

# Determination of quark and gluon distributions in nuclei using correlated nucleon pairs

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Institute of Nuclear Physics PAN, Krakow, Poland

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nCTEQ presentations

- ▶ T. Jezo (Thur 12:00)
- ▶ N. Derakhshanian (poster)



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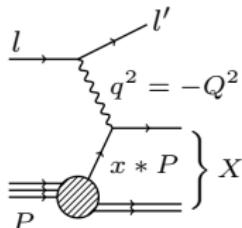
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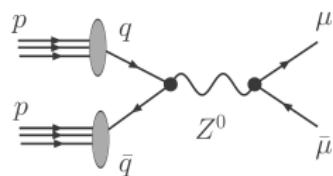
# PDFs and QCD Factorization

- **Factorization** in case of **Deep Inelastic Scattering** (DIS)



$$\frac{d^2\sigma}{dx dQ^2} = \sum_{i=q,\bar{q},g} \int_x^1 \frac{dz}{z} f_i(z, \mu) d\hat{\sigma}_{il \rightarrow l' X} \left( \frac{x}{z}, \frac{Q}{\mu} \right) + \mathcal{O}\left(\frac{\Lambda_{\text{QCD}}^2}{Q^2}\right)$$

- **Factorization** in case of **Drell-Yan lepton pair production** (DY)



$$\begin{aligned} \sigma_{pp \rightarrow l\bar{l} X} = & \sum_{i,j=q,\bar{q},g} \int_{x_1}^1 dz_1 \int_{x_2}^1 dz_2 \\ & \times f_i(z_1, \mu) f_j(z_2, \mu) \hat{\sigma}_{ij \rightarrow l\bar{l} X} \left( \frac{x_1}{z_1}, \frac{x_2}{z_2}, \frac{Q}{\mu} \right) + \mathcal{O}\left(\frac{\Lambda_{\text{QCD}}^2}{Q^2}\right) \end{aligned}$$

- $f_i(z, \mu)$  – proton PDFs of parton  $i$  (**non-perturbative**).

PDFs are **UNIVERSAL** – do not depend on the process!!!

- $\hat{\sigma}$  – parton level matrix element (**calculable in pQCD**).

- $\mathcal{O}\left(\frac{\Lambda_{\text{QCD}}^2}{Q^2}\right)$  – non-leading terms defining accuracy of factorization formula.

# Properties of PDFs

## ► Sum rules

- ▶ **Number sum rules** – connect partons to quarks from SU(3) flavour symmetry of hadrons; proton ( $uud$ ), neutron ( $udd$ ). For protons:

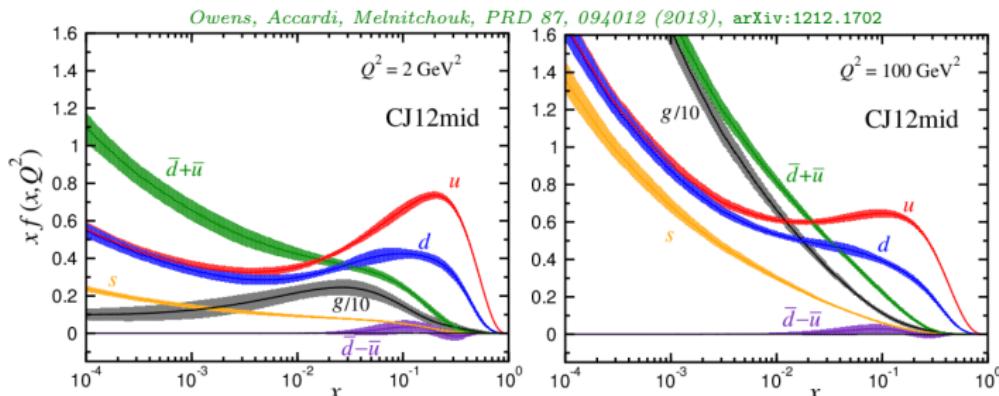
$$\int_0^1 dx \underbrace{[f_u(x) - f_{\bar{u}}(x)]}_{u-\text{valence distr.}} = 2 \quad \int_0^1 dx \underbrace{[f_d(x) - f_{\bar{d}}(x)]}_{d-\text{valence distr.}} = 1$$

- ▶ **Momentum sum rule** – momentum conservation connecting all flavours

$$\sum_{i=q,\bar{q},g} \int_0^1 dx x f_i(x) = 1$$

## ► Scale dependence

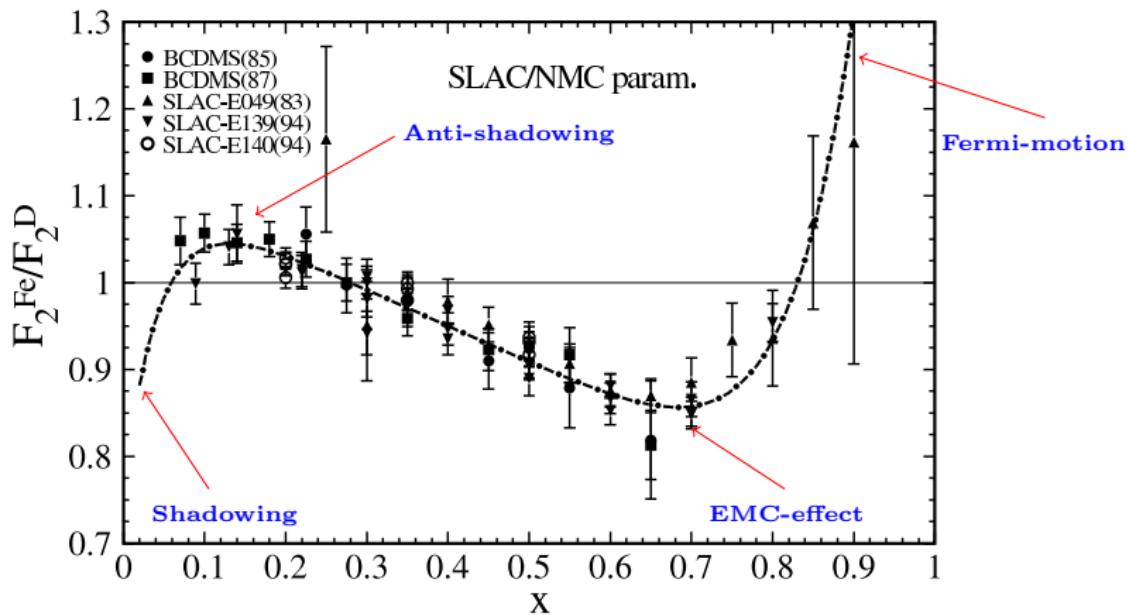
- ▶  **$x$ -dependence** of PDFs is NOT calculable in pQCD
- ▶  **$\mu^2$ -dependence** is calculable in pQCD – given by **DGLAP** equations



