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# Spin-Induced Heavy-Quark Interactions and Transport in the QGP

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# Outline

1. Introduction to T-matrix approach
2. Role of spin in vacuum spectroscopy of heavy-quarkonium
3. Impact on heavy-quark transport coefficient in QGP
4. Summary

# 1.1 T-Matrix Approach

[F. Riek+R. Rapp '10]  
[S. Liu+R. Rapp '18]

- Quantum many-body approach to quarkonium in vacuum and medium

$$T_{ij} = V_{ij} + \int V_{ij} G_i G_j T_{ij}$$

Dyson-Schwinger type self-consistent problem

- $G_i = 1/[\omega - \omega_k - \Sigma_i]$ : 1-body propagator

Self-energy:

- $V_{ij}$ : potential (input of T-matrix)

- Vacuum potential (Cornell):  $V = -\frac{4}{3} \alpha_s \frac{1}{r} + \sigma r$

- In-medium potential constrained by  $Q\bar{Q}$  free energy from lattice QCD
- Motivation: introducing spin-dependent potentials to account for  $Q\bar{Q}$  hyper-/fine splittings

# 1.2 Corrections to Potential

- Relativistic corrections

- Breit correction:  $V = RV^{vec} + V^{sca}$ ,

$$\text{with } R = \sqrt{\frac{\epsilon_i(\mathbf{p})\epsilon_j(\mathbf{p})}{M_i M_j}} \sqrt{1 + \frac{p^2}{\epsilon_i(\mathbf{p})\epsilon_j(\mathbf{p})}} \sqrt{\frac{\epsilon_i(\mathbf{p}')\epsilon_j(\mathbf{p}')}{M_i M_j}} \sqrt{1 + \frac{p'^2}{\epsilon_i(\mathbf{p}')\epsilon_j(\mathbf{p}')}}$$

relativistic correction  
for the vector interaction

$$V^{vec} = V_{Coul}$$

$$\text{Common assumption: } V^{sca} = V_{conf}$$

[N. Brambilla+A. Vairo '97]

[A. Szczepaniak et al. '96, '97]

[D. Ebert et al. '98, '03]

$$\leftarrow \text{Improved assumption: } V^{vec} = V_{Coul} + (1 - \chi)V_{conf}, V^{sca} = \chi V_{conf}$$

↓  
mixing coefficient (proportion of scalar component in  $V_{conf}$ )

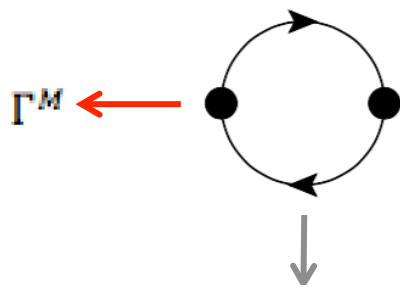
- Higher order in  $1/M_Q$ :  $V = RV^{vec} + V^{sca} + V^{LS} + V^{SS} + V^T$

$$\text{spin-orbit: } V^{LS} = \frac{1}{2M_Q^2 r} \langle \mathbf{L} \cdot \mathbf{S} \rangle \left( 3 \frac{d}{dr} V^{vec} - \frac{d}{dr} V^{sca} \right) \quad \text{spin-spin: } V^{SS} = \frac{3}{3M_Q^2} \langle \mathbf{S}_1 \cdot \mathbf{S}_2 \rangle \Delta V^{vec}$$

$$\text{tensor: } V^T = \frac{1}{12M_Q^2} S_{12} \left( \frac{1}{r} \frac{d}{dr} V^{vec} - \frac{d^2}{dr^2} V^{vec} \right)$$

# 2.1 Correlation/Spectral Functions

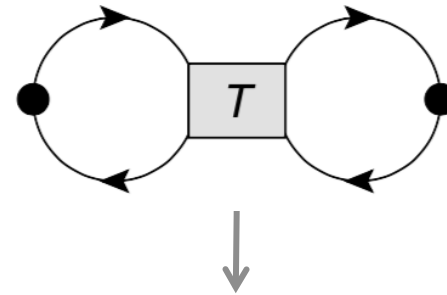
- Quarkonium mass read from spectral functions
- Spectral functions:  $\sigma(E) = -\frac{1}{\pi} \text{Im}[G_0(E) + G_{\text{int}}(E)]$
- Correlation functions:



$$G_0(E) \sim \Gamma^M G_{Q\bar{Q}}^0(E, p) \Gamma^M$$

non-interacting (free) part

+



$$G_{\text{int}}(E) \sim \Gamma^M G_{Q\bar{Q}}^0(E, p) G_{Q\bar{Q}}^0(E, p') \Gamma^M T_{Q\bar{Q}}(E, p, p')$$

