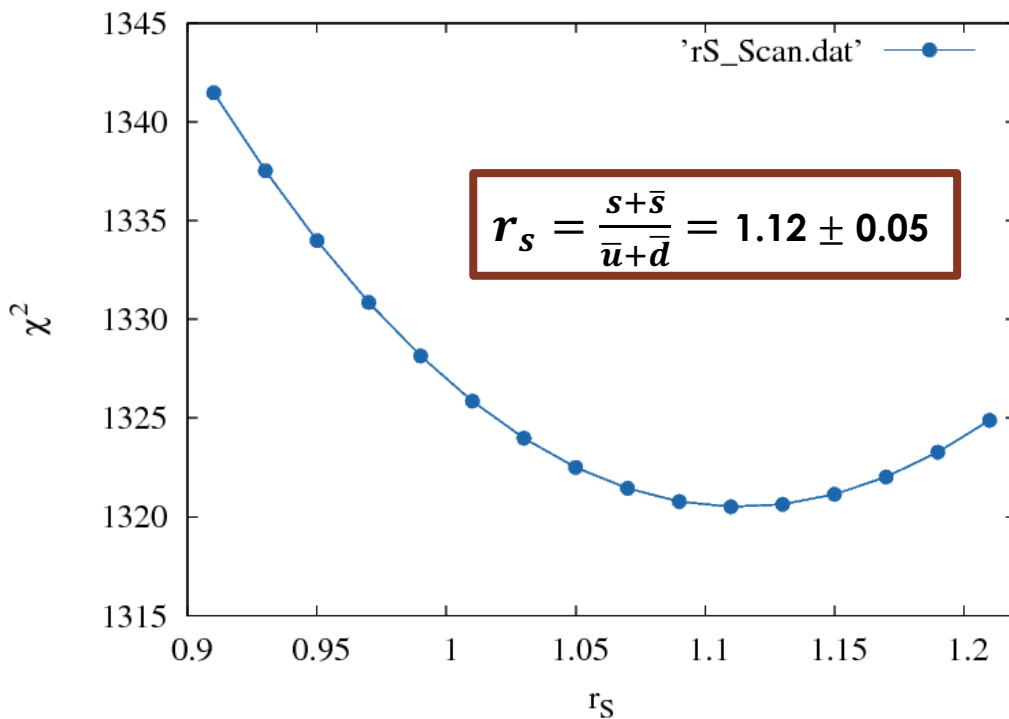
- To run xFitter:

```
$> xfitter
```

- To draw your results:

