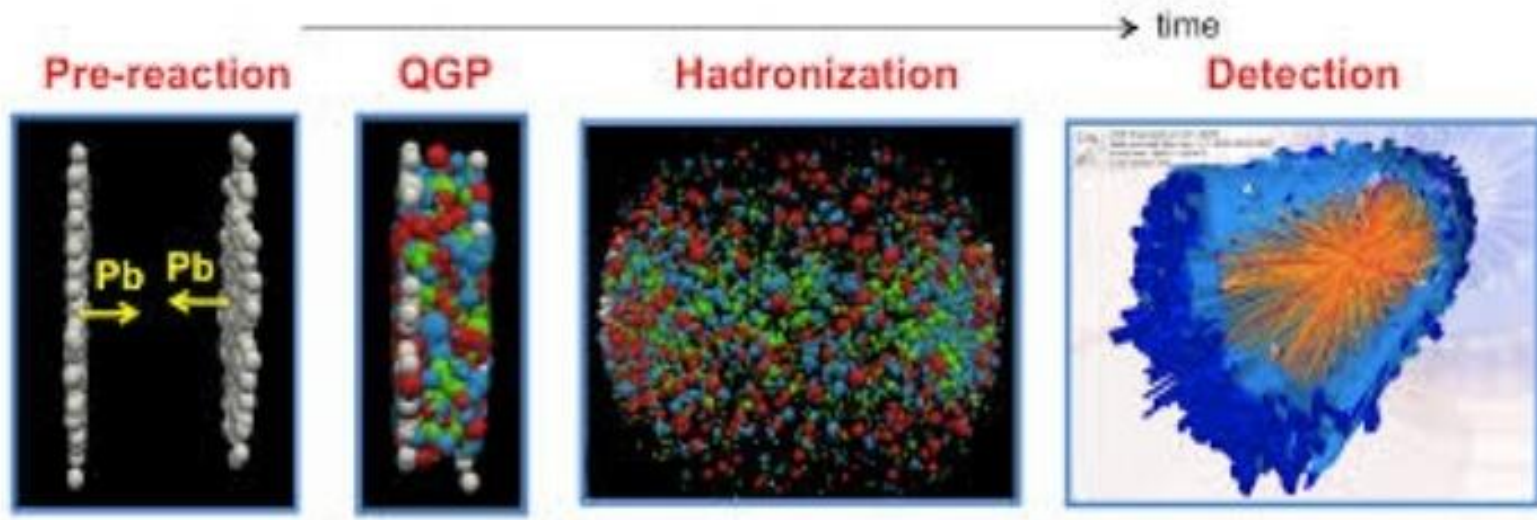


# Open heavy flavors: Theory



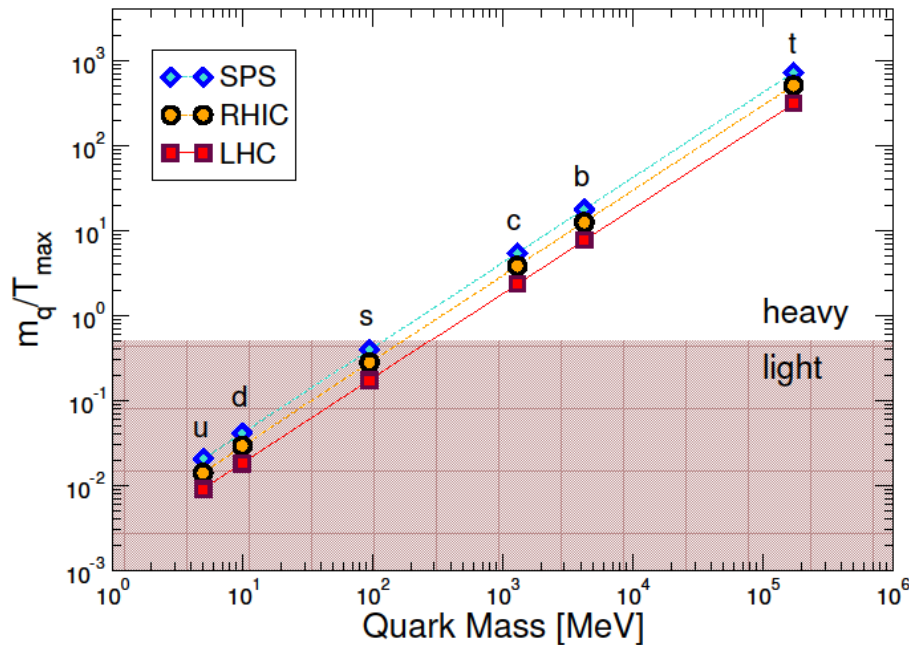
**Santosh Kumar Das**  
**School of Physical Science**  
**Indian Institute of Technology Goa**  
**Goa, India**



## **OUTLINE**

- ❑  **$R_{AA}$  vs  $v_2$ : Heavy quark diffusion**  
D<sub>s</sub>, Heavy quark thermalization
  
- ❑ **Recent developments**  
New observables, Radiation, Hadronization  
Non-equilibrium effect, Small system
  
- ❑ **Heavy quark as a probe of Initial stage**  
EM fields, Glasma, Verticity

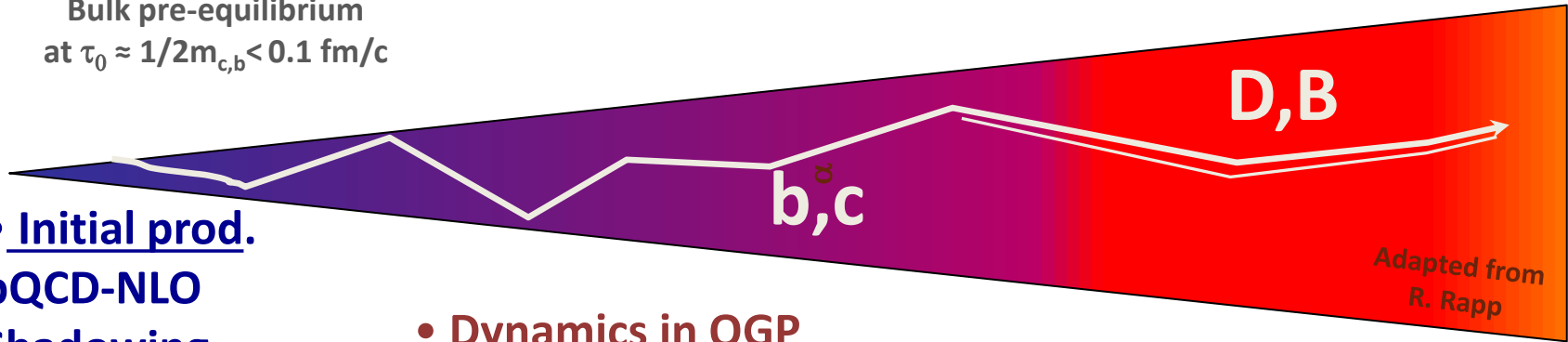
# Heavy Quark in Quark-Gluon Plasma



- $m_{c,b} \gg \Lambda_{\text{QCD}}$  pQCD initial production
- $m_{c,b} \gg T_{\text{RHIC,LHC}}$  negligible thermal production (not @FCC)
- $\tau_0 < 0.08 \text{ fm}/c \ll \tau_{\text{QGP}}$  witness of all the QGP evolution
- $\tau_{\text{th}} \approx \tau_{\text{QGP}} \gg \tau_{q,g}$  carry more information of their evolution
- $m_{c,b} \gg gT_{\text{RHIC,LHC}}$  soft scatterings  $\rightarrow$  Brownian motion (low p charm)

# Studying the HF dynamics in HIC

Bulk pre-equilibrium  
at  $\tau_0 \approx 1/2 m_{c,b} < 0.1 \text{ fm}/c$



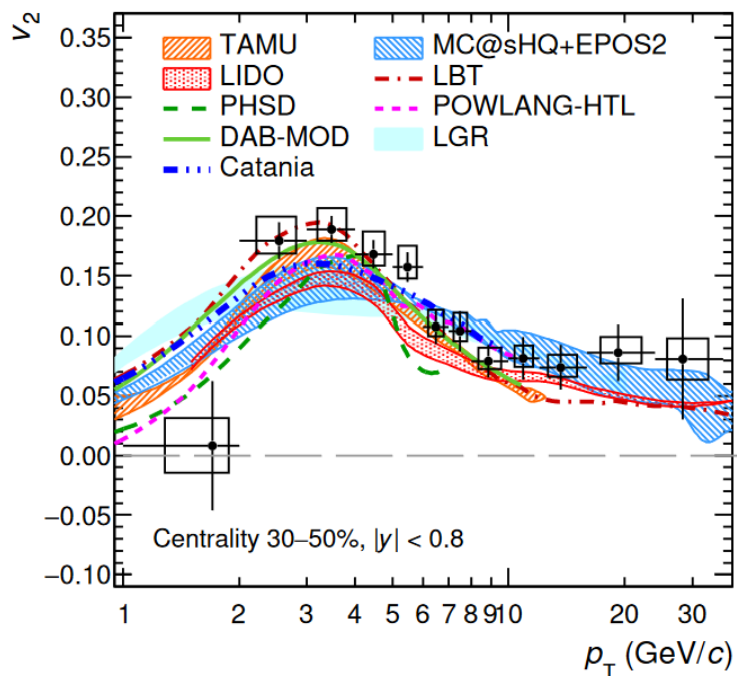
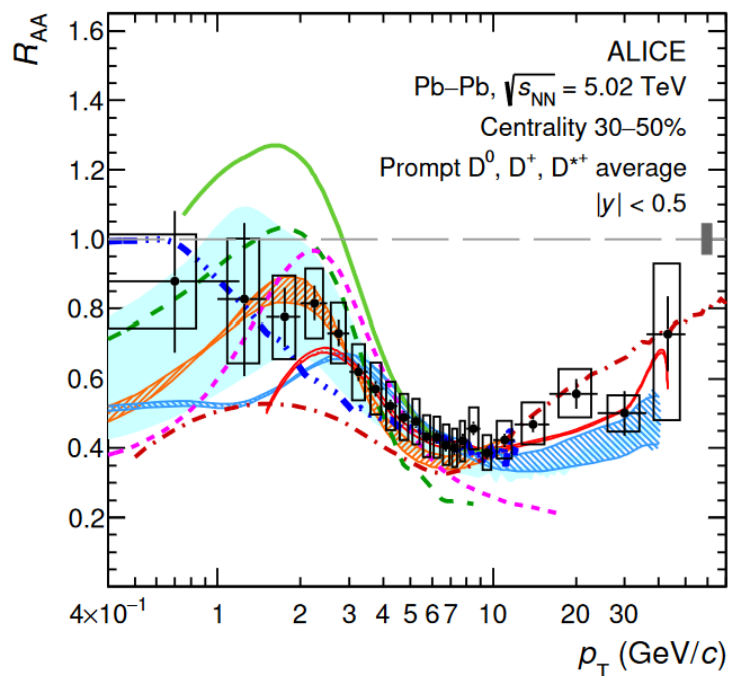
- Initial prod.  
pQCD-NLO  
Shadowing  
Pre-equilibrium  
Effect/Glasma  
Electromagnetic  
Filed/Vorticity