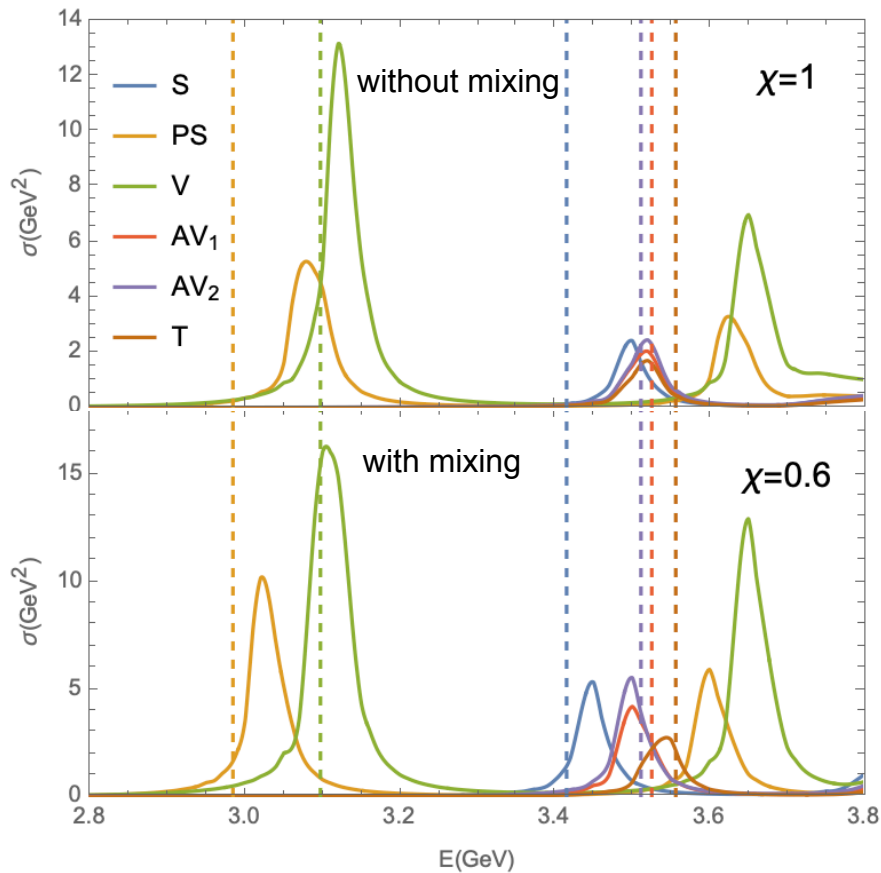
interacting part

	scalar (S)	pseudoscalar (PS)	vector (V)	axial-vector (AV)	tensor (T)
$\Gamma^M$	1	$i\gamma_5$	$\gamma^\mu$	$\gamma^\mu \gamma_5$	$i[\gamma^\mu, \gamma^\nu]/2$