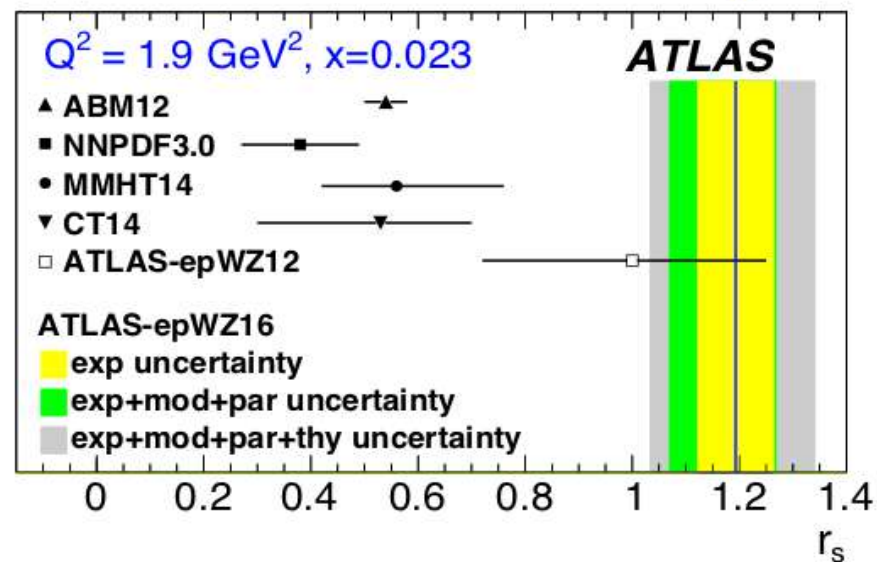
```
$> xfitter-draw rsFixed rsFree
```

Exercise 6 - Results



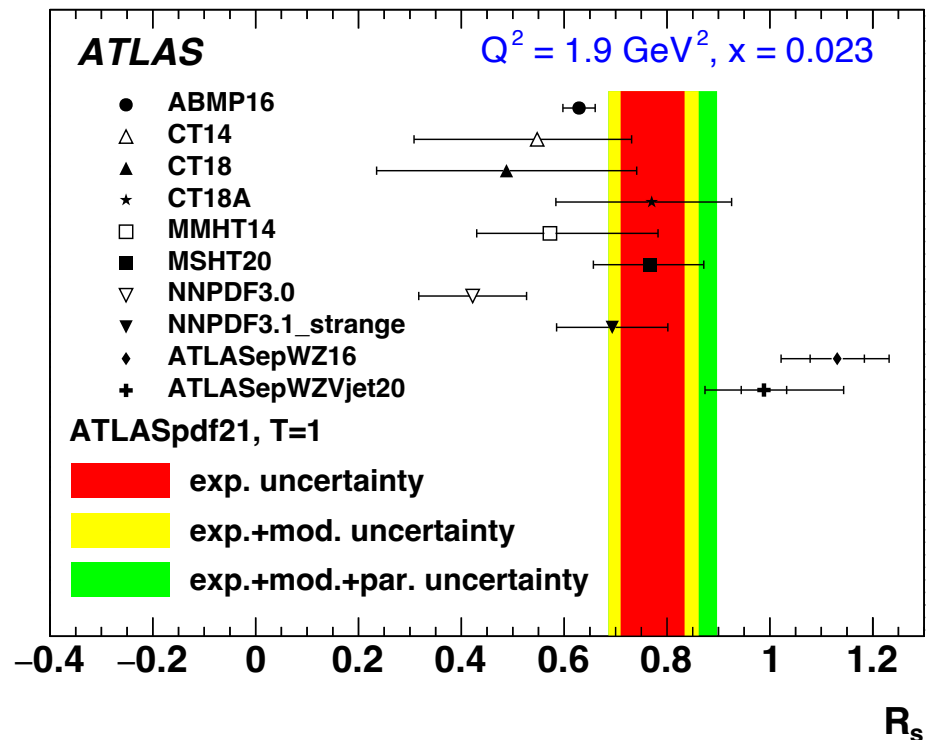
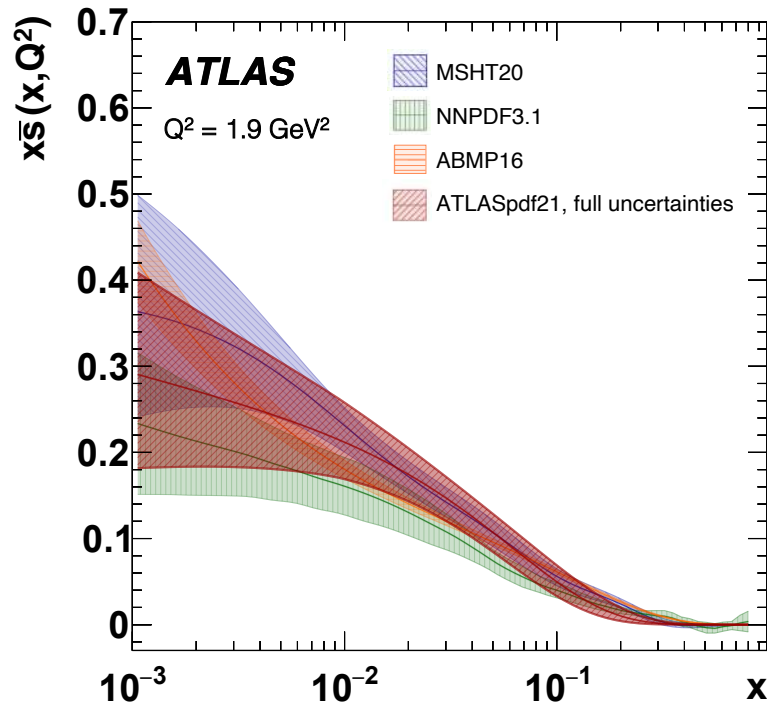
Enhanced r_s confirmed!