- Dynamics in QGP  
Heavy quark QGP interaction  
Transp. coeff. of QCD matter  
-> thermalization ?!  
Mass & color in Jet quenching  
Heavy quark momentum evol.  
(Langevin/Boltzmann/E. loss model)

- Hadronization:  
coalescence and/or  
fragmentation.  
Hadronic rescattering

# $R_{AA}$ and $v_2$

## Comparison with models

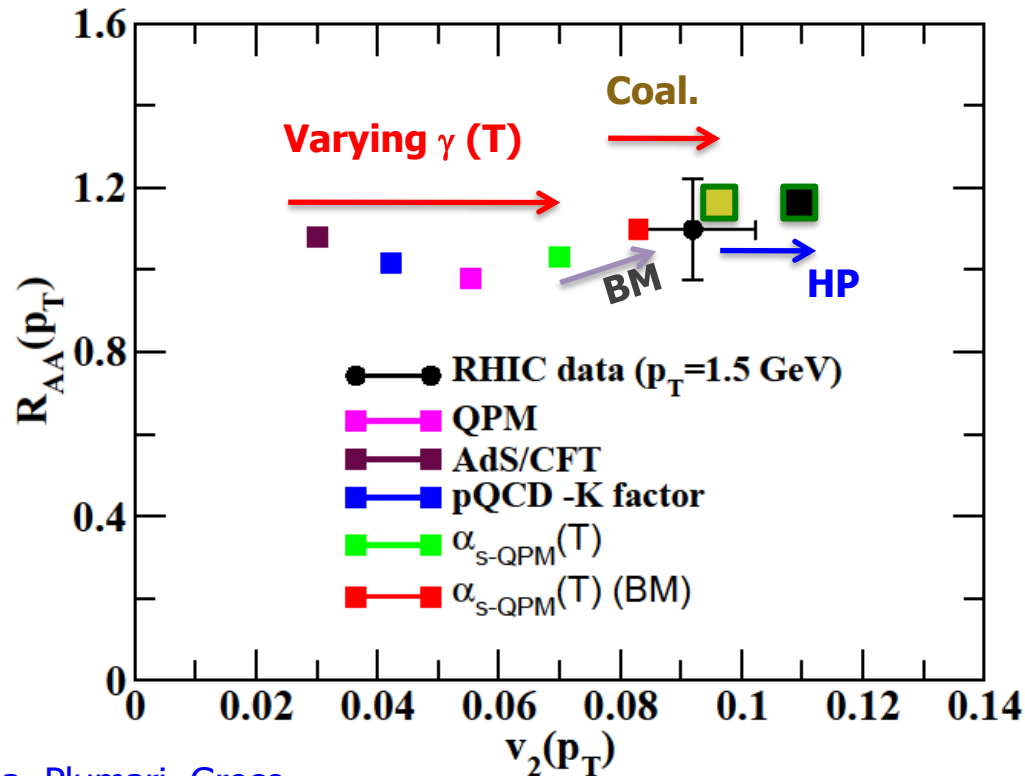


ALICE, JHEP 01 (2022) 174

**Most of the models able to describe both  $R_{AA}$  and  $v_2$  in certain  $p_T$  domain**

**Simultaneous description of  $R_{AA}$  and  $v_2$  is still a challenge in the whole measured  $p_T$  and centrality ranges, colliding energy, system size.**

# Summary on the build-up of $v_2$ at fixed $R_{AA}$

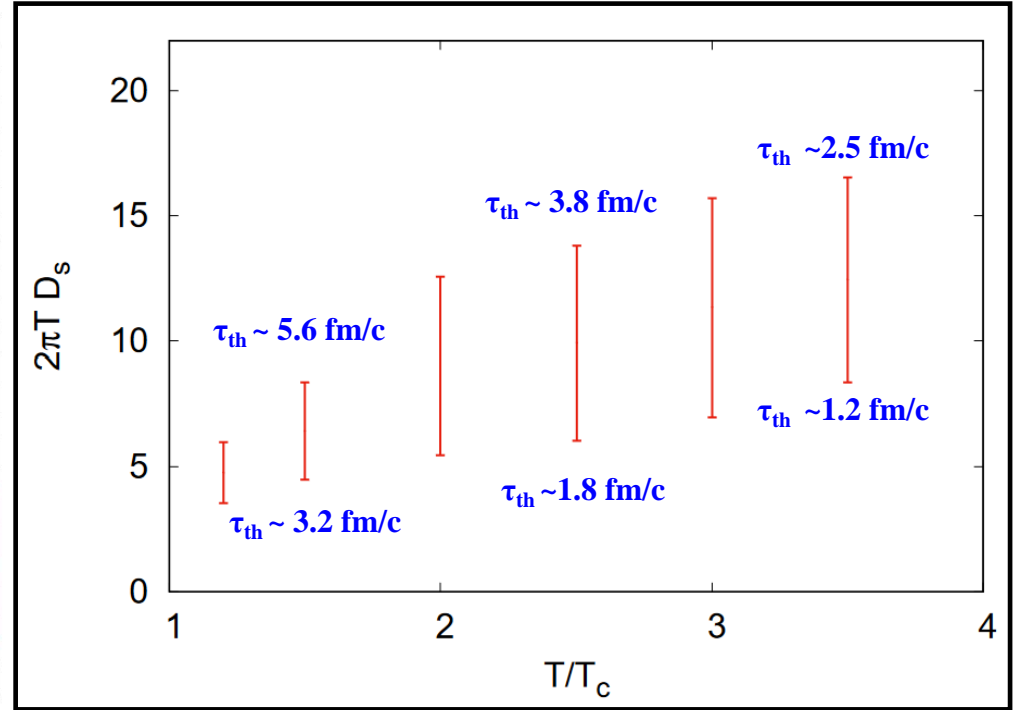
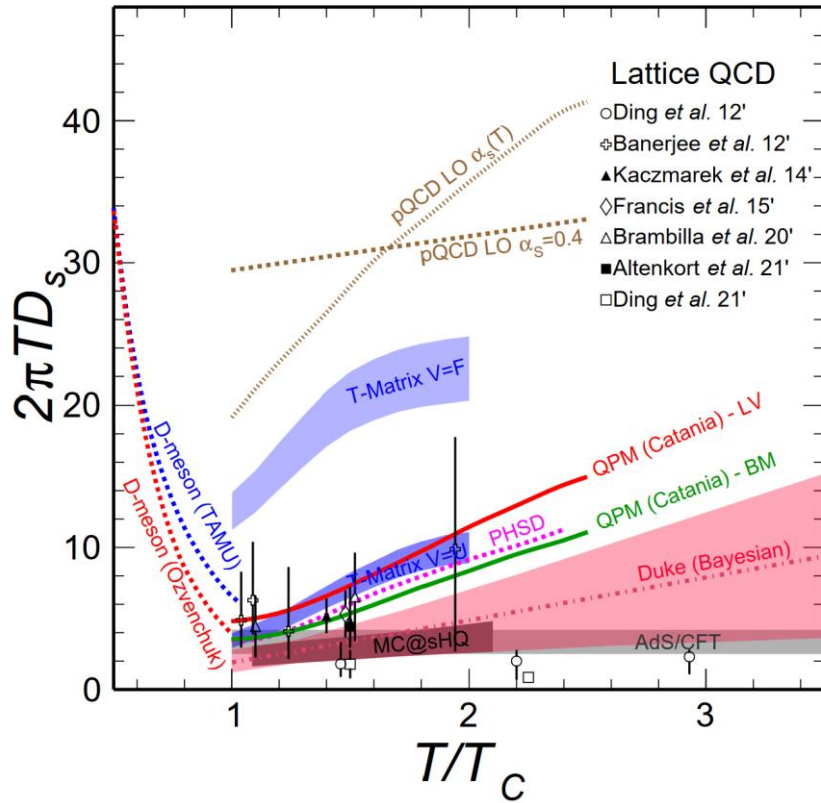


TAMU, Nantes, Catania, BAMPS,  
PHSD, Duke, POWLANG-HTL,  
UrQMD, Duke, LBL-CCNU, CUJET,  
DREENA,.....

Das, Scardina, Plumari, Greco  
Phys. Lett. B 747 (2016)260-264

$R_{AA}$  and  $V_2$  are correlated but still one can have  
 $R_{AA}$  about the same while  $v_2$  can change up to a factor 2-3  
 $\gamma(T)$  + Boltzmann dynamics+ hadronization+ hadronic phase

# Heavy quark diffusion



$$D_s = T/M * \gamma(p \rightarrow 0)$$

He, Fries, Rapp, PRL,110, 112301 (2013)

Banerjee, Datta, Gavai, Majumdar  
arxiv: 2206.15471 [hep-ph]

$$\tau_{th} = \frac{M}{2\pi T^2} (2\pi T D_s) \cong 1.8 \frac{2\pi T D_s}{(T/T_c)^2} \text{ fm/c}$$

Scardina, Das, Minissale, Plumari, Greco  
PRC,96, 044905 (2017)

$2\pi T D_s \propto T^2$ , corresponds to a constant thermalization time.