# Nuclear collision → nuclear PDFs

- Cross-sections in nuclear collisions are modified

$$F_2^A(x) \neq Z F_2^p(x) + N F_2^n(x)$$



- Can we translate these modifications into **universal nuclear PDFs**?

$$\frac{d^2\sigma}{dx dQ^2} = \sum_{i=q,\bar{q},g} \int_x^1 \frac{dz}{z} f_i^A(z, \mu) d\hat{\sigma}_{il \rightarrow l' X} \left( \frac{x}{z}, \frac{Q}{\mu} \right) + \mathcal{O}\left(\frac{\Lambda_{\text{QCD}}^2}{Q^2}\right)$$

# Schematics of Global Analysis

1. Choose experimental data (e.g. DIS, DY, inclusive jet prod., etc.)
2. Parametrize **nuclear PDFs** at low initial scale  $\mu = Q_0 = 1.3\text{GeV}$ :

$$f_i^{(A,Z)} = \frac{Z}{A} f_i^{p/A} + \frac{A-Z}{A} f_i^{n/A}$$
$$f_i^{p/A}(x, Q_0) = f_i^{p/A}(x; c_0, c_1, \dots) = c_0 x^{c_1} (1-x)^{c_2} P(x; c_3, \dots)$$

with  $c_j = c_j(A) \stackrel{\text{nCTEQ}}{=} p_k + a_k (1 - A^{-b_k})$  depending on the nuclei.

3. Use DGLAP equation to evolve  $f_i(x, \mu)$  from  $\mu = Q_0$  to  $\mu = Q_{\max}$ .
4. Calculate theory predictions corresponding to the data ( $\sigma_{\text{DIS}}$ ,  $\sigma_{\text{DIS}}$ , etc.).
5. Calculate appropriate  $\chi^2$  function – compare data and theory

$$\chi^2(\{c_i\}) = \sum_{\text{experiments}} w_n \chi_n^2(\{c_i\})$$

$$\chi_n^2(\{c_i\}) = \sum_{\text{data points}} \left( \frac{\text{data} - \text{theory}(\{c_i\})}{\text{uncertainty}} \right)^2$$

6. Minimize  $\chi^2$  function with respect to parameters  $c_0, c_1, \dots$

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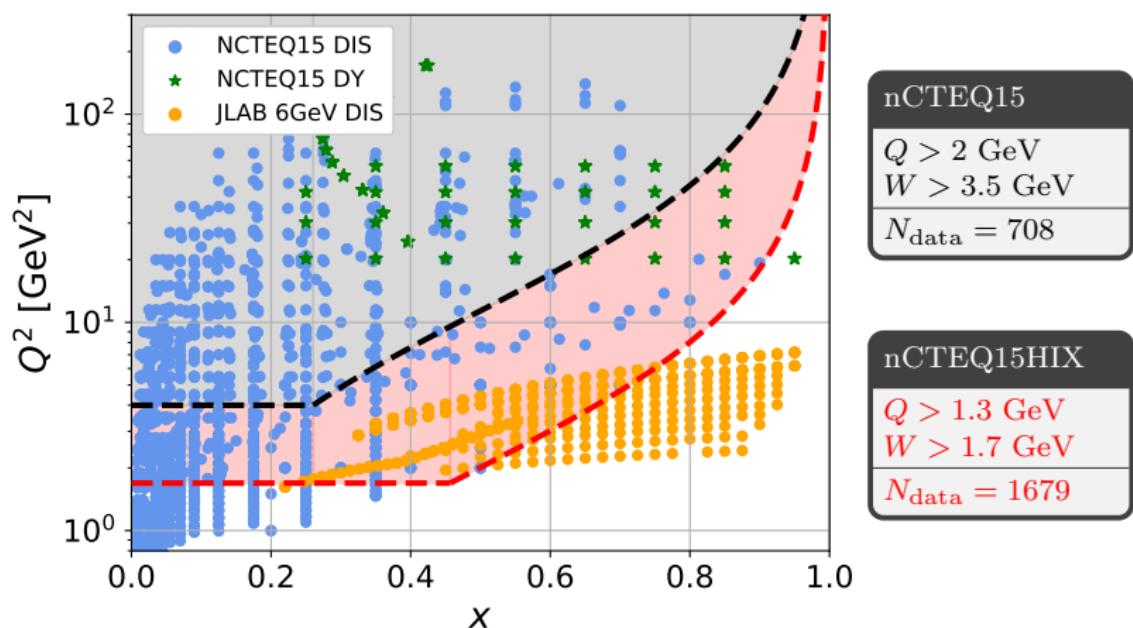
## Data in nPDF analyses [nCTEQ15HIX: PRD 103, 114015 (2021)]