The two approaches give compatible results



Exercise 6 - bonus

- What happens if you start adding more and more ATLAS data?
- **ATLASpdf21** is a PDF fit to **multiple ATLAS data sets** - [EPJC 82 \(2022\) 5, 438](#)
 - [Fit example](#) + [data files](#) (to reproduce published results)
- **ATLAS r_s** has come **DOWN** from ~ 1.2 to 0.8
- **MSHT, CT** and **NNPDF r_s** have come **UP** from ~ 0.5 to 0.8 when including W,Z 7 TeV ATLAS data



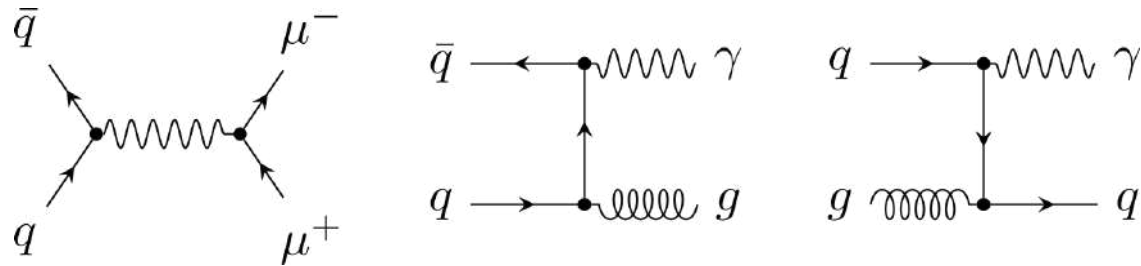
EXERCISE 7

Charged pion PDF

Exercise 7

- **Purpose:** Extract the charged pion PDF (poorly studied experimentally)

- **Data set:** Data from **E615**, **NA10** and **WA70** experiments (di-muon and direct photon production)



- Charge symmetry $d = \bar{u}$ and SU(3)-symmetric sea $u = \bar{d} = s = \bar{s}$ at the initial scale $Q_0^2 = 1.9 \text{ GeV}^2$

$$v := (d - \bar{d}) - (u - \bar{u}),$$

$$xv(x) = A_v x^{B_v} (1-x)^{C_v} (1 + D_v x^{\frac{5}{2}}),$$

$$S := 2u + 2\bar{d} + s + \bar{s} = 6u,$$

$$xs(x) = A_S x^{B_S} (1-x)^{C_S},$$

$$g := g,$$

$$xg(x) = A_g x^{B_g} (1-x)^{C_g}.$$

- The A_v and A_g parameters are determined by the sum rules:

$$\int_0^1 v(x) dx = 2,$$

$$\int_0^1 x(v(x) + S(x) + g(x)) dx = 1$$

Exercise 7 - settings

➤ \$> cd ~/xFitterTutorial/exercise7

➤ We need to add data from **E615**, **NA10** and **WA70** experiments in the steering.txt file

```
InputFileNames =
```

```
'datafiles/fixedTarget/NA10/thexp-0.dat',
'datafiles/fixedTarget/NA10/thexp-1.dat',
'datafiles/fixedTarget/NA10/thexp-2.dat',
'datafiles/fixedTarget/NA10/thexp-3.dat',
'datafiles/fixedTarget/NA10/thexp-4.dat',
'datafiles/fixedTarget/NA10/thexp-5.dat',
'datafiles/fixedTarget/NA10/thexp-6.dat',
'datafiles/fixedTarget/NA10/thexp-7.dat',
'datafiles/fixedTarget/NA10/thexp-8.dat',
'datafiles/fixedTarget/WA70/thexp-0.dat',
'datafiles/fixedTarget/WA70/thexp-1.dat',
'datafiles/fixedTarget/WA70/thexp-2.dat',
'datafiles/fixedTarget/WA70/thexp-3.dat',
'datafiles/fixedTarget/WA70/thexp-4.dat',
'datafiles/fixedTarget/WA70/thexp-5.dat',
'datafiles/fixedTarget/WA70/thexp-6.dat',
'datafiles/fixedTarget/WA70positive/thexp-0.dat',
'datafiles/fixedTarget/WA70positive/thexp-1.dat',
'datafiles/fixedTarget/WA70positive/thexp-2.dat',
'datafiles/fixedTarget/WA70positive/thexp-3.dat',
'datafiles/fixedTarget/WA70positive/thexp-4.dat',
'datafiles/fixedTarget/WA70positive/thexp-5.dat',
'datafiles/fixedTarget/WA70positive/thexp-6.dat',
```

```
'datafiles/fixedTarget/NA10-286/thexp-0.dat',
'datafiles/fixedTarget/NA10-286/thexp-1.dat',
'datafiles/fixedTarget/NA10-286/thexp-2.dat',
'datafiles/fixedTarget/NA10-286/thexp-3.dat',
'datafiles/fixedTarget/NA10-286/thexp-4.dat',
'datafiles/fixedTarget/NA10-286/thexp-5.dat',
'datafiles/fixedTarget/NA10-286/thexp-6.dat',
'datafiles/fixedTarget/NA10-286/thexp-7.dat',
'datafiles/fixedTarget/NA10-286/thexp-8.dat',
'datafiles/fixedTarget/NA10-286/thexp-9.dat',
'datafiles/fixedTarget/NA10-286/thexp-10.dat',
'datafiles/fixedTarget/E615/thexp-0.dat',
'datafiles/fixedTarget/E615/thexp-1.dat',
'datafiles/fixedTarget/E615/thexp-2.dat',
'datafiles/fixedTarget/E615/thexp-3.dat',
'datafiles/fixedTarget/E615/thexp-4.dat',
'datafiles/fixedTarget/E615/thexp-5.dat',
'datafiles/fixedTarget/E615/thexp-6.dat',
'datafiles/fixedTarget/E615/thexp-7.dat',
'datafiles/fixedTarget/E615/thexp-8.dat',
'datafiles/fixedTarget/E615/thexp-9.dat',
'datafiles/fixedTarget/E615/thexp-13.dat',
'datafiles/fixedTarget/E615/thexp-14.dat',
'datafiles/fixedTarget/E615/thexp-15.dat',
'datafiles/fixedTarget/E615/thexp-16.dat',
'datafiles/fixedTarget/E615/thexp-17.dat',
```

Exercise 7 - settings

- We need to modify the parametrization in `parameters.yaml`, as well as decomposition

Parameters:

```
Av: SUMRULE
Bv: [ 0.75,0.03]
Cv: [ 0.95,0.04, 0,10]
As: [ 0.21,0.1]
Bs: [ 0.5 ,0.1,-1,10]
Cs: [ 8,3]
Ag: SUMRULE
Bg: 0
Cg: [ 3,1]
```

Parameterisations:

```
v:
  class: HERAPDF
  parameters: [Av,Bv,Cv]
S:
  class: Normalized
  parameters: [As,Bs,Cs]
g:
  class: Normalized
  parameters: [Ag,Bg,Cg]
```

Decompositions:

```
pion:
  class: SU3_Pion
  valence: v
  sea: S
  gluon: g
```

- We also need to change evolution, and define it for both π^+ and π^-

Evolutions:

```
negative_pion:
  ? !include evolutions/QCDNUM.yaml
  decomposition: pion
positive_pion:
  class: FlipChange
  input: negative_pion
tungsten_target:
  class: LHAPDF
  set: nCTEQ15FullNuc_184_74
  member: 0
proton:
  class: LHAPDF
  set: nCTEQ15FullNuc_1_1
  member: 0
DefaultEvolution: negative_pion
```