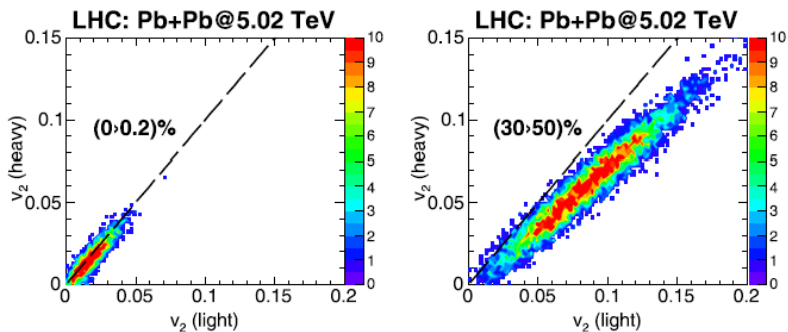
**Memory effect can impact the HQ thermalization**

Ruggieri, Pooja, Jai Prakash, Das, PRD, 106 (2022)

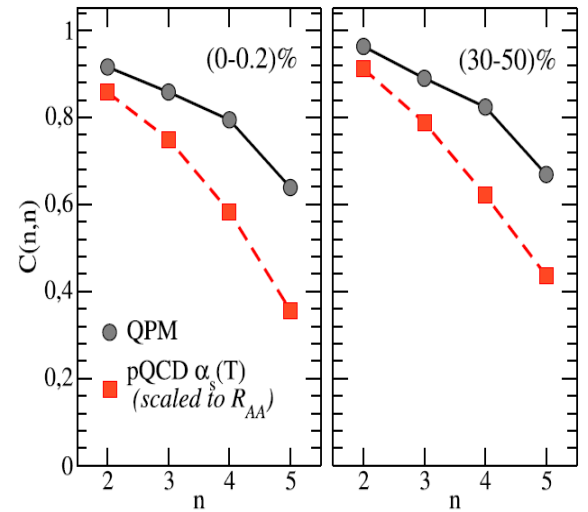
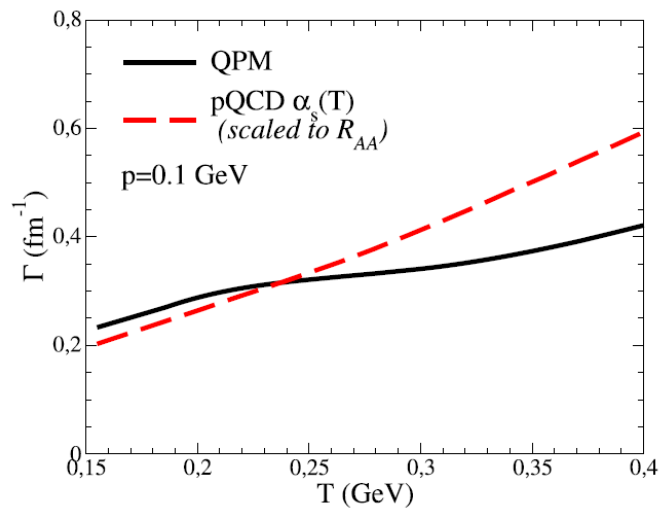
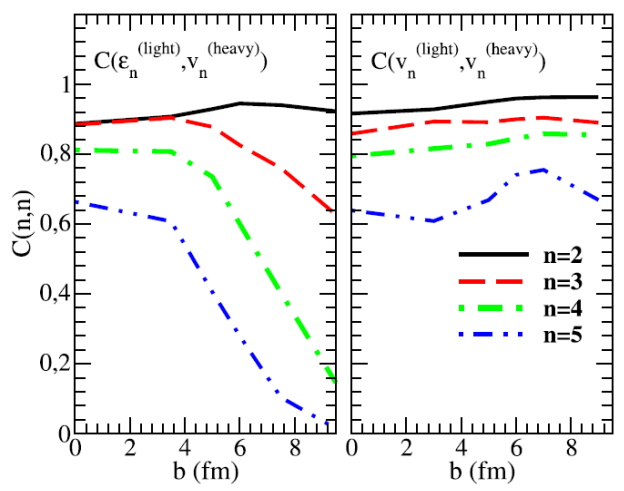
# Recent Developments



# Heavy-light event-by-event correlation



$$C(n, m) = \frac{\sum_i (v_n^{L,i} - \langle v_n^L \rangle)(v_m^{H,i} - \langle v_m^H \rangle)}{\sqrt{\sum_i (v_n^{L,i} - \langle v_n^L \rangle)^2 \sum_i (v_m^{H,i} - \langle v_m^H \rangle)^2}}$$



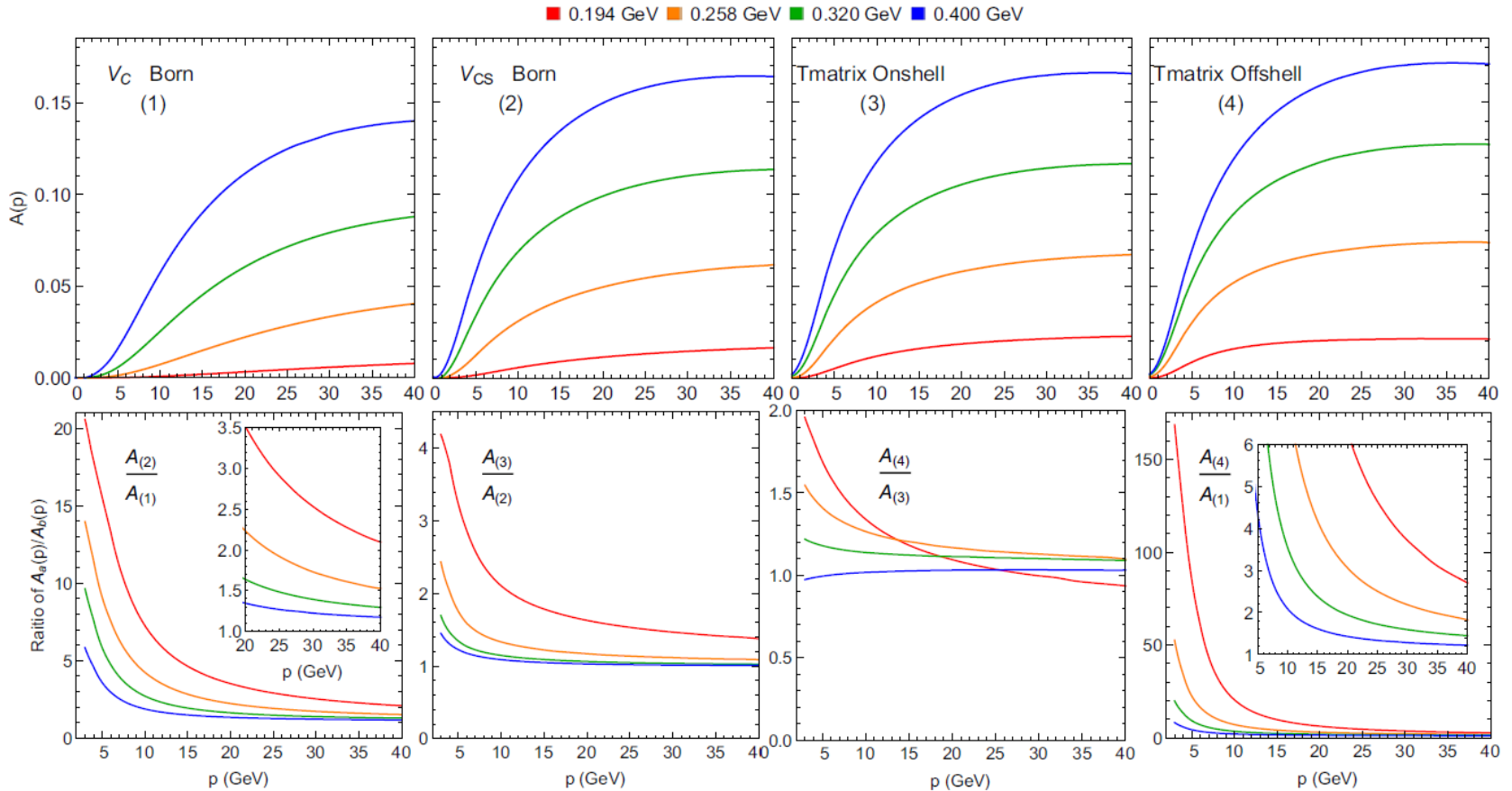
$V_n(D)$  more correlated to  $v_n(N_{ch})$  than  $\epsilon_n$

Very large sensitivity to T dep. of Ds

This can put further constrain on heavy quark transport coefficients

Plumari, Coci, Minissale, Das, Sun, Greco  
PLB 805 (2020) 135460

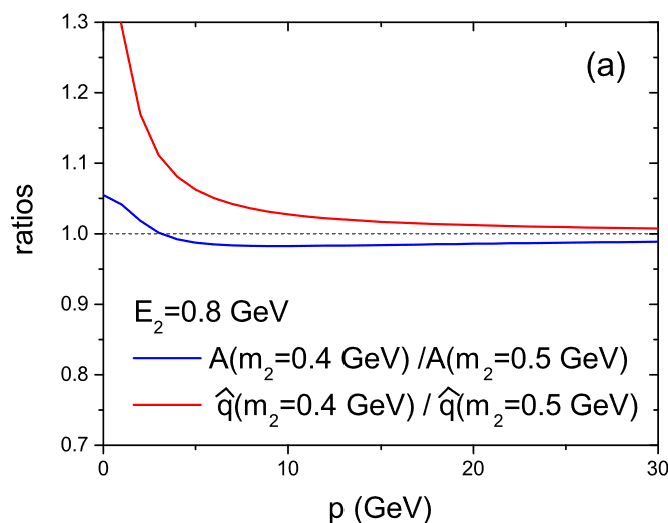
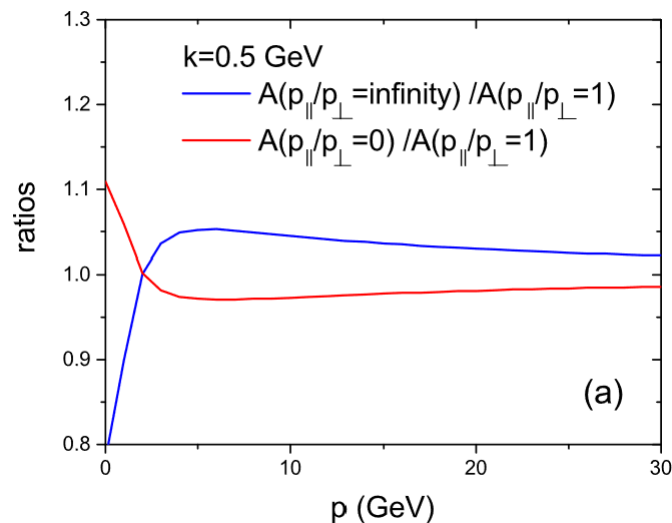
# Heavy quark radiation in T-matrix approach



Liu, Rapp, JHEP 08 (2020) 168

- ❖ Perturbative processes experience a strong suppression due to thermal mass
- ❖ Nonperturbative effect enhance the radiative contribution at low  $p$  and  $T$ .
- ❖ But its magnitude is small compared to the elastic contribution.