In (n)PDF analyses we use kinematic cuts to exclude data that are

- in *non-perturbative region*
- have significant *higher-twist corrections*

$$\mathcal{O}\left(\frac{\Lambda_{\text{QCD}}^2}{Q^2}\right)$$

This is typically done by *kinematic cuts* on  $Q^2$  and  $W^2 = Q^2 \frac{1-x}{x} + M_N^2$



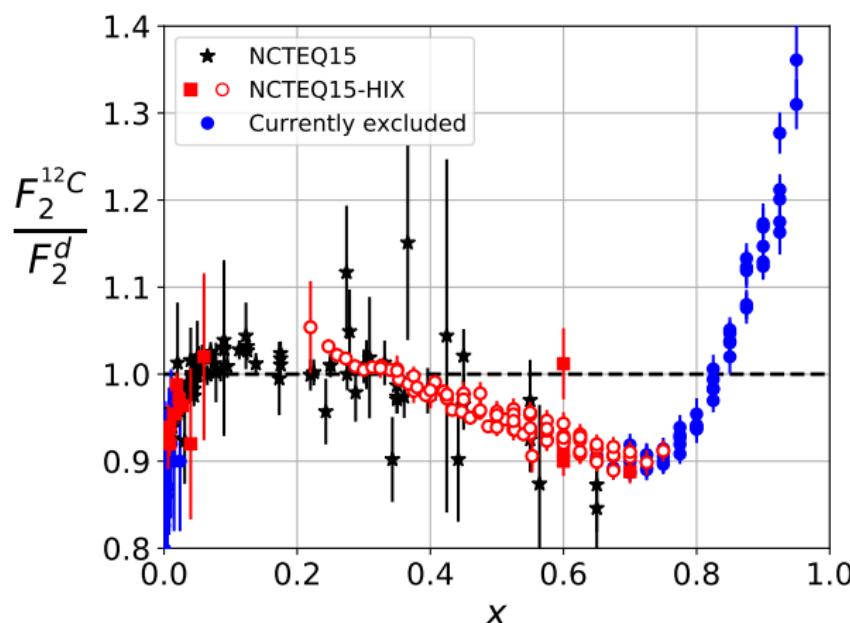
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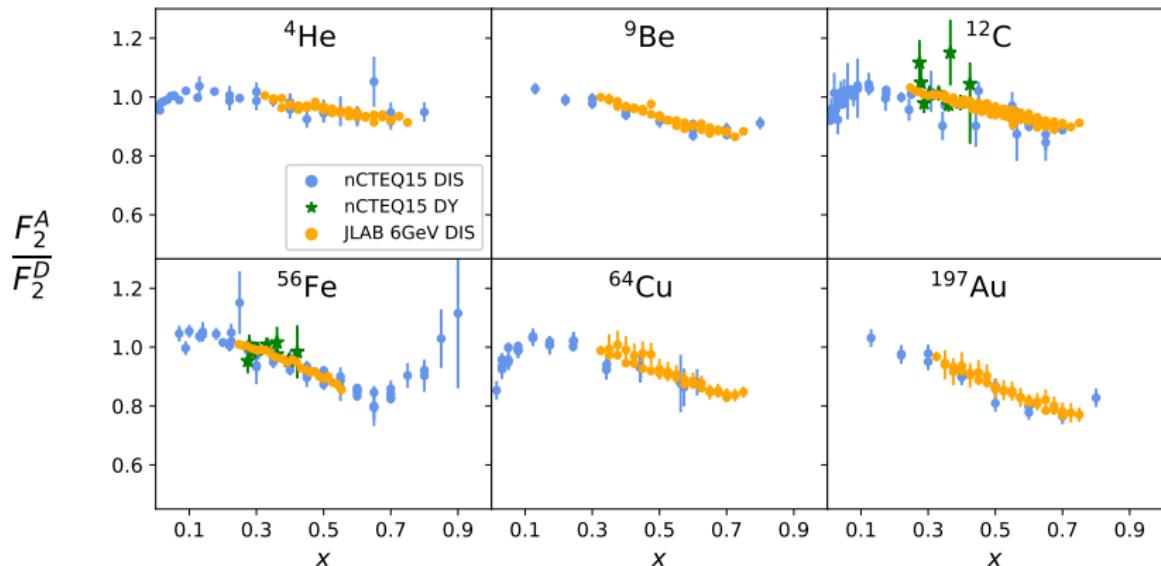
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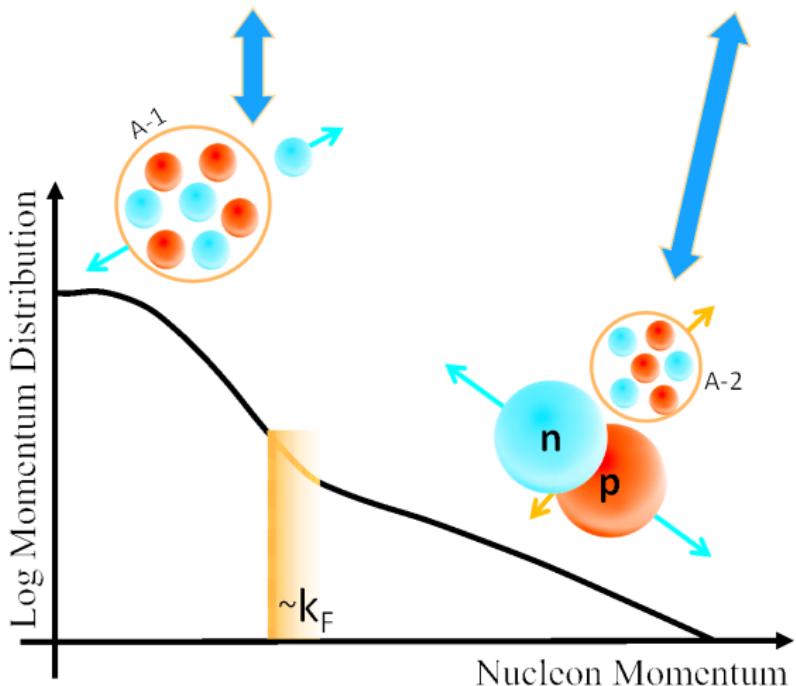