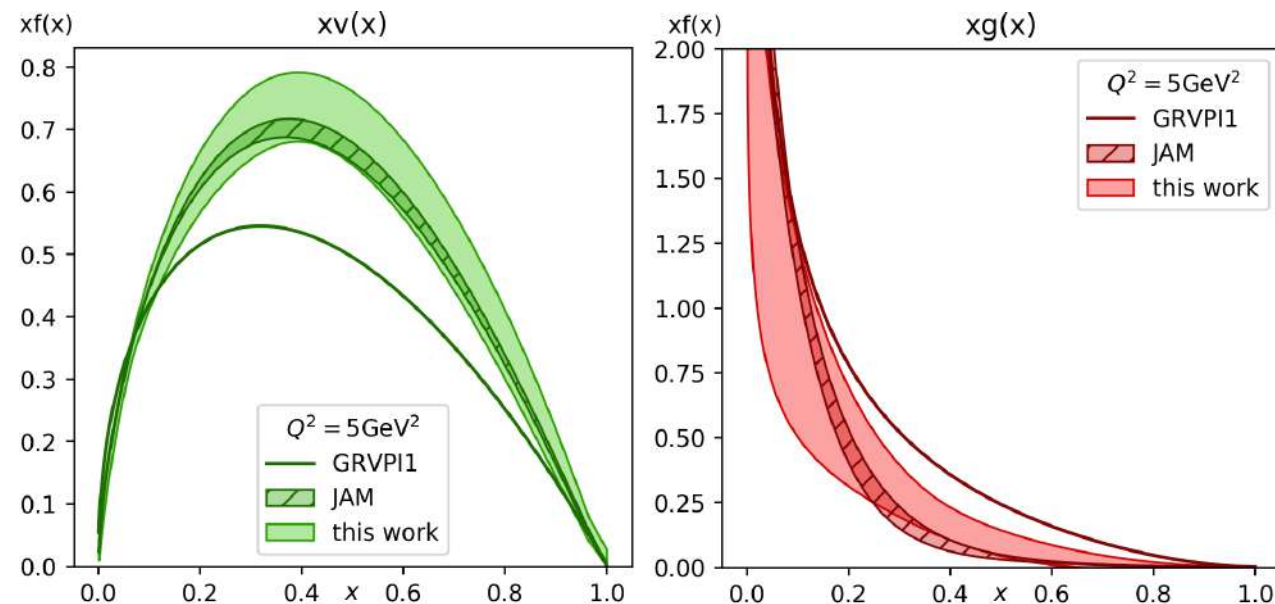
Nice feature! In this way you have the same evolution used for π^- , just with inverted charged

We have to define a nuclear PDF set for both the incoming proton and the target (tungsten in this case)

Exercise 7 - results

- To obtain datafiles: `$> ln -s ~/Software/xfitter-master/datafiles .`
- To run xFitter: `$> xfitter`
- To draw your results: `$> xfitter-draw output`
- You need to compare these PDFs with i.e. JAM or GRVPI1
- Valence and gluon distributions in good agreement with JAM and both disagree with the early GRV analysis

[Phys. Rev. D 102 \(2020\) 014040](#)



| Experiment | χ^2/N_{points} |
|----------------|----------------------------|
| E615 | 194/140 |
| NA10 (194 GeV) | 98/67 |
| NA10 (286 GeV) | 92/73 |
| WA70 | 74/99 |