## Heavy quark transport coefficients: Non-equilibrium effect



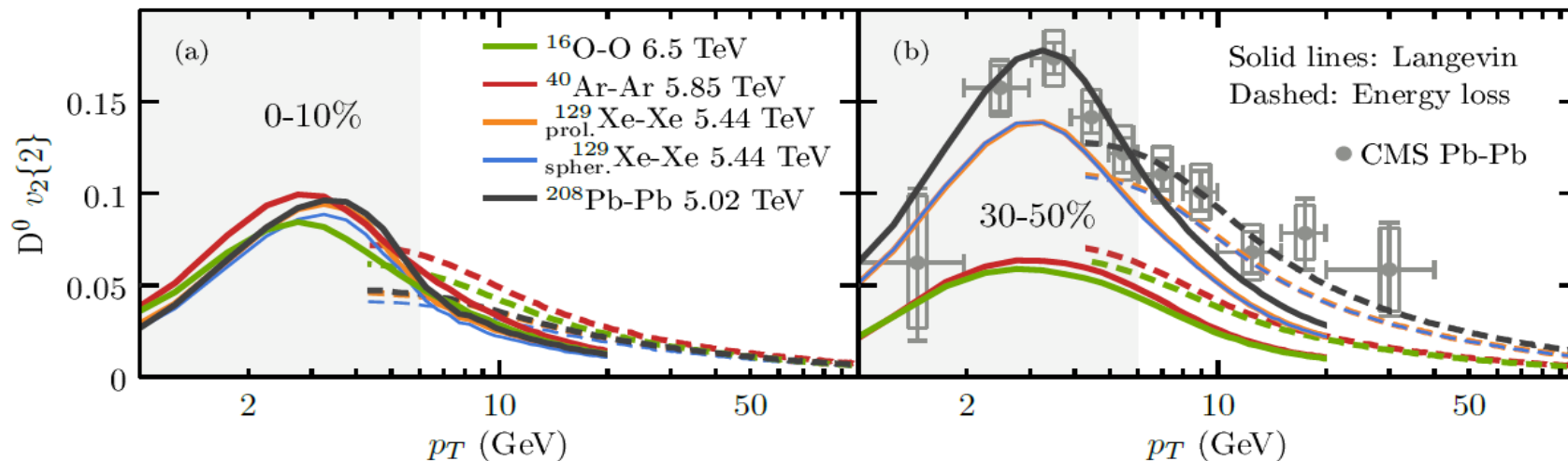
Anisotropic bulk distribution

Shift in poll mass

Each non-equilibrium scenario affects  $A$  of charm quarks in a different way.

Song, Moreau, Aichelin, Bratkovskaya, PRC, 101 (2020)

## System size scan of D meson $R_{AA}$ and $v_2$

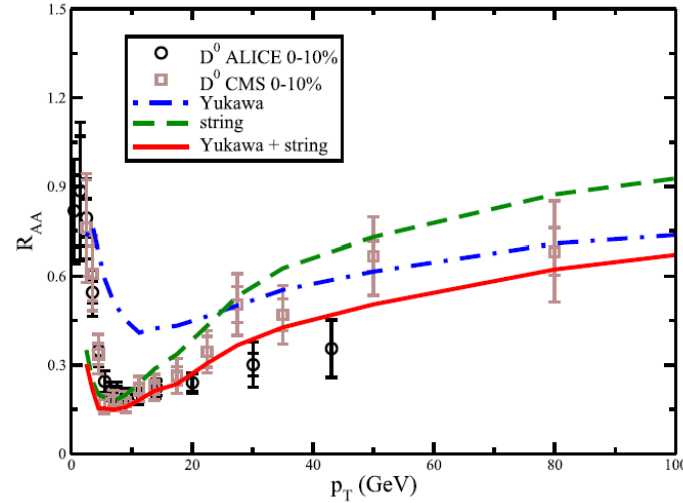
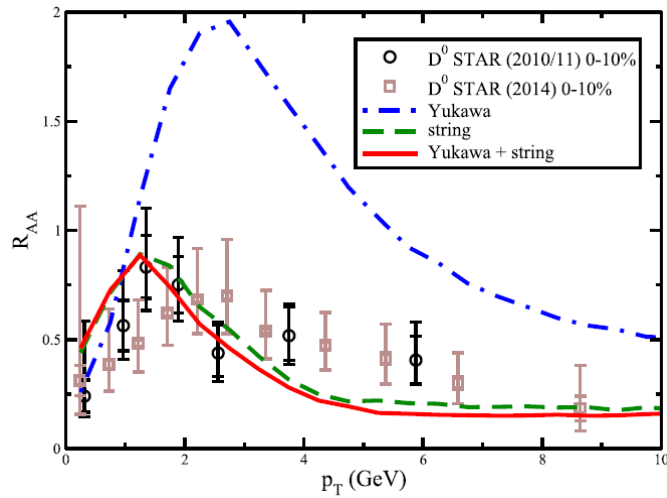


In central collisions the  $v_2$  is independent of system size.

System size vs Eccentricity

R. Katz et. al, PRC,102 (2021)

# In-medium heavy quark potential from the open heavy flavor observables

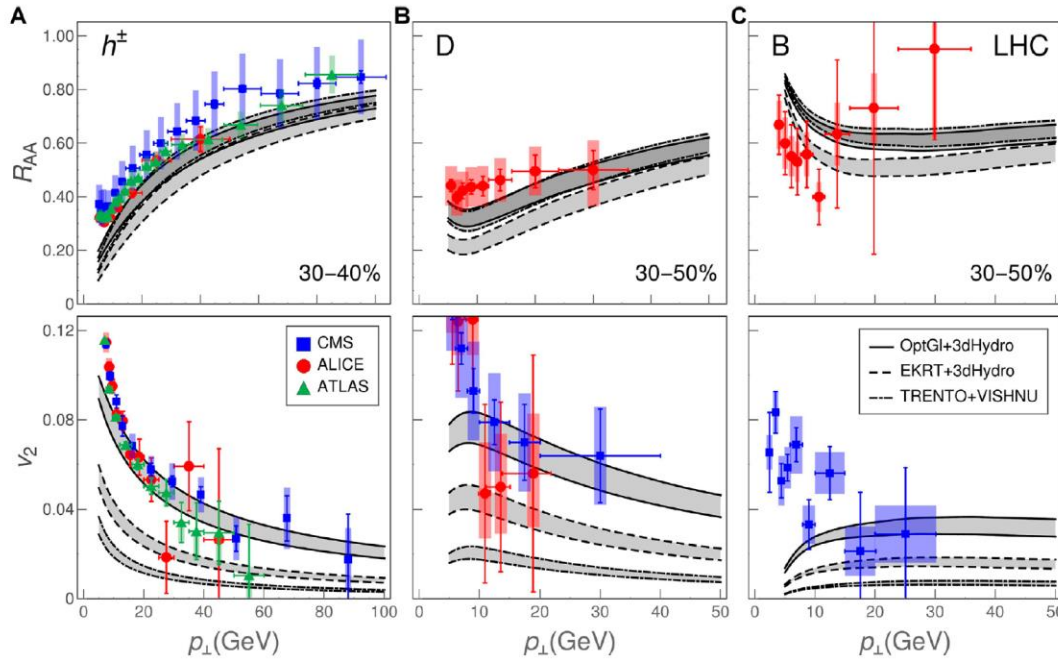


Xing, Qin, Cao  
PLB 838 (2023) 137733

❖ Xing's Talk (Wed)

High  $p_T$  are dominated by the short-range Yukawa potential.  
Low  $p_T$  are dominated by the long-range string potential

## Dynamical Radiative and Elastic Energy loss Approach-A



Exploit differences in temperature profiles

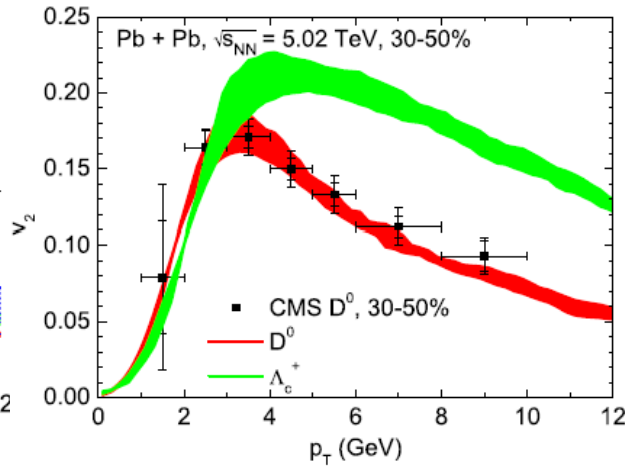
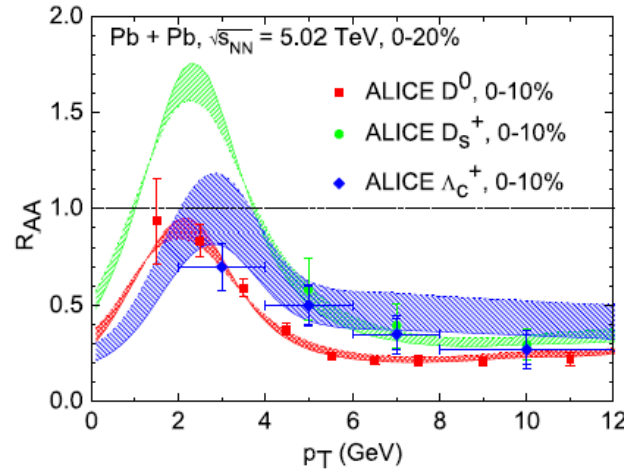
Can describe the data at high  $p_T$

❖ Djordjevic's Talk (Tus)