- ▶ JLAB data are mostly in EMC region
- ▶ The EMC region is directly connected with Short Range Correlatation (SRC) models.

# Short Range Correlation (SRC) picture of nuclei

Bound = 'Quasi-Free' + Modified SRCs



[Or Hen, 4th International Workshop on Quantitative Challenges  
in SRC & EMC Effect Research, CEA France, 03/02/2023.]

## Standard nPDF parametrization

1. One of the standard ways of parametrizing nuclear PDFs (nPDFs) is by extending the proton PDF parametrizations to account for  $A$ -dependence.
2. E.g. in the nCTEQ group:
  - ▶ *PDF of nucleus* ( $A$  - mass,  $Z$  - charge,  $N$  - number of neutrons)

$$f_i^{(A, Z)}(x, Q) = \frac{Z}{A} f_i^{p/A}(x, Q) + \frac{N}{A} f_i^{n/A}(x, Q)$$

- ▶ bound proton PDFs are parametrized

$$x f_i^{p/A}(x, Q_0) = x^{c_1} (1 - x)^{c_2} P(x, \{c_k\})$$

- ▶ bound neutron PDFs are constructed assuming *isospin symmetry*
- ▶  $A$ -dependence

$$c_k \rightarrow c_k(\textcolor{red}{A}) \equiv p_k + a_k \left( 1 - \textcolor{red}{A}^{-b_k} \right)$$

### 3. Sum rules

$$\int_0^1 dx f_{u_v}^{p/A}(x, Q) = 2, \quad \int_0^1 dx f_{d_v}^{p/A}(x, Q) = 1, \quad \int_0^1 dx \sum_i x f_i^{p/A}(x, Q) = 1.$$

# SRC inspired parametrization

- ▶ **Short Range Correlations (SRC)** pairs can have isospin  $I = 0, 1$ , possible configurations:  $(pn)$ ,  $(pp)$ ,  $(nn)$
- ▶ Partonic content of SRC pairs could be expressed as a convolution of distributions of a parton inside a nucleon and a nucleon inside a pair, then the distribution of the full nucleus:

$$f_i^A = \frac{Z}{A} \left[ (1 - [C_A^{(pp)} + C_A^{(pn)}]) f_{i/p} + C_A^{(pp)} f_{\text{SRC}}^{p/(pp)} \otimes f_{i/p} + C_A^{(pn)} f_{\text{SRC}}^{p/(pn)} \otimes f_{i/p} \right]$$
$$+ \frac{N}{A} \left[ (1 - [C_A^{(nn)} + C_A^{(pn)}]) f_{i/n} + C_A^{(nn)} f_{\text{SRC}}^{n/(nn)} \otimes f_{i/n} + C_A^{(pn)} f_{\text{SRC}}^{n/(pn)} \otimes f_{i/n} \right]$$

- ▶ For phenomenological purpose we can simplify it assuming:

$$f_{i/p}^{\text{SRC}} \equiv [f_{\text{SRC}}^{p/(pp)} + f_{\text{SRC}}^{p/(pn)}] \otimes f_{i/p}$$

$$C_A^p \equiv C_A^{(pp)} + C_A^{(pn)}$$

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- ▶ As a consequence we will be able to determine only total number of paired neutrons and protons.

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# SRC inspired parametrization

Our **phenomenological SRC inspired parametrization** takes form:

$$f_i^A(x, Q) = \frac{Z}{A} \left[ (1 - C_A^p) f_{i/p}(x, Q) + C_A^p f_{i/p}^{\text{SRC}}(x, Q) \right] \\ + \frac{N}{A} \left[ (1 - C_A^n) f_{i/n}(x, Q) + C_A^n f_{i/n}^{\text{SRC}}(x, Q) \right]$$

with  $f_{i/p}(f_{i/n})$  being the free proton (neutron) PDFs and  $f_{i/p}^{\text{SRC}}(f_{i/n}^{\text{SRC}})$  the effective SRC proton (neutron) distributions.

The full nPDF  $f_i^A$  need to fulfill:

1. DGLAP evolution.
2. Momentum and number sum rules:

$$\int_0^1 dx x f_i^A(x, Q) = 1, \quad \int_0^1 dx f_{uv}^A(x, Q) = \frac{A + Z}{A}, \quad \int_0^1 dx f_{dv}^A(x, Q) = \frac{A + N}{A}.$$

We assume that both  $f_{i/n}$  and  $f_{i/n}^{\text{SRC}}$  can be determined using isospin symmetry. We also restrict  $f_{i/p}^{\text{SRC}}(f_{i/n}^{\text{SRC}})$  (and  $f_i^A$ ) to be define on  $x \in (0, 1)$ , then  $f_{i/p}^{\text{SRC}}(f_{i/n}^{\text{SRC}})$ :

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with  $f_{i/p}(f_{i/n})$  being the free proton (neutron) PDFs and  $f_{i/p}^{\text{SRC}}(f_{i/n}^{\text{SRC}})$  the effective SRC proton (neutron) distributions.