EXERCISE 8

Charged pion Fragmentation Functions

Exercise 8

- **Purpose:** Extract the charged pion **fragmentation functions** (FFs)
- **Data set:** Single inclusive electron-positron annihilation (SIA) + BELLE13/20 data
- **Parametrization form:**
$$D_i^{\pi^\pm}(z, Q_0) = \frac{\mathcal{N}_i z^{\alpha_i} (1-z)^{\beta_i} [1 + \gamma_i (1-z)^{\delta_i}]}{B[2+\alpha_i, \beta_i+1] + \gamma_i B[2+\alpha_i, \beta_i+\delta_i+1]}$$
- We assume isospin symmetry $D_u^{\pi^+} = D_{\bar{d}}^{\pi^-}$ and $D_{\bar{u}}^{\pi^+} = D_d^{\pi^-}$
- We assume the charge conjugate $D_i^{\pi^+} = D_i^{\pi^-}$ for all the flavour component
- We fit the flavour combinations $i = u^+, d^+, s^+, c^+, b^+$ and g
- We parametrise FFs at a starting scale of $Q_0^2 = 5 \text{ GeV}^2$
- **19 free parameters in total**
- Fitted distributions: $\frac{d\sigma^h}{dz}, \frac{1}{\sigma_{\text{tot}}} \frac{d\sigma^h}{dp_h}, \frac{s}{\beta} \frac{d\sigma^h}{dz}, \frac{1}{\beta\sigma_{\text{tot}}} \frac{d\sigma^h}{dz}, \dots$ ($z = 2E_h/\sqrt{s}$)

Exercise 8 - settings

➤ `$> cd ~/xFitterTutorial/exercise8`

➤ We need to add SIA and BELLE13/20 data in the `steering.txt` file

```
NInputFiles = 17
  InputFileNames =
! Input files:
!   4 active flavour
      'datafiles/NC_SIA/BABAR/inclusive/BABAR_inclusive_pi_o.dat',
      'datafiles/NC_SIA/BELLE20/BELLE20_inclusive_pi_1.dat'

!   Inclusive
      'datafiles/NC_SIA/ALEPH/inclusive/ALEPH_inclusive_pi_h.dat',
      'datafiles/NC_SIA/DELPHI/inclusive/DELPHI_inclusive_pi.dat',
      'datafiles/NC_SIA/OPAL/inclusive/OPAL_inclusive_pi.dat',
      'datafiles/NC_SIA/SLD/inclusive/SLD_inclusive_pi.dat',
      'datafiles/NC_SIA/TASSO/inclusive/TASSO_12_inclusive_pi.dat',
      'datafiles/NC_SIA/TASSO/inclusive/TASSO_14_inclusive_pi.dat',
      'datafiles/NC_SIA/TASSO/inclusive/TASSO_22_inclusive_pi.dat',
      'datafiles/NC_SIA/TASSO/inclusive/TASSO_34_inclusive_pi.dat',
      'datafiles/NC_SIA/TASSO/inclusive/TASSO_44_inclusive_pi.dat',
      'datafiles/NC_SIA/TPC/TPC_inclusive_pi.dat',

!   b tag
      'datafiles/NC_SIA/DELPHI/b_tag/DELPHI_b_tag_pi.dat',
      'datafiles/NC_SIA/SLD/b_tag/SLD_b_tag_pi.dat',

!   c tag
      'datafiles/NC_SIA/SLD/c_tag/SLD_c_tag_pi.dat',

!   light tag
      'datafiles/NC_SIA/DELPHI/light_tag/DELPHI_light_tag_pi_o.dat',
      'datafiles/NC_SIA/SLD/light_tag/SLD_light_tag_pi.dat',
```

Exercise 8 - settings

- We need to modify the parametrization in `parameters.yaml`, as well as decomposition

Parameters:

```

ABp : [ 1.0199, 0.01618693 ]
ACp : [ 1.1305, 0.01827819 ]
ASp : [ 0.7049, 0.09370628 ]
Ag : [ 2.0073, 0.03766856 ]
Aup : [ 1.4261, 0.04923525 ]
BBp : [ -0.4543, 0.04601485 ]
BCp : [ -1.0443, 0.04583320 ]
BSp : [ -0.5754, 0.55702822 ]
Bg : [ 3.3722, 0.37066418 ]
Bup : [ -0.7829, 0.04777496 ]
CBp : [ 3.9881, 0.22672656 ]
CCp : [ 4.6312, 0.16315390 ]
CSp : [ 8.7524, 1.01469245 ]
Cg : [ 58.3529, 3.15872362 ]
Cup : [ 1.6871, 0.02898839 ]
DBp : [ 17.0749, 1.31370713 ]
DCp : [ 0.00000000, 0.00000000 ]
DSp : [ 0.00000000, 0.00000000 ]
Dg : [ 0.00000000, 0.00000000 ]
Dup : [ 5.1060, 0.61927213 ]
EBp : [ 9.0314, 0.68378218 ]
ECp : [ 0.00000000, 0.00000000 ]
ESp : [ 0.00000000, 0.00000000 ]
Eg : [ 0.00000000, 0.00000000 ]
Eup : [ 4.0594, 0.32218262 ]
ZERO : [ 0.00000000, 0.00000000 ]