Zigic, Salom, Auvinen, Huovinen, Djordjevic  
FIP 10(2022) 957019

# Heavy quark hadronization

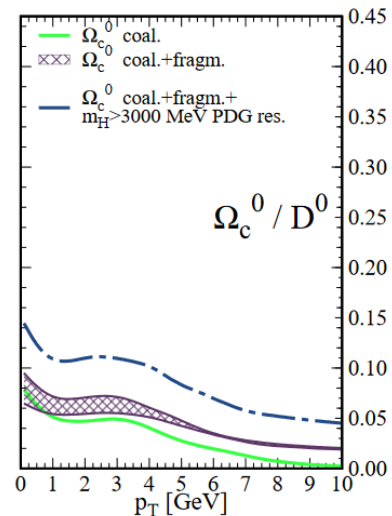
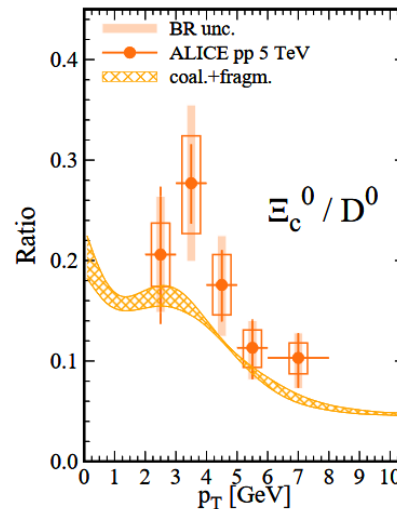
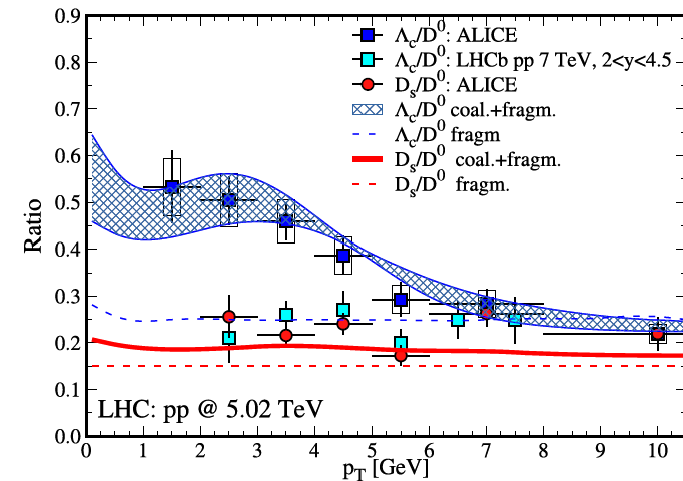
❖ Beraudo's Talk (Wed)



- 4-momentum conserving three-body recombination
- Equilibrium limit
- Improved HF hadrochemistry

He, Rapp, PRL 124 (2020) 042301

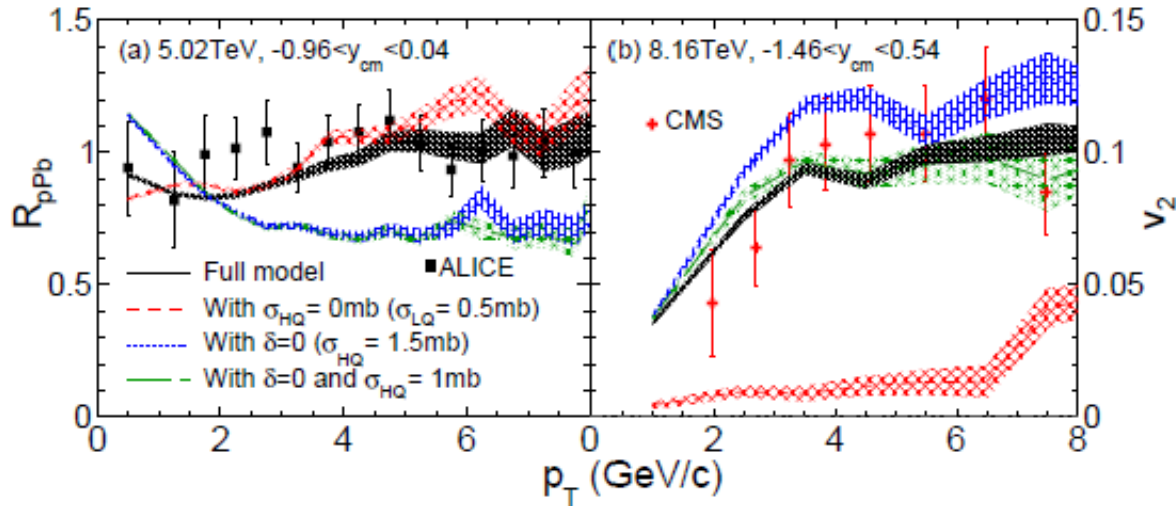
# Charm hadrons coalescence plus fragmentation in pp



$$P_{fragm} = 1 - P_{coal}. \quad \lim_{p \rightarrow 0} P_{coal}^{tot} = 1.$$

Minissale, Plumari, Greco, PLB 821(2021) 136622

# $R_{pA}$ and $v_2$ puzzle of D mesons in p-Pb collisions



**$v_2$ : charm quark interaction**  
 **$R_{pPb}$ : Cronin effect**

**No radiation**  
**No T and p-dependence interaction**

Cronin effect enhances the charm quark yield at relatively high  $p_T$  and cancels out the effect from jet quenching.

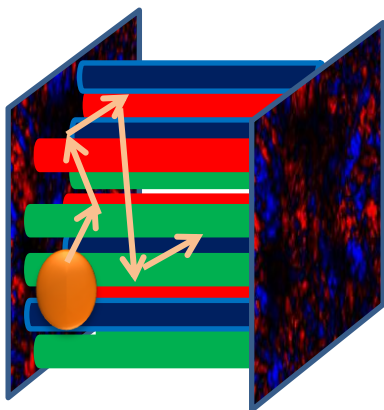
❖ **Lin's Talk (Wed)**

Zhang, Zheng, Shi, Lin, arXiv: 2210.07767[nucl-th]

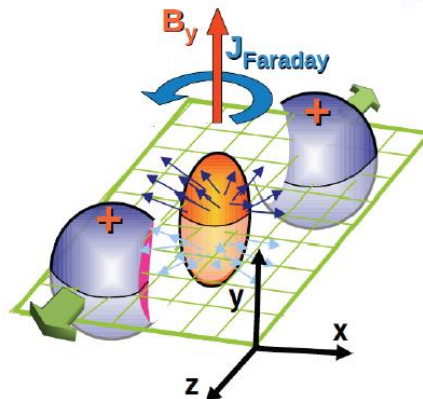
**Heavy quark as a probe of Initial stage**

# Heavy quark as a probe of Initial stage

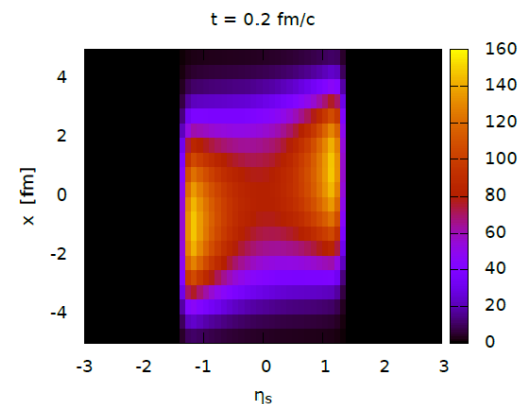
(Adapted from M. Ruggieri)



Impact of Glasma phase



Electromagnetic field



Vorticity

## Initial Glasma in Pre-equilibrium phase can induce strong diffusion

Mrowczynski, EPJA 54 (2018)

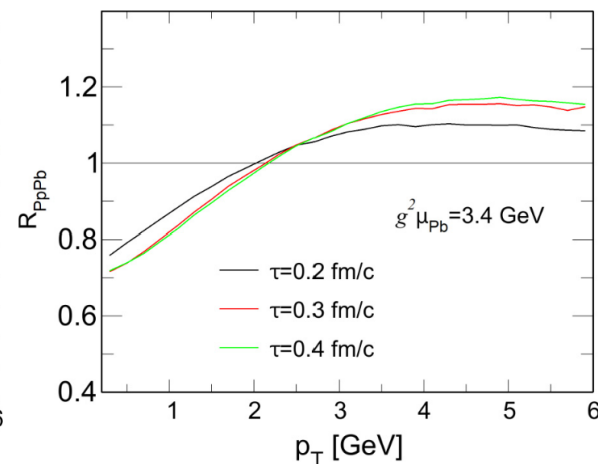
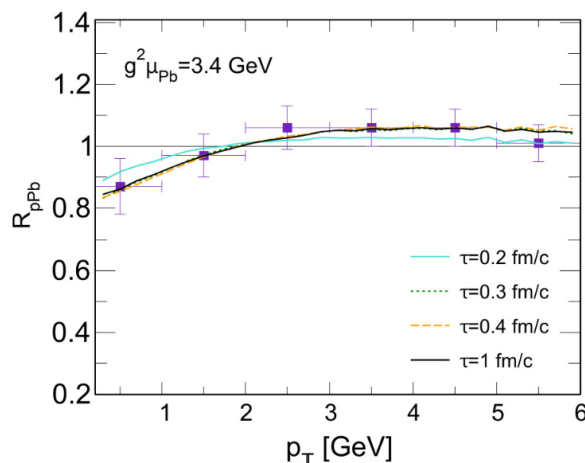
Ruggieri and Das, PRD98 (2018)

$$\frac{dx_i}{dt} = \frac{p_i}{E},$$

$$E \frac{dp_i}{dt} = gQ_a F_{i\nu}^a p^\nu,$$

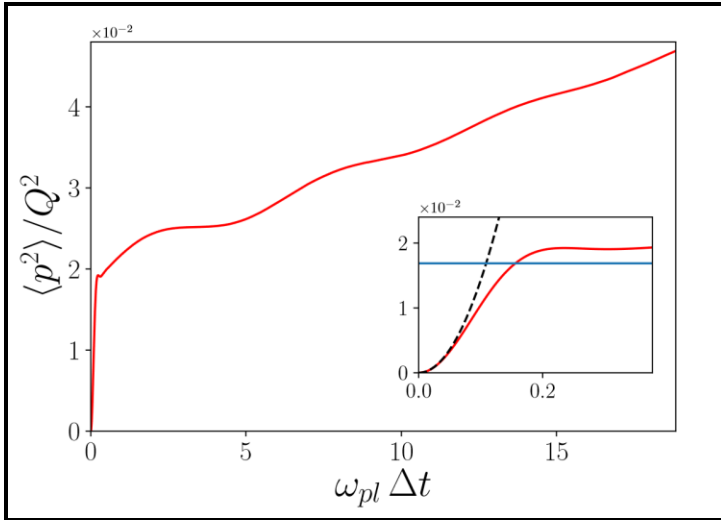
$$E \frac{dQ_a}{dt} = -gQ_c \varepsilon^{cba} \mathbf{A}_b \cdot \mathbf{p};$$

Wong (1979)



Liu, Plumari, Das, Greco, Ruggieri, PRC, 102 (2020)