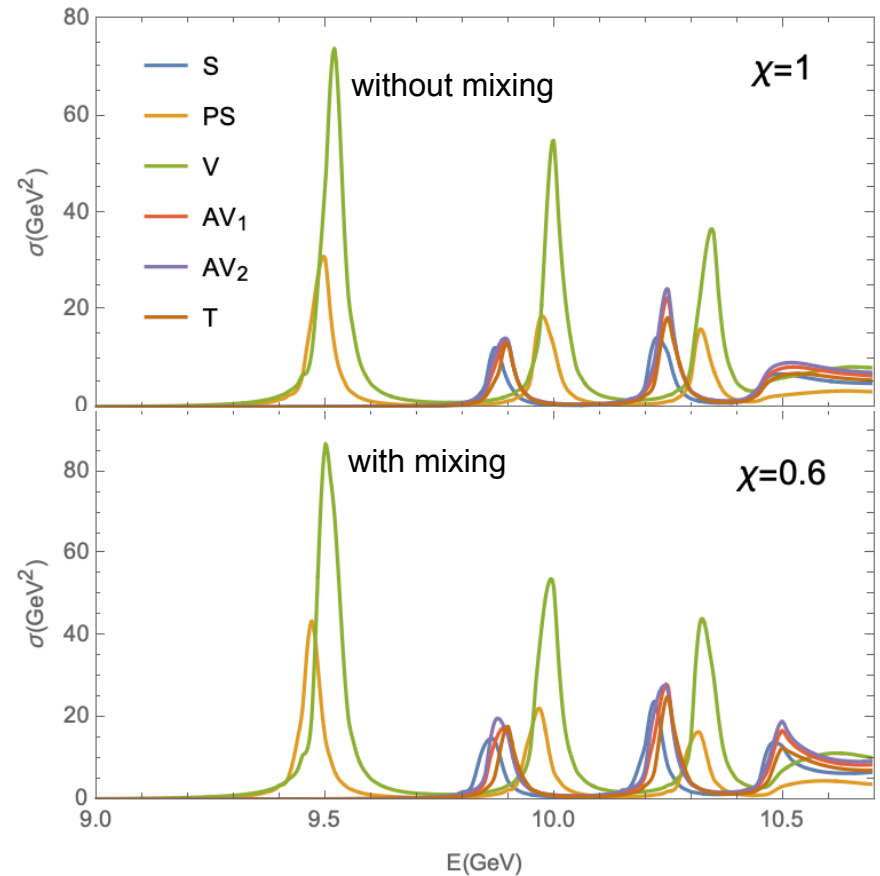
- S-wave (PS, V) and P-wave (S, AV, T) states degenerate without spin-related ( $1/M_Q$ ) corrections

## 2.2 Quarkonium Vacuum Spectroscopy

### Charmonium

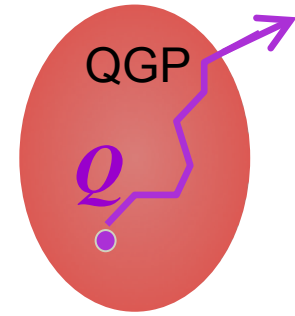


### Bottomonium



- Mass splittings significantly improved by mixing effect
- Less significant for bottomonium ( $1/M_b < 1/M_c$ )

# 3.1 In-Medium Charm-Quark Transport



- Fokker-Planck equation

$$\frac{\partial}{\partial t} f(\mathbf{p}, t) = \frac{\partial}{\partial p_i} \left\{ A(\mathbf{p}) p_i f(\mathbf{p}, t) + \frac{\partial}{\partial p_j} [B_{ij}(\mathbf{p}) f(\mathbf{p}, t)] \right\}$$

thermal relaxation rate  
(friction coefficient)

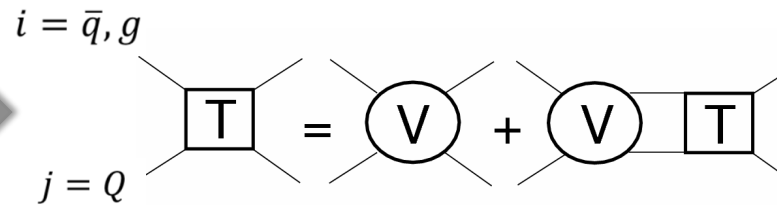
momentum diffusion coefficient

Brownian motion for heavy quarks through the QGP

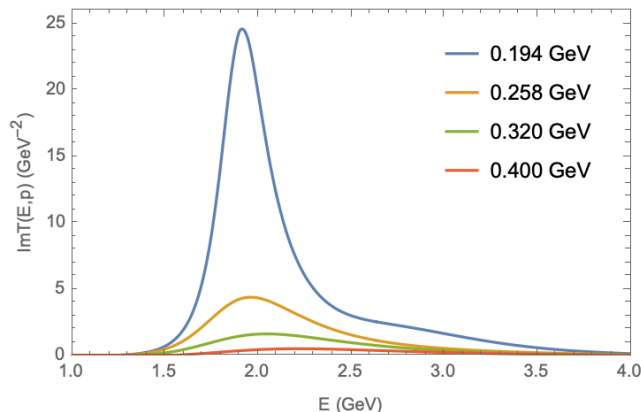
$$A(\mathbf{p}) \sim \sum_i \int d^4 p' d^4 q d^4 q' |T_{Qi}|^2 \left( 1 - \frac{\mathbf{p} \cdot \mathbf{p}'}{p^2} \right)$$

spatial diffusion coefficient:  $D_s = \frac{T}{M_Q A(\mathbf{p} \rightarrow 0)}$

- $T_{Qi}$ : heavy-light T-matrices



Prediction for D-meson from T-matrix approach



As temperature decreases...