```

Parameterisations:

```

par_up:
  class: Pion_FF
  parameters: [Aup,Bup,Cup,Dup,Eup]
par_cp:
  class: Pion_FF
  parameters: [ACp,BCp,CCp,DCp,ECp]
par_bp:
  class: Pion_FF
  parameters: [ABp,BBp,CBp, DBp, EBp]
par_sp: # s=fs/(1-fs) * Dbar
  class: Pion_FF
  parameters: [ASp,BSp,CSp,DSp,ESp]
par_g:
  class: Pion_FF
  parameters: [Ag,Bg,Cg,Dg,Eg]

```

DefaultDecomposition: Pion_FF_B_C

Decompositions:

```

Pion_FF_B_C: #proton:
  class: Pion_FF_BC
  xup: par_up
  xcp: par_cp
  xbp: par_bp
  xsp: par_sp
  xg: par_g

```

DefaultEvolution: proton-APFELff

Evolutions:

```

proton-APFELff:
  ? !include evolutions/APFEL.yaml
  fragmentation : "on"
  decomposition: Pion_FF_B_C #proton
proton-LHAPDF:
  class: LHAPDF
  set: "NNPDF30_nlo_as_0118"
  #set: "CT10nlo"
  member: 0
antiproton:
  class: FlipCharge
  #input: proton-QCDNUM
  input: proton-LHAPDF

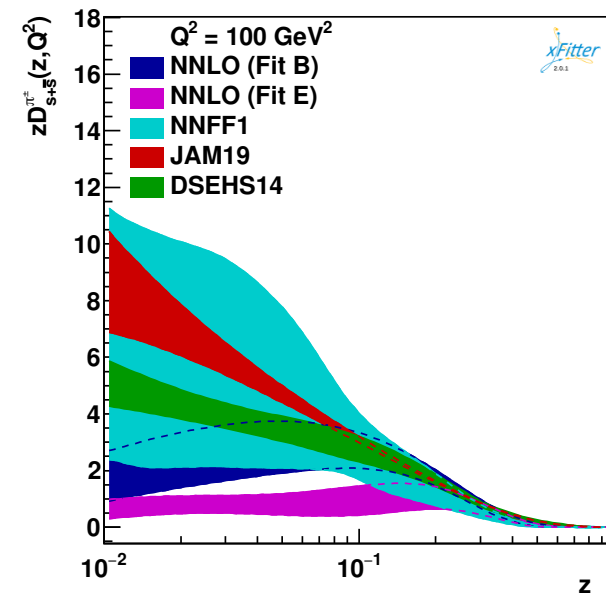
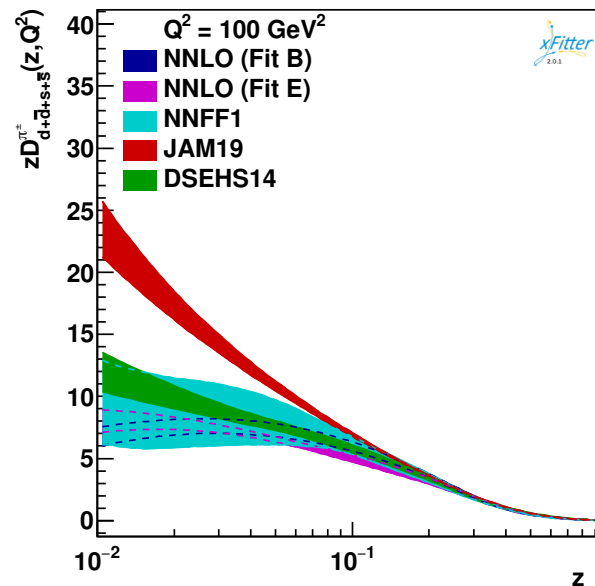
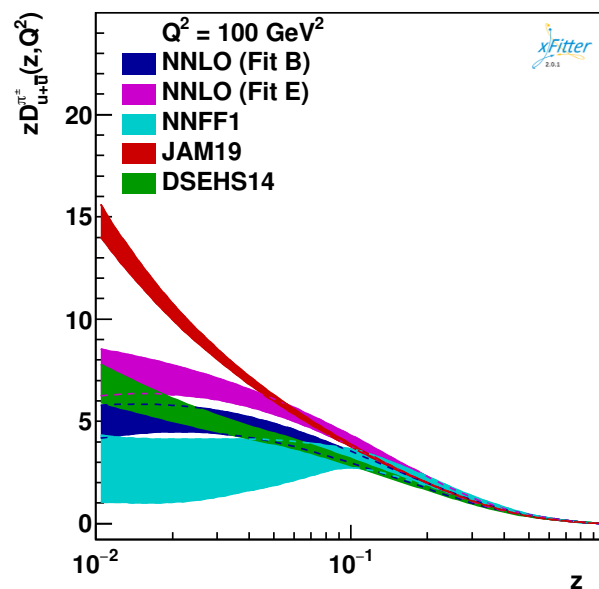
```