## Correlator method

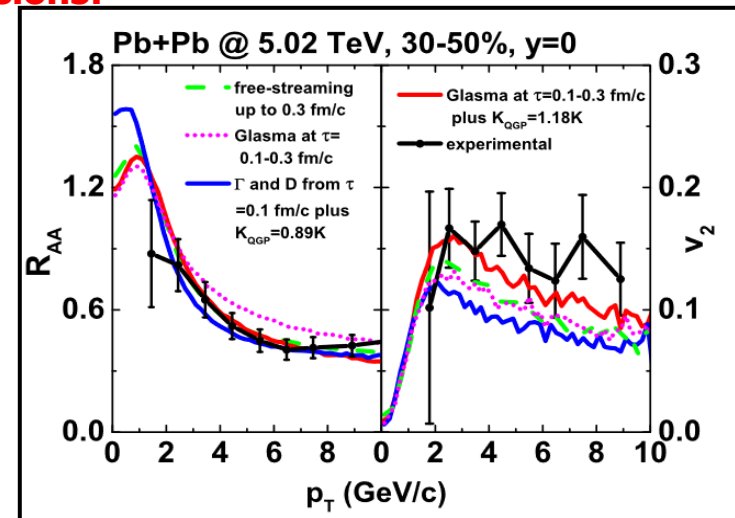
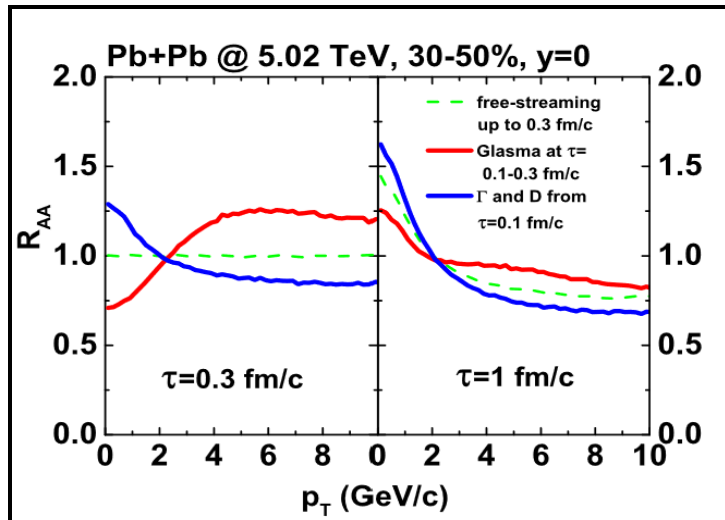
$$\langle \dot{p}_i(t) \dot{p}_i(t') \rangle = \frac{g^2}{2N_c} \langle E_i^a(t) E_i^a(t') \rangle$$

Strong heavy quark diffusion in Glasma:

- ❖ Can affect the D-Dbar correlation
- ❖ Strong diffusion enhance the  $R_{AA}$  in AA
- ❖ Leads to large  $v_2$  to have the same  $R_{AA}$

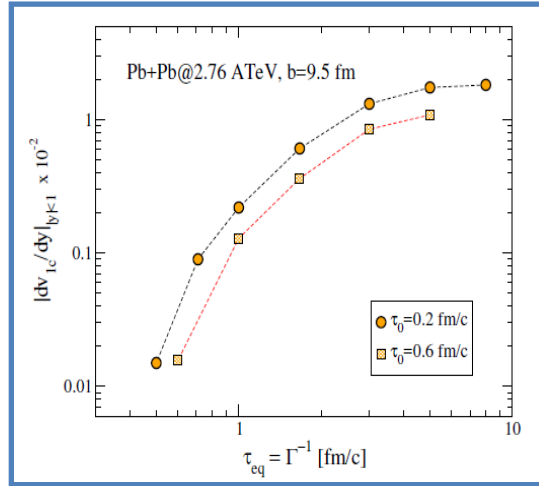
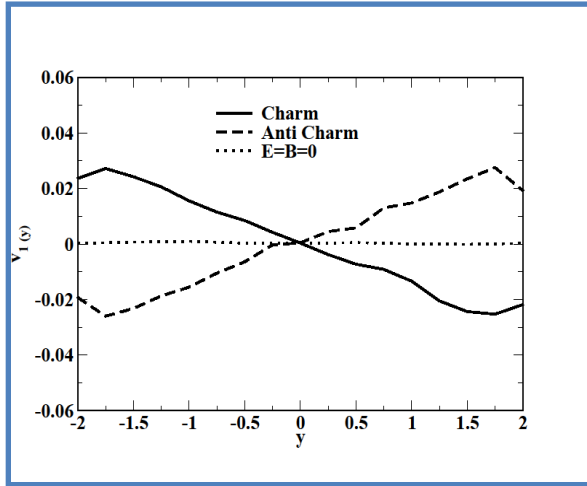
Boguslavski, Kurkela, Lappi and J. Peuron, JHEP (2020)

## Impact of Glasma phase on nucleus-nucleus collisions:



Sun, Coci, Das, Plumari, Ruggieri, Greco  
PLB, 798 (2019) 134933

# Heavy quark directed flow in EM fields



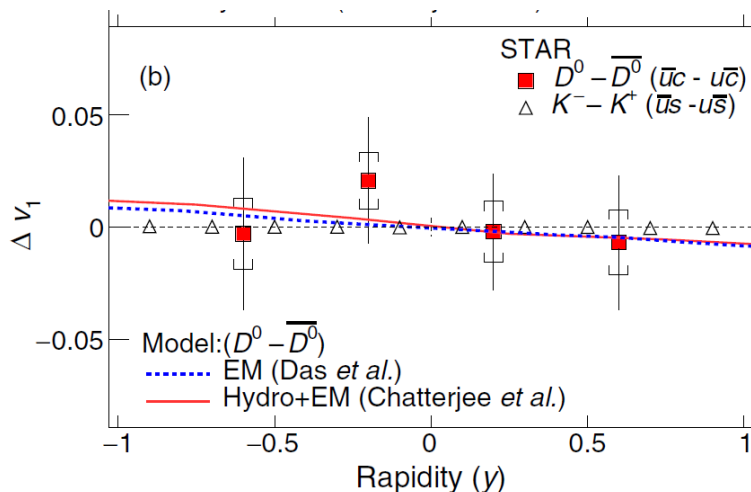
❖ Order of magnitude larger than light hadron  $v_1$

❖ Opposite  $v_1$  for charm and anti-charm

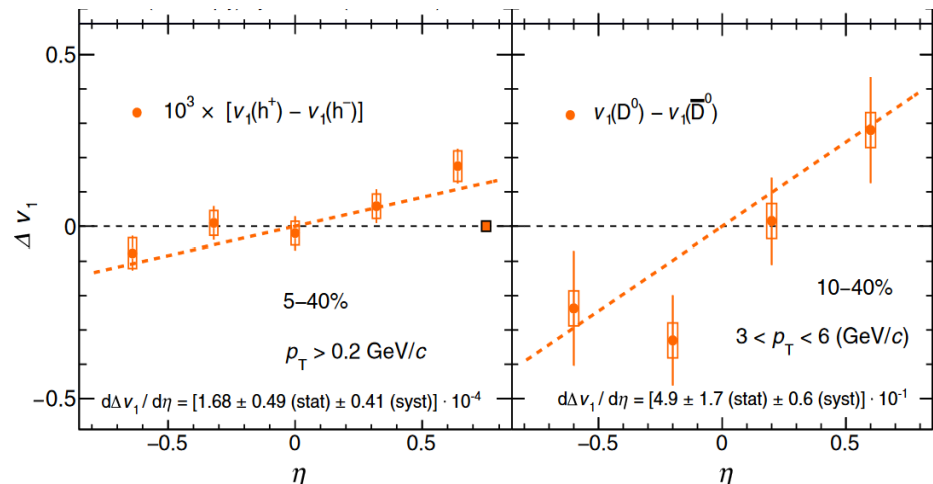
Das, Plumari, Chatterjee, Scardina, Greco, Alam  
Phys. Lett. B, 768 (2017) 260

$$\Delta v_1(D) = v_1(D^0) - v_1(\bar{D}^0)$$

## Heavy meson directed flow at RHIC & LHC:

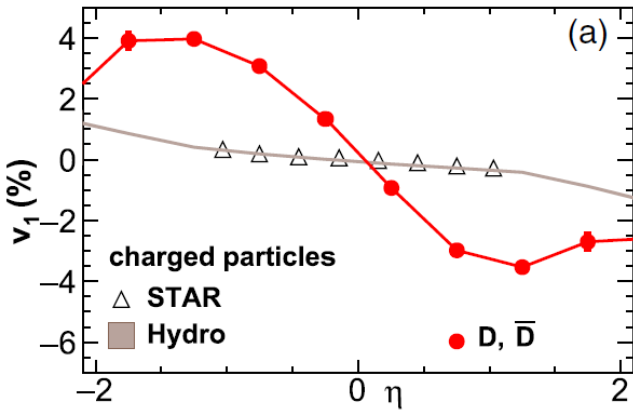


STAR Collaboration PRL 123, 162301 (2019)

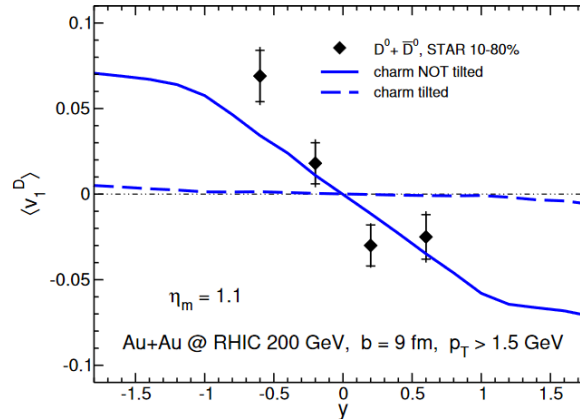


ALICE Collaboration PRL 125, 022301 (2020)