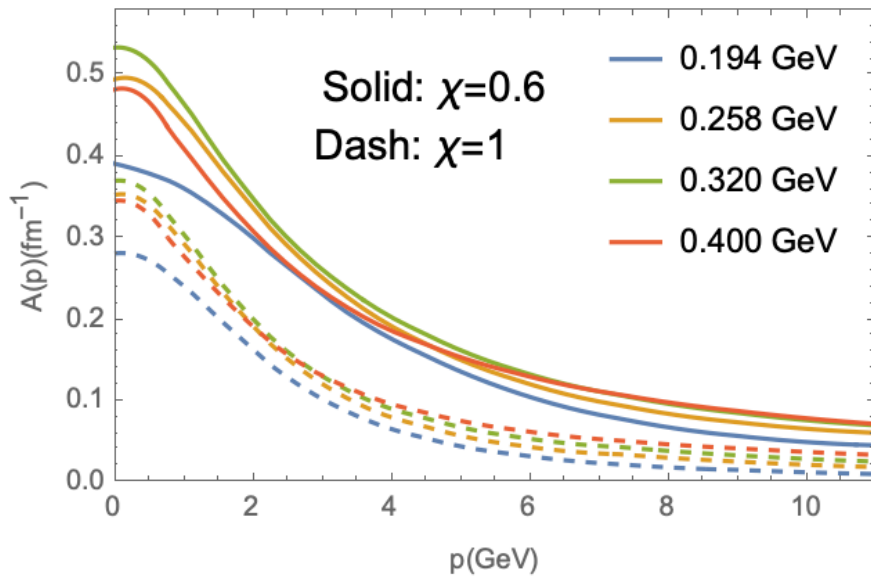
- Screening for potential decreases
- Confining force appears
- D-meson emerges (with reasonable mass at  $\sim T_c$ )



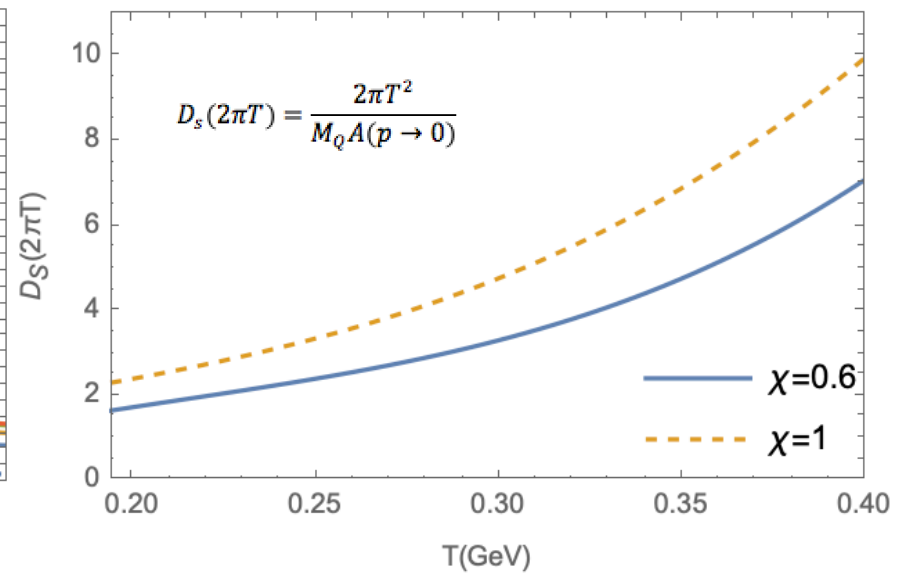
important for  $D_s$  at  $\sim T_c$

## 3.2 In-Medium Charm-Quark Transport

- Transport coefficients :