For the purpose of global analysis we:

- ▶ fix the free proton PDFs to the nCTEQ15 proton,
- ▶ parametrize the SRC PDFs as:

$$x f_{i/p}^{\text{SRC}}(x, Q_0) = x^{c_1} (1 - x)^{c_2} e^{c_3 x} (1 + e^{c_4 x})^{c_5}$$

Free parameters:

- ▶  $x$ -shape: set of  $\{c_k\}$  parameters for each flavour (total of 21),
- ▶  $A$ -dependence: pairs of  $(C_A^p, C_A^n)$  parameters which are independent for each nuclei (instead we could use nuclear model to constrain them).

## Data & Fits

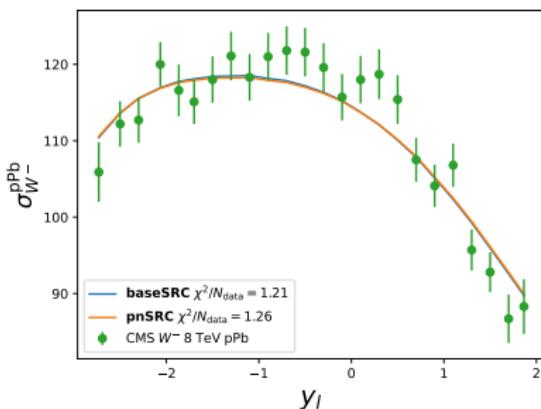
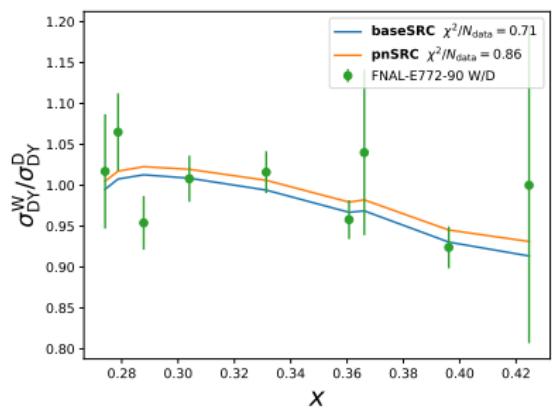
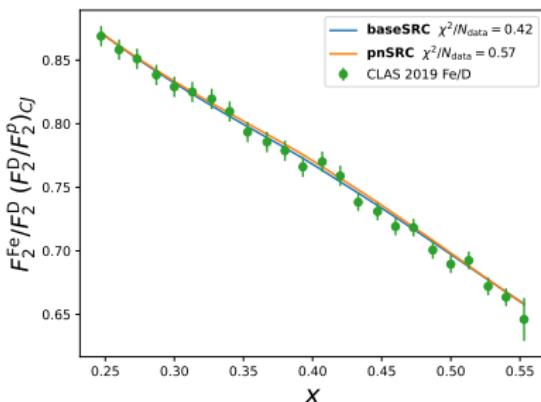
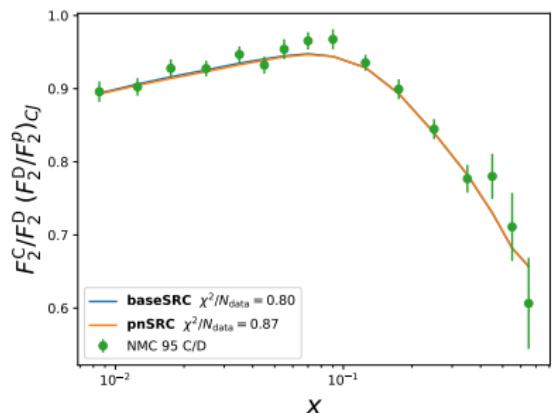
Used data:

- ▶ all DIS & DY data used in the nCTEQ15 analysis [[PRD 93, 085037 \(2016\)](#)],
- ▶ high- $x$  DIS data from JLAB which we used in the nCTEQ15hix analysis [[PRD 103, 114015 \(2021\)](#)],
- ▶  $p\text{Pb}$  data for  $W/Z$  production from the LHC used in the nCTEQ15WZ analysis [[EPJC 80, 968 \(2020\)](#)].

Performed fits:

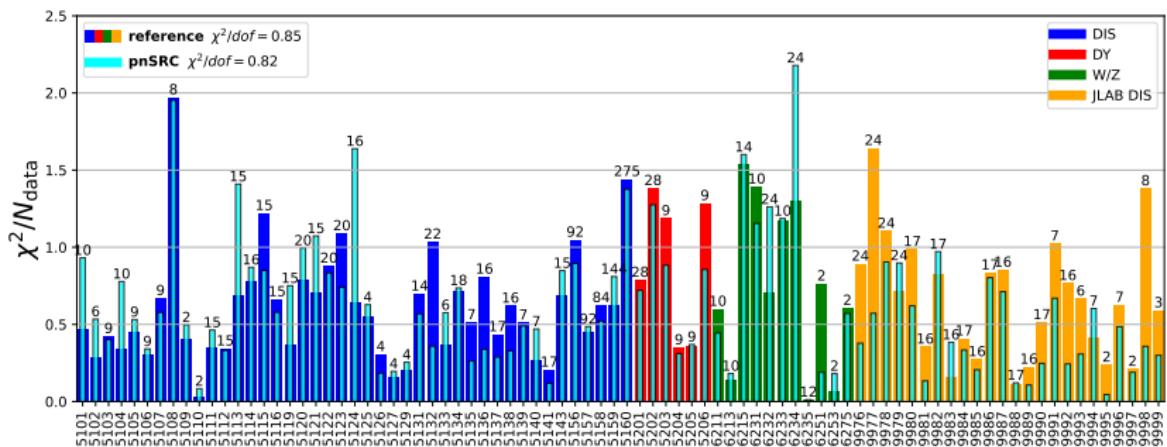
- ▶ **Reference**— fit using standard nCTEQ PDF fitting framework,
- ▶ **baseSRC**— use SRC parametrization, keep  $C_A^p$  and  $C_A^n$  parameters **independent**,
- ▶ **pnSRC**— use SRC parametrization, **tie together**  $C_A^p$  and  $C_A^n$ .