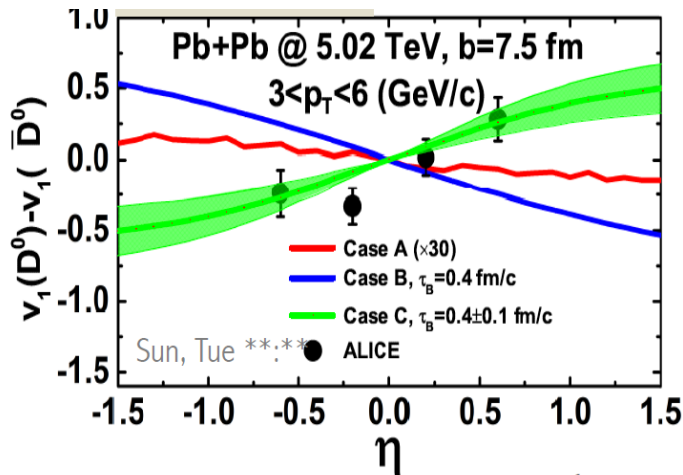
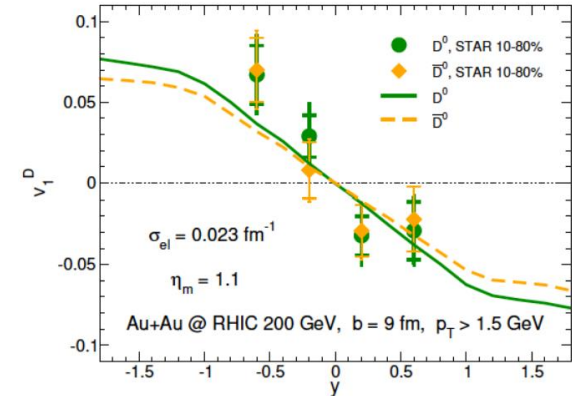
# Heavy quark as a probe of initial stage: vorticity



Chatterjee and Bozer, PRL, 120 (2018)



Oliva, Plumari, Greco, JHEP (2021)



$$B(\tau) = eB_0 / (1 + \tau^2 / \tau_B^2)$$

$\tau < 1$  fm/c  
 $B(\tau) \approx B(\tau)$

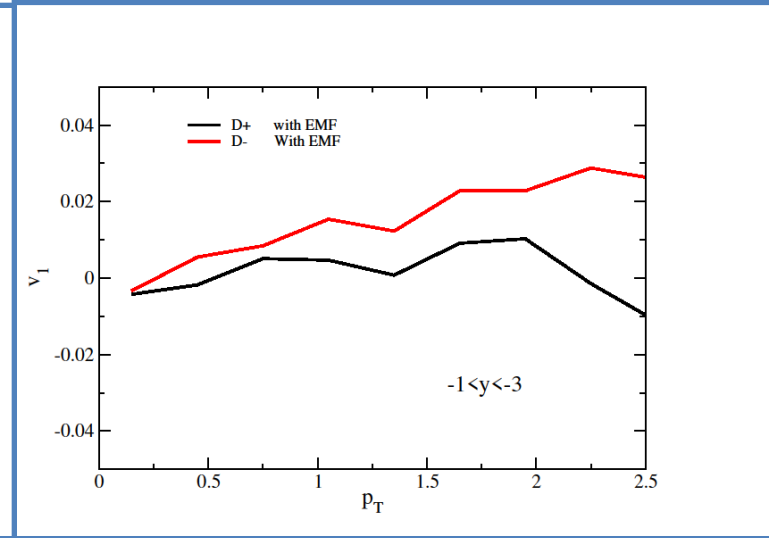
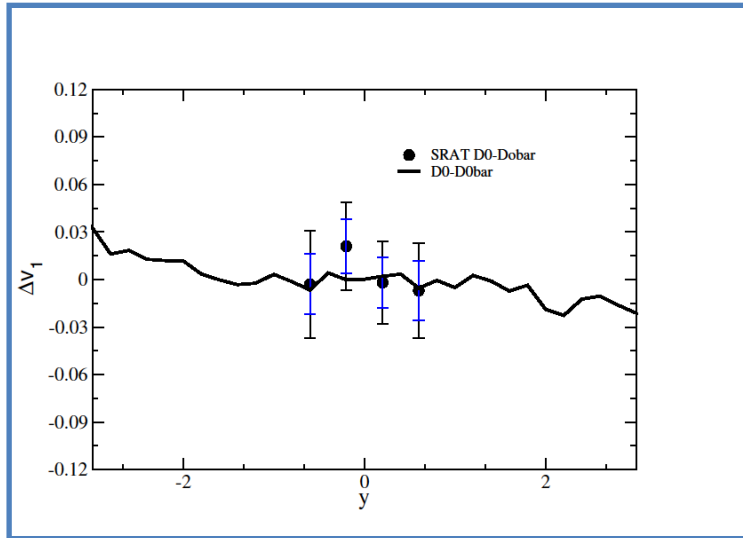
$$B(\tau) = eB_0 / (1 + \tau / \tau_B)$$

$E_x(\tau) > E_x(\tau)$

- ❖ Large directed flow of heavy meson than the light hadron
- ❖ Charm quarks distribution are not tilted
- ❖ Yet to understand the  $\Delta v_1$  sign change from RHIC to LHC
- ❖ Computation of early stage EM field is very essential

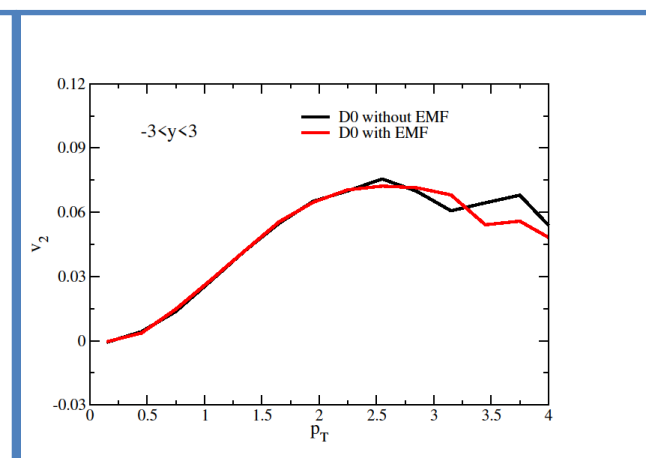
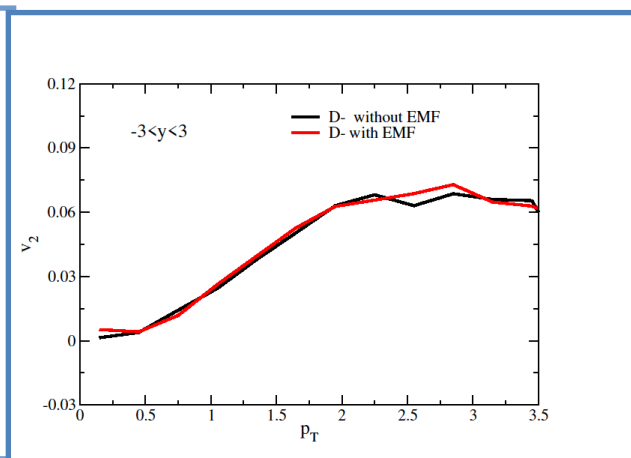
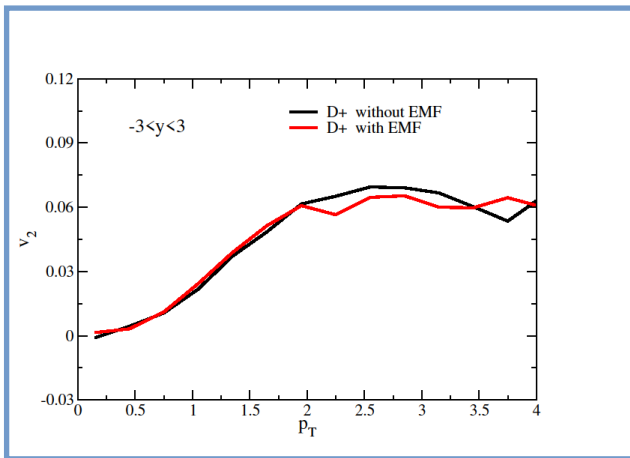
Sun, Plumari, Greco, PLB, 861 (2021)

# Heavy quark directed flow within PHSD @ RHIC



The splitting is larger as a function of momentum

Das, Soloveva, Song, Bratkovskaya  
Under preparation



Impact of electromagnetic field on heavy quark elliptic flow is negligible

# Conclusions and Perspectives:

- ❖ Present calculations indicate  $\tau_{\text{th}} \sim 2\text{-}6 \text{ fm}/c$  for low  $p_{\text{T}}$  charm quark.
- ❖ More precision data and additional observables can further constrain the  $D_s$   
Heavy-light event-by-event correlation, System size scan, D-Dbar correlation,  
B meson,  $\Lambda_c$ ,  $p \rightarrow 0$ ,...
- ❖ Time evolution of EM field in HIC  $\rightarrow$  opposite sign of HF  $v_1$  from RHIC to LHC
- ❖ Heavy quark can act as an excellent probe of the early stage dynamics  
Pre-equilibrium phase, EM fields, Vorticity
- ❖ Time to focus heavy quark dynamics in small system, Beam energy scan....  
So far major focus: Highest RHIC energy and LHC energies  
Recent STAR data on HF decay electron@ 54.4 GeV and 27 GeV...

*Thank You*



A stylized illustration of a tropical island with two palm trees, a small white circle representing the sun or moon, and a body of water with ripples in the foreground.