Friction coefficients



Spatial diffusion coefficients

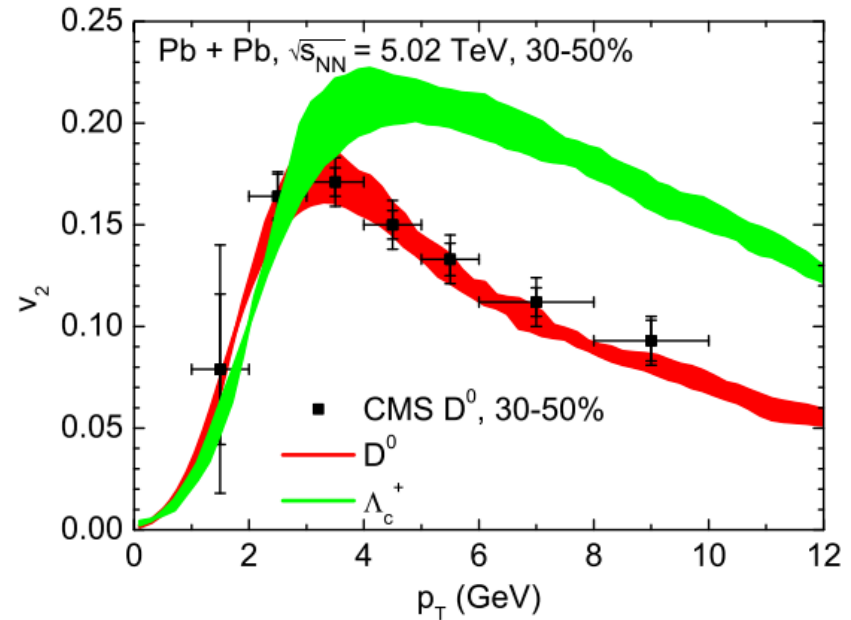
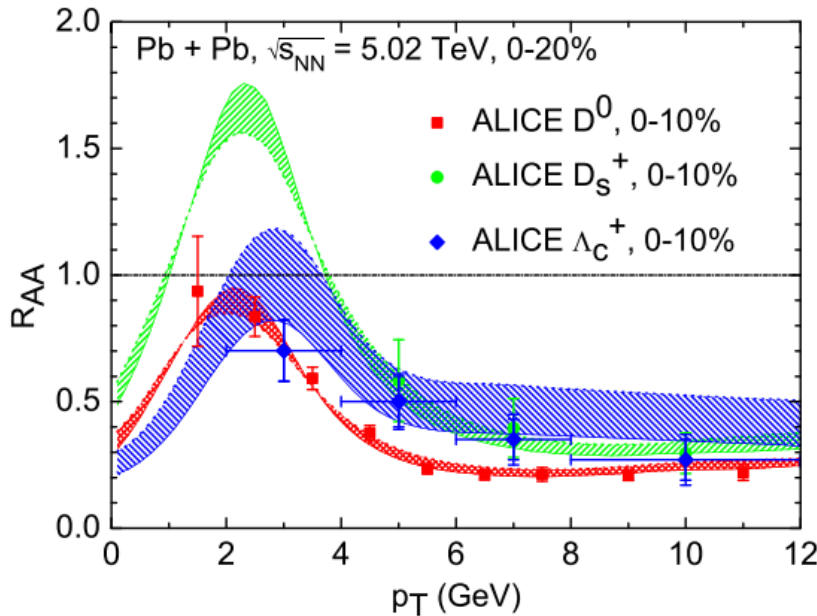
- Increase in  $A(p)$  + harder dependence on momentum

→ important ramifications for the phenomenology of **open heavy flavor probes** in URHICs.



## 3.3 Connection to Experimental Observables

- A good description of  $D$ ,  $D_s$  and  $\Lambda_c$  observables in heavy-ion collisions



[M. He+R. Rapp '20]

- Using T-matrix with U-potential as input + an extra  $K \approx 1.6$
- Mixing effect (larger  $A(p)$ ) promising to explain K factor