# Results – very good data description

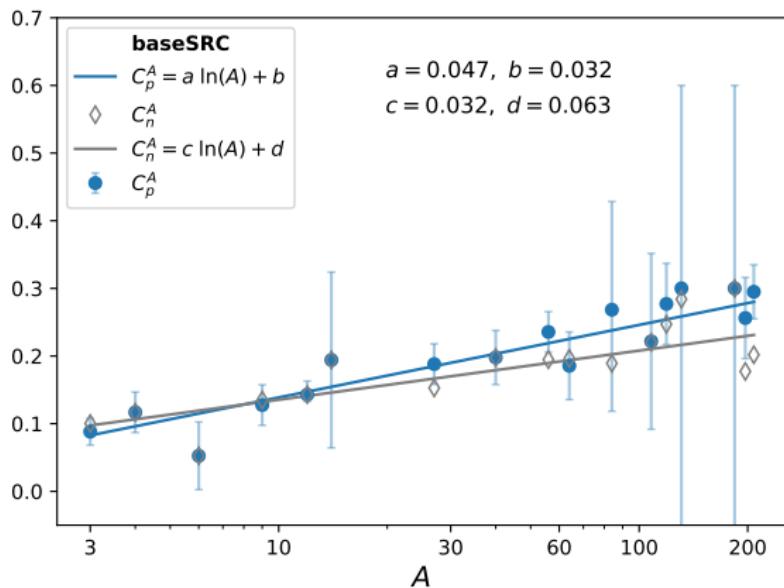


# Results – very good data description

$\chi^2/N_{\text{data}}$	DIS	DY	$W/Z$	JLab	$\chi^2_{\text{tot}}$	$\frac{\chi^2_{\text{tot}}}{N_{\text{DOF}}}$
Reference	0.85	0.97	0.88	0.72	1408	0.85
baseSRC	0.84	0.75	1.11	0.41	1300	0.80
pnSRC	0.85	0.84	1.14	0.49	1350	0.82



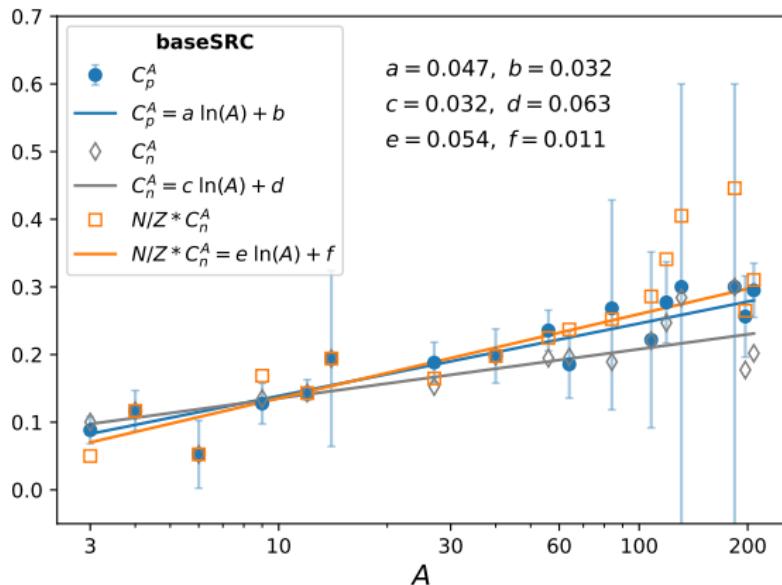
## Results: $A$ -dependence of the $(C_A^p, C_A^n)$ parameters



The number of protons and neutrons in SRC pairs is approximately equal, e.g.

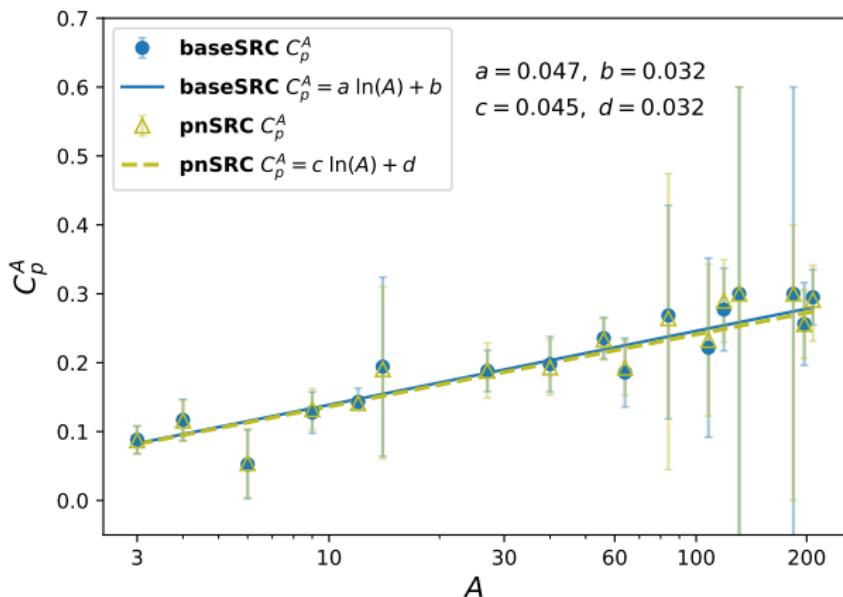
- $^{197}\text{Au}$  ( $C_A^p=0.256, C_A^n=0.178$ ):  $79 \times C_A^p \approx 20.2$  protons and  $118 \times C_A^n \approx 21.0$  neutrons.
- $^{208}\text{Pb}$  ( $C_A^p=0.295, C_A^n=0.202$ ):  $82 \times C_A^p \approx 24.2$  protons and  $126 \times C_A^n \approx 25.5$  neutrons.