**4th Heavy  
Flavour  
Meet**

**IIT Goa, 2-4 Nov 2023**

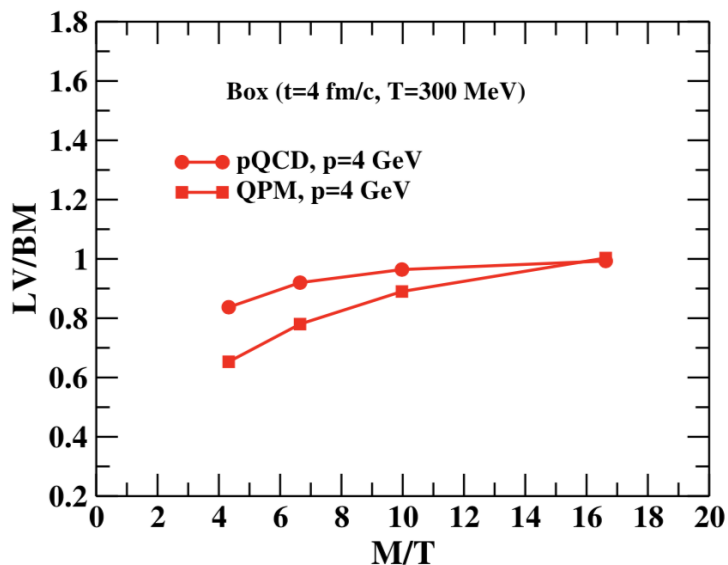
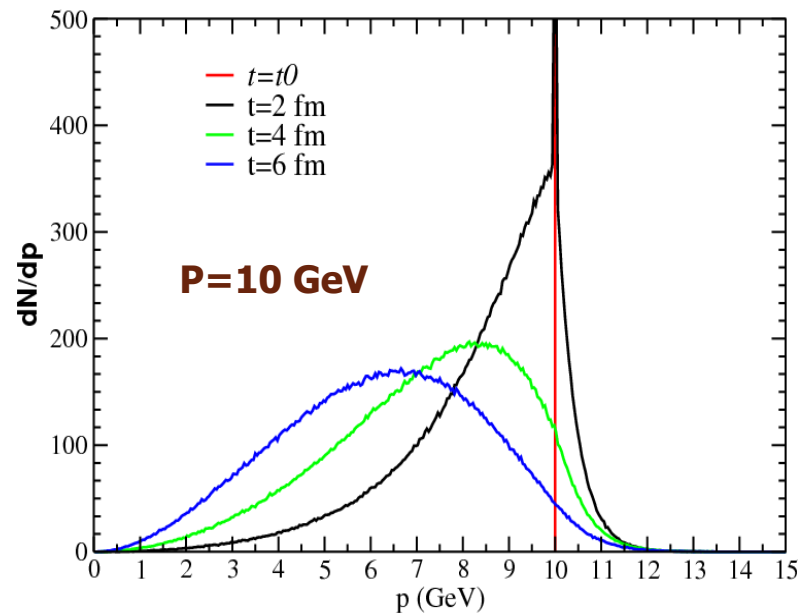
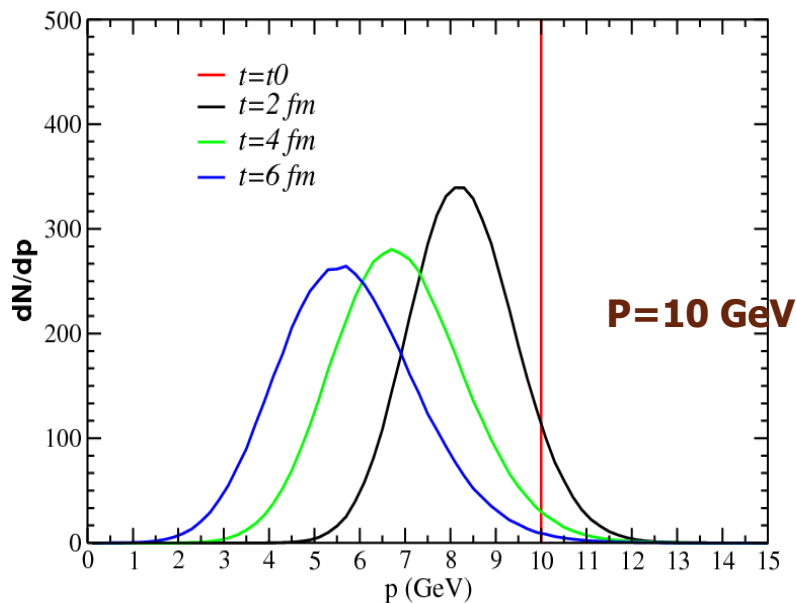


# Momentum evolution starting from a $\delta$ (Bottom)

Langevin

In a Box

Boltzmann



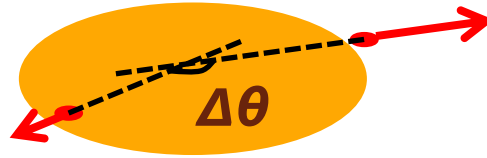
Das, Scardina, Plumari and Greco  
 PRC,90,044901(2014)

Langevin dynamics overestimate the interaction  
 Boltzmann generate more  $v_2$  for the same RAA.

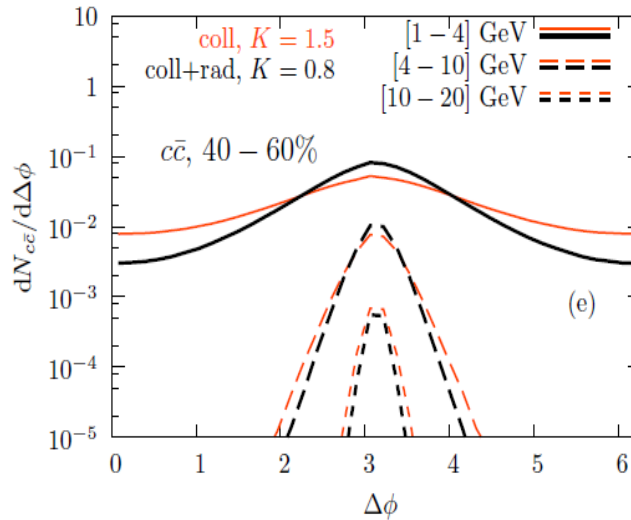
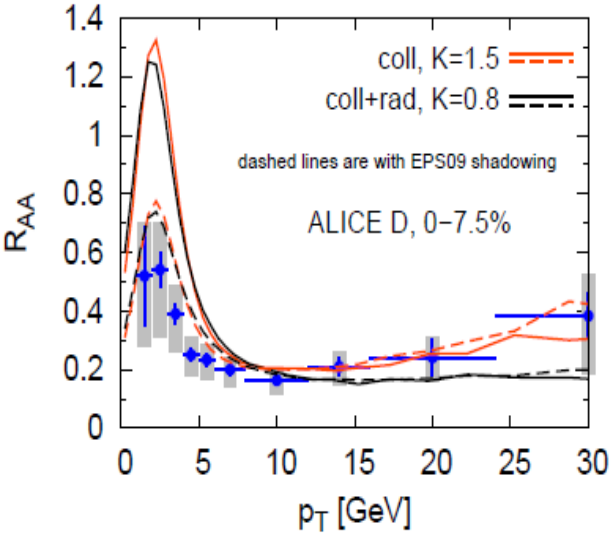
Rapp et. al. EMMI-RRTE, NPA 979 (2018)



# Angular De-correlation of $c\bar{c}$ :

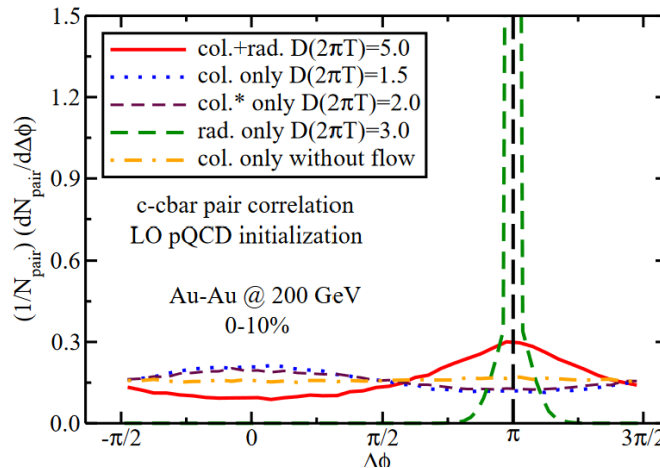
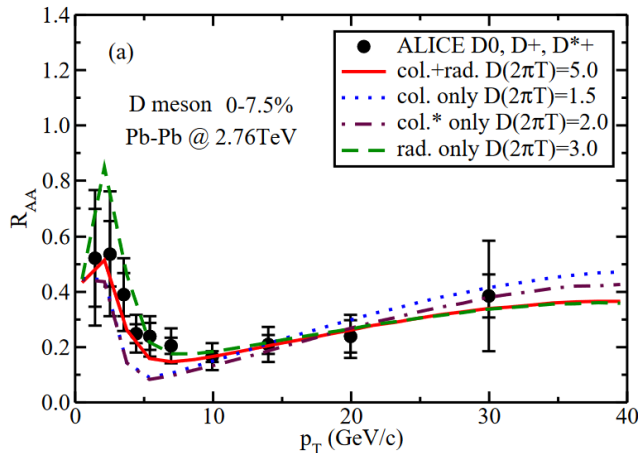


Zhu ,Xu, Zhuang, PRL100, 152301 (2008)



**DDbar correlation is sensitive to energy loss mechanism**

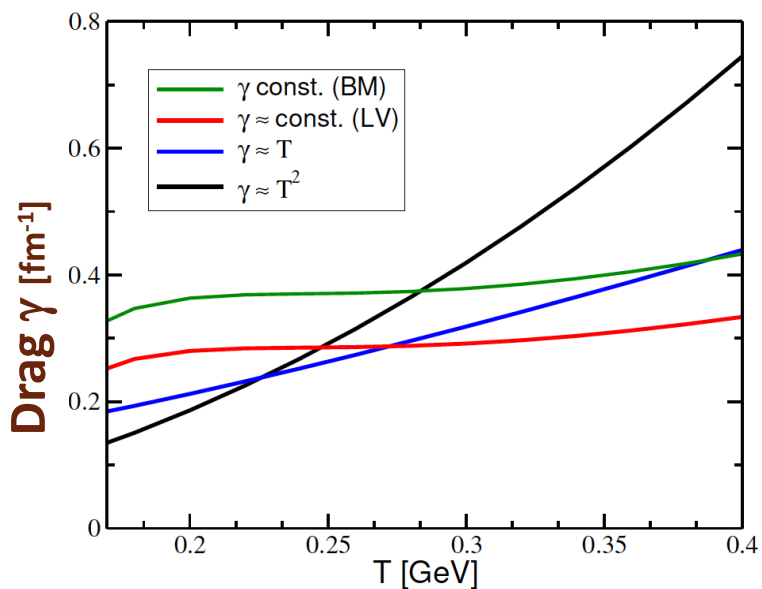
Nahrgang, Aichelin, Gossiaux, Werner  
PRC,90, 024907 (2014)



**DDbar correlation can disentangle different Energy loss mechanism**

Cao, Qin, Bass  
PRC, 95 (2015)

# Impact of T dep. interaction on $R_{AA} - v_2$



Looking at it beyond the specific modelings

➤  $\gamma \approx T^2$  [Ads/CFT, pQCD  $\alpha_s = \text{const}$ ]

➤  $\gamma \approx T$  [pQCD strong  $\alpha_s$  running]

➤  $\gamma \approx \text{const.}$  [QPM, PHSD, T-matrix]

$\gamma$  rescaled to fit  $R_{AA}(p_T)$ , D from FDT

$$\frac{d\mathbf{p}}{dt} = -\gamma\mathbf{p} + \eta(t)$$