# 4. Summary

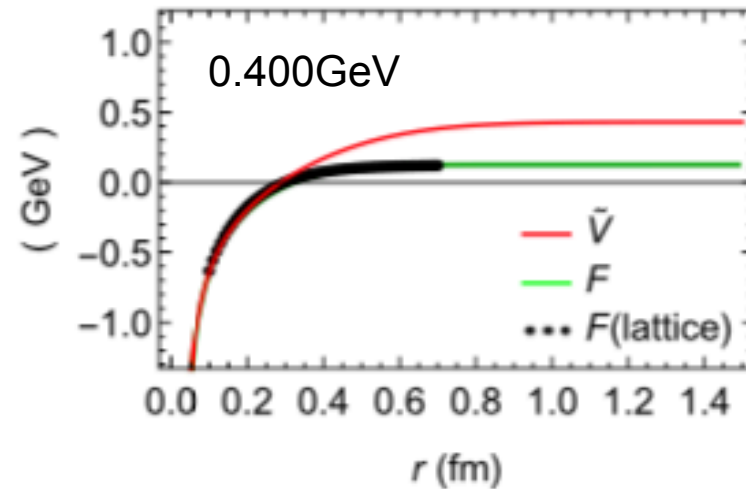
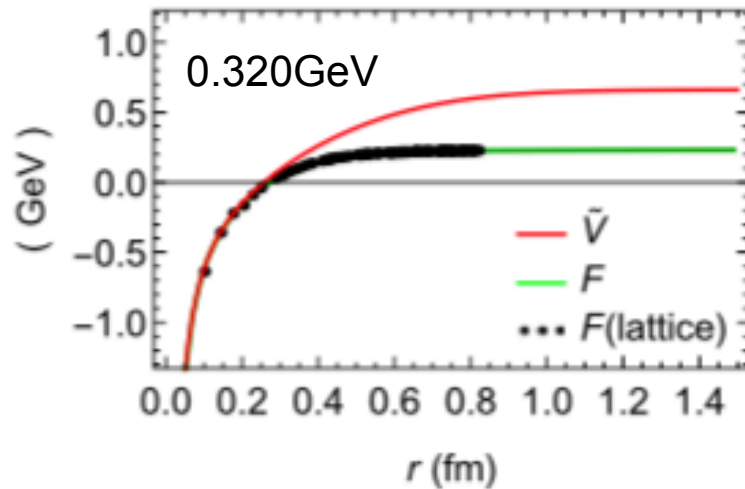
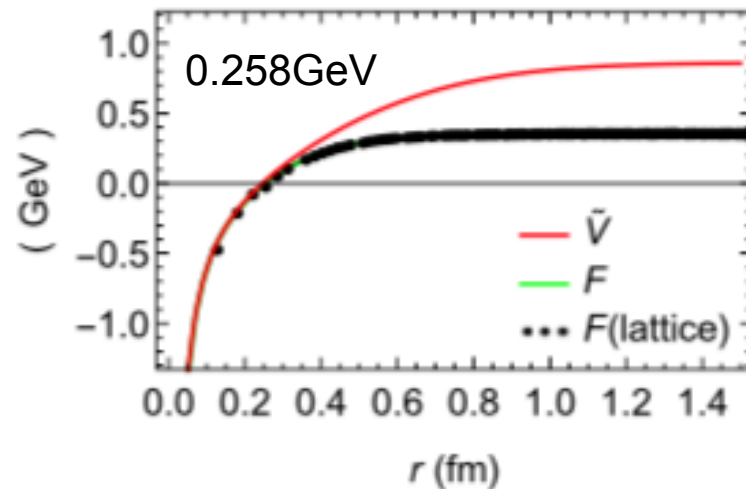
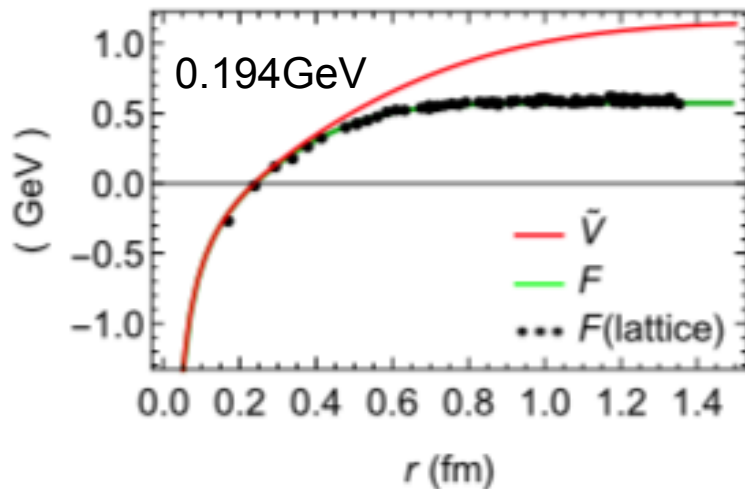
- Extending T-matrix approach to include **spin-induced interactions** in vacuum
- Introducing **vector component** in confining potential  $V_{\text{conf}}$
- Vacuum charmonium and bottomonium mass splittings improve
- Friction coefficients for charm quarks in the QGP enhanced, especially at high momenta (consequence of the enhancement from extra relativistic correction factor for the vector component of  $V_{\text{conf}}$ )

# Thanks for Your Attention!

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# Fit to $Q\bar{Q}$ Free Energy



[S. Liu+R. Rapp '18]

# $D^0$ - $D^*$ Splitting in Vacuum