## Results: $A$ -dependence of the $(C_A^p, C_A^n)$ parameters



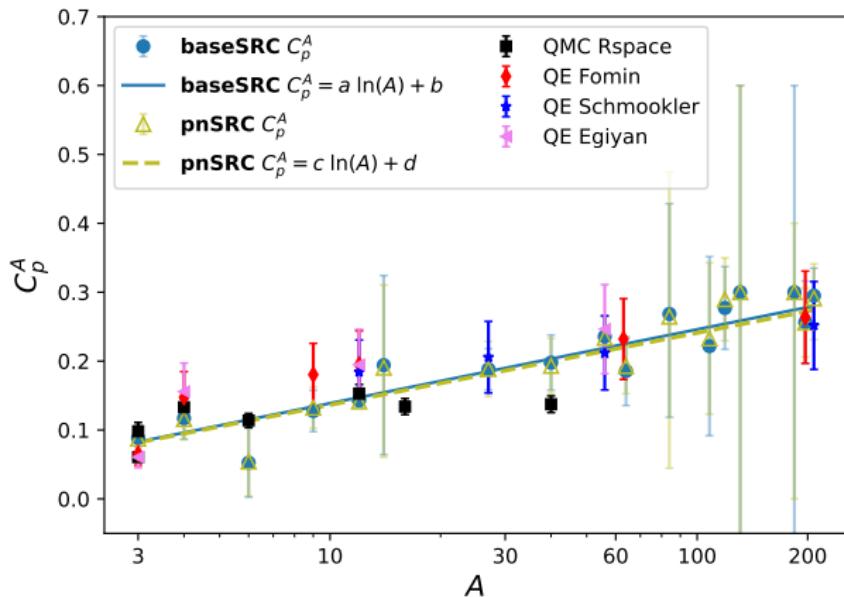
- ▶ Correcting for the access of neutrons we obtained a very comparable numbers of protons and neutrons bounded in the SRC pairs.
- ▶ This is **consistent** with the hypothesis that the **SRC pairs are dominantly proton-neutron combinations**.
- ▶ We can use this observation to restrict number of fit parameters by linking  $C_A^n = (Z/N)C_A^p$ .

## Results - pnSRC fit with $C_A^n = (Z/N)C_A^p$



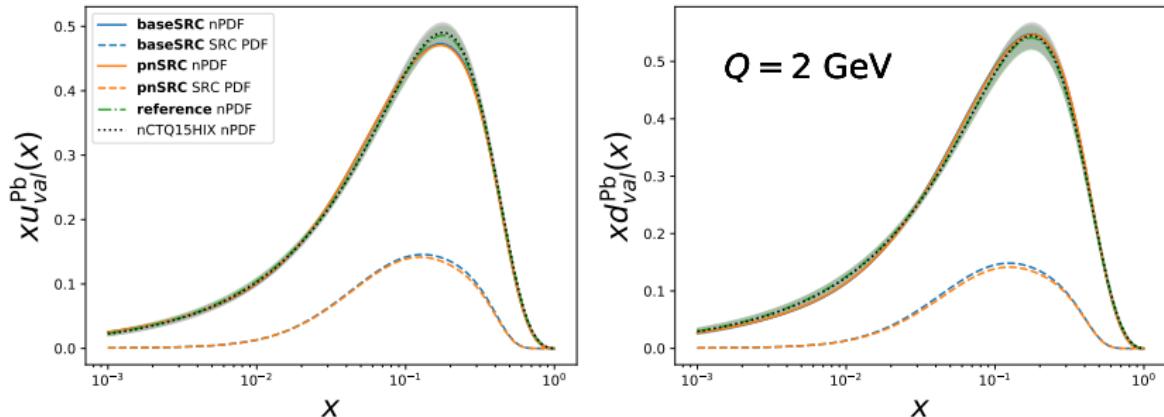
- The obtained  $C_A^p$  values are nearly the same as for the **baseSRC** fit.
- Fit quality is very comparable  $\chi^2/N_{\text{DOF}} = 0.82$  (vs  $\chi^2/N_{\text{DOF}} = 0.8$ ).

## Results - pnSRC fit with $C_A^n = (Z/N)C_A^p$



- ▶ Results of Quantum Monte Carlo calculations (QMC) [Nature Physics 17, 306-310 (2021)]
- ▶ Results of measurements in quasi-elastic region:
  - ▶ Fomin [Nature 566, 354-358 (2019)]
  - ▶ Schmookler [Phys. Rev. Lett. 96, 082501 (2006)]
  - ▶ Egiyan [Phys. Rev. Lett. 108, 092502 (2012)]