- We also need to change evolution – to study antiproton, we used the same trick used for π^+ in Exercise 7 (FlipCharge)

Exercise 8 - results

- To obtain datafiles: `$> ln -s ~/Software/xfitter-master/datafiles .`
- To run xFitter: `$> xfitter`
- To draw your results: `$> xfitter-draw output`
- You can compare these PDFs with NNLO NNFF1 and NLO JAM19 and DSEHS14
- **Generally compatible with NNFF1 and DSEHS14 at larger z** , but they differ at low- z (more pronounced for Fit E)

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How to generate fixed order predictions

- First of all, you need to download APPLgrid from [here](#)
 - You can download the latest version available 1.6.32
- Then you need to download aMC@NLO from [here](#)
 - I would recommend you to download version 2.9.X/3.5.X (standard in ATLAS)
- After having installed aMC@NLO you need to generate the process you want to simulate, so e.g. $p p \rightarrow l \nu l$. An example set of commands might be:

```
import model loop_sm-no_b_mass
define p = p b b~
define j = p
define l = e+ e- mu+ mu-
define vl = ve ve~ vm vm~
generate p p > l vl [NLO]
output run_Wlnu
```

If you have doubts, please follow the instructions on any MG5_aMC@NLO tutorial to produce this process

- Then download aMCfast and follow the instructions described [here](#)
- At this stage, you need to write your analysis file (I would suggest the top-drawer format). You have lots of examples in the FOAnalysis folder, please have a look there
 - It is in fortran, but it should be pretty straightforward to understand how to define new distribution

How to generate fixed order predictions

➤ Then you have to run first a preparatory run

➤ To perform this preparatory run, we set in the run card

```
1 = iappl ! aMCfast switch (0=OFF, 1=prepare APPLgrids, 2=fill grids)
```

➤ Since at this stage the interpolation grids are not filled up, there is no need of a high accuracy, thus setting something like `0.01 = req_acc_F0` in the run card is enough

➤ If the run finishes successfully, the code will have created the starting grid that now need to be filled up. So we have to run again the code giving: `launch -o` ("-o" ensures that the code restarts the run from the grids generated in the previous run)

➤ Now for this second run, we only need to edit the run card and to set:

```
2 = iappl ! aMCfast switch (0=OFF, 1=prepare APPLgrids, 2=fill grids)
```

➤ In addition, we might want to increase the accuracy of the integration by setting, for example: `0.001 = req_acc_F0`

➤ Requiring an higher accuracy should get rid of the statistical fluctuation