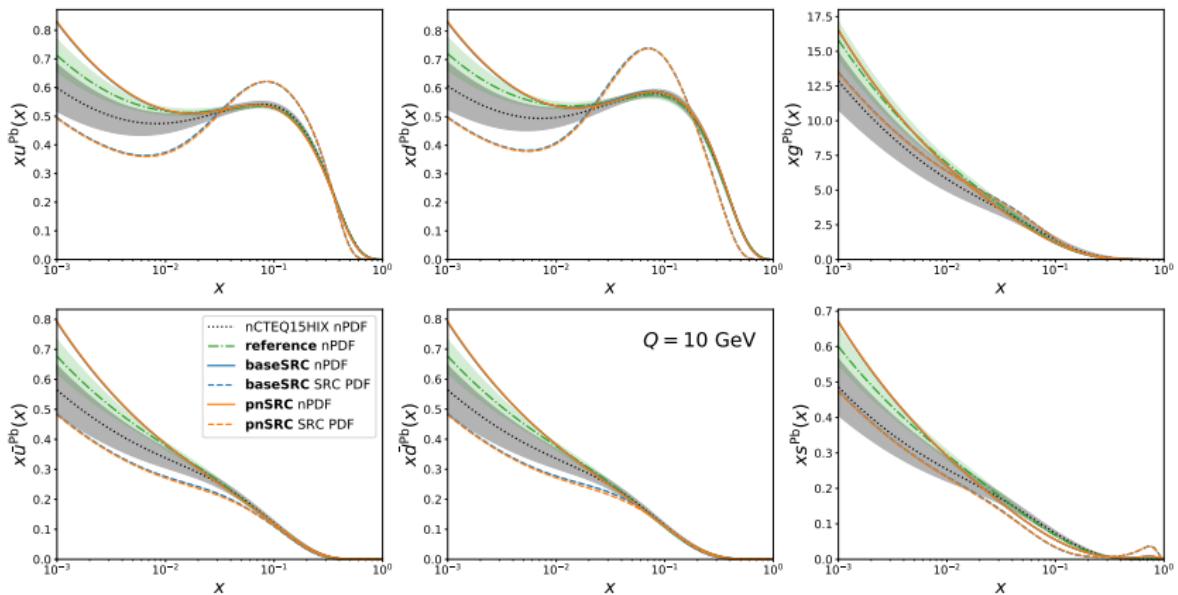
## Results: PDFs



- nPDFs obtained from SRC fits lie within the error bands of the **Reference** fit.
- The SRC components of the full nPDFs are in the range 20% to 30% – in agreement with the  $\{C_A^p, C_A^n\}$  values.

$$f_i^A(x, Q) = \frac{Z}{A} \left[ (1 - C_A^p) f_{i/p}(x, Q) + C_A^p f_{i/p}^{\text{SRC}}(x, Q) \right] \\ + \frac{N}{A} \left[ (1 - C_A^n) f_{i/n}(x, Q) + C_A^n f_{i/n}^{\text{SRC}}(x, Q) \right]$$

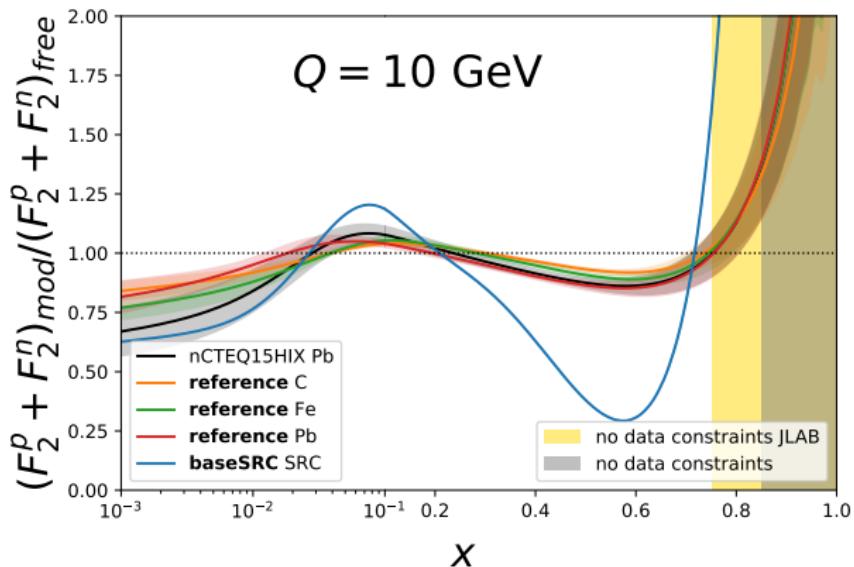
## Results: PDFs



- ▶ Clearly “exaggerated” modifications for pure SRC distribution.

$$f_i^A(x, Q) = \frac{Z}{A} \left[ (1 - C_A^p) f_{i/p}(x, Q) + C_A^p f_{i/p}^{\text{SRC}}(x, Q) \right] \\ + \frac{N}{A} \left[ (1 - C_A^n) f_{i/n}(x, Q) + C_A^n f_{i/n}^{\text{SRC}}(x, Q) \right]$$

## Results: modification of $F_2$ structure function



- ▶ Clearly “exaggerated” modifications for pure SRC distribution.

## Summary

- ▶ The simple SRC-based picture of nPDFs leads to comparable or better data description than the traditional nPDF parameterization.
- ▶ The obtained values of  $\{C_A^p, C_A^n\}$  suggest approximately equal number of protons and neutrons in the SRC pairings which is consistent with other observations *pn-dominance in SRC pairs*.
- ▶ Even when the  $\{C_A^p, C_A^n\}$  parameters are constrained in the pnSRC fit, we obtain a very good fit to the data, yielding lower  $\chi^2$  than in the Reference fit. This can be used to further constrain the used parametrization.
- ▶ It is notable that all the above results, obtained from purely data driven fits, seem to support the SRC-based description of nuclei.
- ▶ The obtained SRC distributions feature “exaggerated” modifications compared to the full nPDFs.